

# Computer Architecture: Gates and Wires

Truth tables

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# Truth Tables to Boolean Algebra

INPUTS		OUT
A	B	R
0	0	0
0	1	1
1	0	1
1	1	0



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$(!A).B$

$A.(!B)$



# Truth Tables to Boolean Algebra

INPUTS		OUT
A	B	R
0	0	0
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1	0	1
1	1	0

$$\begin{array}{l} (!A).B \\ A.(!B) \end{array}$$

$$(!A).B + A.(!B) = R$$



# Truth Tables to Boolean Algebra

INPUTS		OUT
A	B	R
0	0	0
0	1	1
1	0	1
1	1	0

$$A = 0, B = 0: (\bar{0}).0 + 0.(\bar{0}) = 1.0 + 0.1 = 0 + 0 = 0$$

$$A = 0, B = 1: (\bar{0}).1 + 0.(\bar{1}) = 1.1 + 0.0 = 1 + 0 = 1$$

$$A = 1, B = 0: (\bar{1}).0 + 1.(\bar{0}) = 0.0 + 1.1 = 0 + 1 = 1$$

$$A = 1, B = 1: (\bar{1}).1 + 1.(\bar{1}) = 0.1 + 1.0 = 0 + 0 = 0$$

$$(\bar{A}).B$$

$$A.(\bar{B})$$

$$(\bar{A}).B + A.(\bar{B}) = R$$



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$(\bar{A}).B$

$A.(\bar{B})$

$$(\bar{A}).B + A.(\bar{B}) = R$$

Every truth table can be converted to a sum of products!



# Boolean Algebra to Circuit

$$(\neg A) \cdot B + A \cdot (\neg B) = R$$



# Boolean Algebra to Circuit

$$(\neg A) \cdot B + A \cdot (\neg B) = R$$

A 

B 

 R



# Boolean Algebra to Circuit

$$(\neg A) \cdot B + A \cdot (\neg B) = R$$

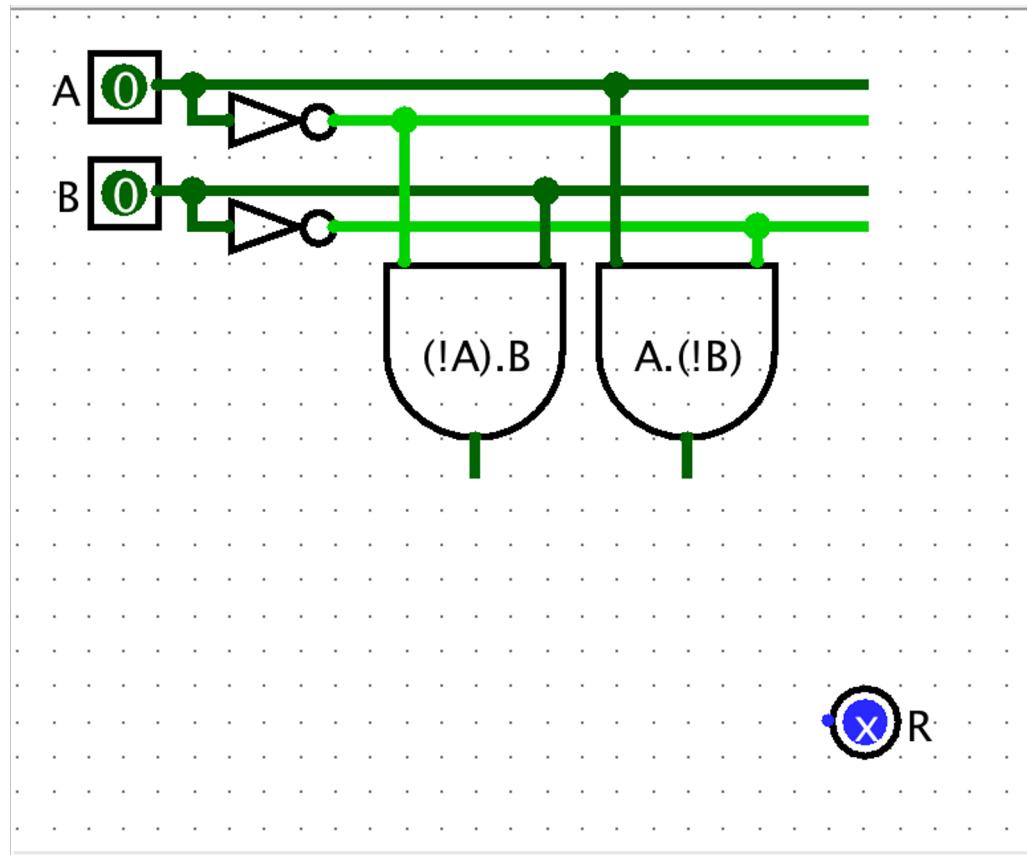


R



# Boolean Algebra to Circuit

$$(\neg A) \cdot B + A \cdot (\neg B) = R$$



# Boolean Algebra to Circuit

$$(\overline{A})B + A.\overline{B} = R$$

