



Synchronous Reactive Languages Lustre

Alexandre Denault
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- What's a Synchronous Reactive Language?
- A Introduction to Lustre
- Verification, Simulation and Execution
- A Simple Example
- Esterel

Synchronous Languages

■ What?

- ♦ Time is expressed as a series of external events.
- ♦ Events are processed at regular intervals.
- ♦ It's like having a clock.

■ Why?

- ♦ It's easier to implement in hardware.
- ♦ It's easier to verify.

■ Concerns

- ♦ If you want to simulate asynchronous behavior, you need to make sure your clock ticks are small enough.

Reactive Systems

■ What?

- ◆ Systems that have a relationship with their environments. (Harel)
- ◆ Their behavior is to react to external stimuli.

■ Why?

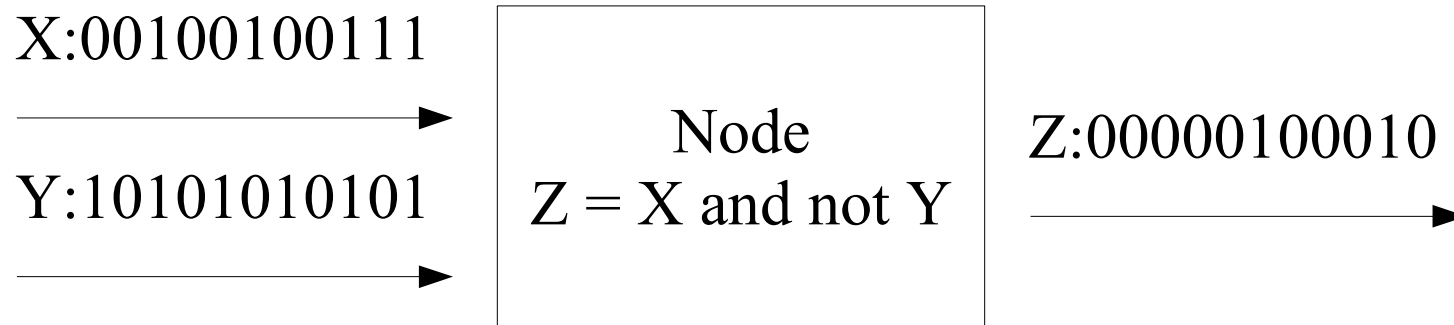
- ◆ Because reactive systems are easier to map onto hardware.

- First created in 1983.
- Commercially transformed to Scade in 1993 by Verilog.
- Esterel Technologies now own the rights to Scade.
- Active research is done by the Synchrone group from the Verimag research center.
- It is not a file system !

- Cases studies on Lustre
 - ◆ Electrical load distribution on A380 aircraft
 - ◆ Gyroscope in Indian Aircraft industry
 - ◆ Ariane v launcher, experimental version
- Companies using Scade (success stories)
 - ◆ Airbus
 - ◆ Pratt & Whitney
 - ◆ CS Canada
 - ◆ Eurocopter

Deeper look at Lustre

- A control module in Lustre is called a node.
- Lustre modules operate on streams.
- Streams can be booleans or numericals.



Syntax Examples

■ On boolean values:

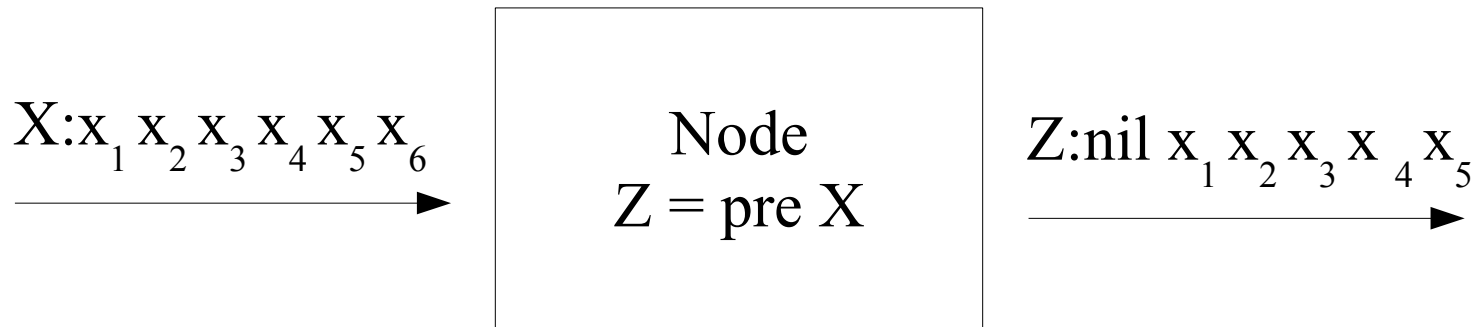
- $A = X \text{ and not } Y$
- $A = X \text{ xor } Y$
- $A = \text{if } X \text{ then } Y \text{ else } Z$

■ On numerical values

- $A = X + Y$
- $A = X - Y$
- $A = X \text{ div } Y$
- $A = \text{if } (X > Y) \text{ then } X \text{ else } Y$
- $A = \text{if } (X <> Z) \text{ then } X \text{ else } Y$

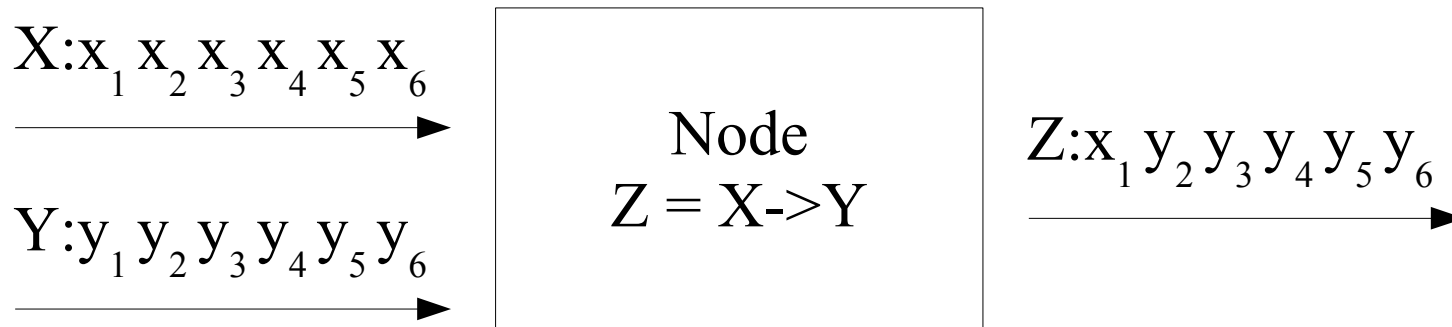
Pre Operator

- The pre operator allows us to refer the n position of a stream as the n-1 position of another stream.



-> Operator

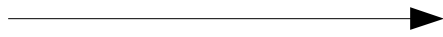
- The -> operator is used to initialize streams.



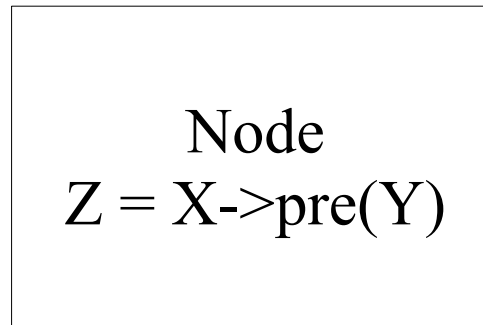
Pre and -> combined

- The Pre and -> operators are most useful when combined.

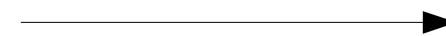
$X: x_1 x_2 x_3 x_4 x_5 x_6$

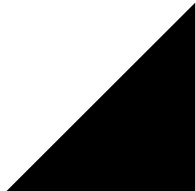


$Y: y_1 y_2 y_3 y_4 y_5 y_6$



$Z: x_1 y_1 y_2 y_3 y_4 y_5$



- **Verification:** We can run verifications on the model to insure that catastrophic situations cannot occur.
 - **Simulation:** We can use a simulator to verify that the model functions correctly.
 - **Execution:** We can generate code from the model, and then integrate that code into the target platform, where it will be executed.
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Verification

- We can establish safety properties for our system:
 - ◆ In a Y segment, only one car at a time should be merging in.
 - ◆ Landing gear should not retract while plane is landing.
- Verification is the action of insuring that these safety properties are never violated.
- In Lustre, safety properties are described as assertions, and must always be true.

Temporal Logic

- Describing certain assertions requires temporal logic.
Any occurrence of a critical situation causes an alarm, which must be sustained within a five seconds delay.
- This statement could be generalized to
Any occurrence of event A must cause the condition B to be true until the next occurrence of C.
- This requires knowledge of the future, which Lustre does not.
- However, this can be rewritten as
Any time A has occurred in the past, either B has been continuously true, or C has occurred at least once, since the last occurrence of A.

Various Forms of Lustre

Lustre: .lus

This contains the Lustre nodes in their textual format.

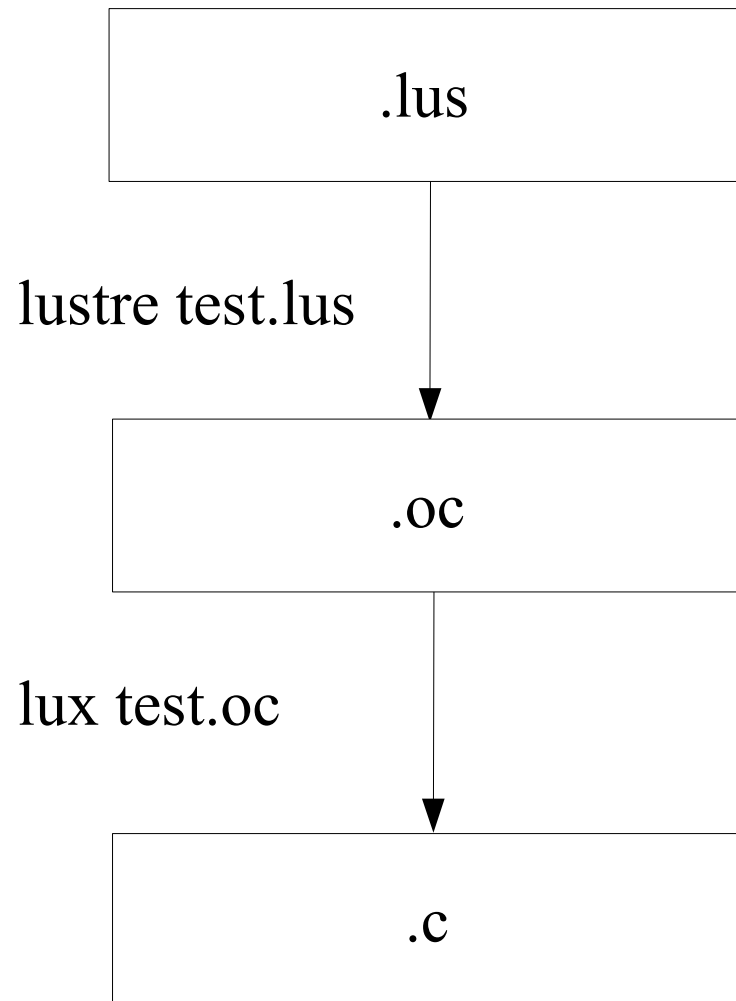
Lustre-Esterel Common Format: .oc

The Lustre application gets reduced to a FSA.

It can then be optimized.

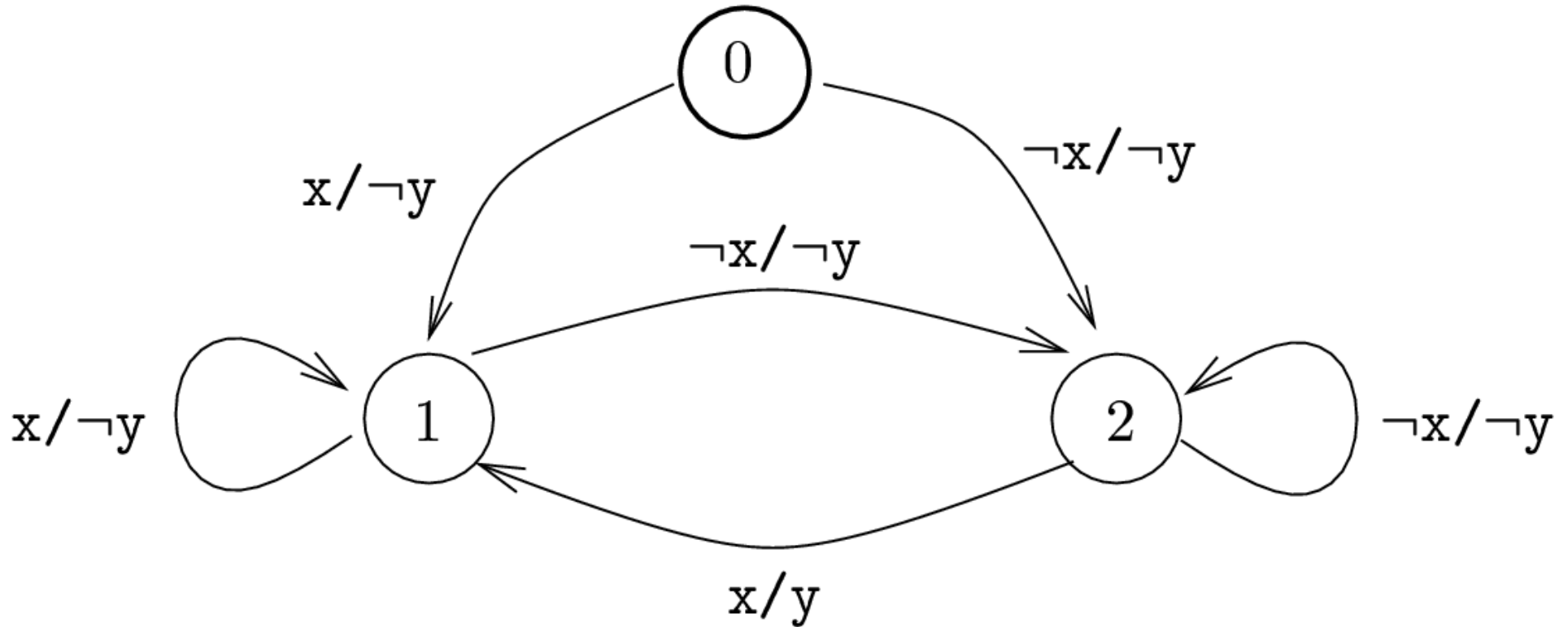
C source code: .c

The FSN gets transformed into C source code.

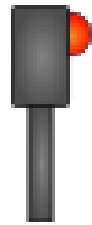


Finite State Automaton

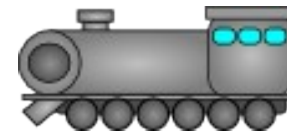
```
node EDGE(x: bool) returns (y: bool);  
  Y = false -> X and not pre(X)
```



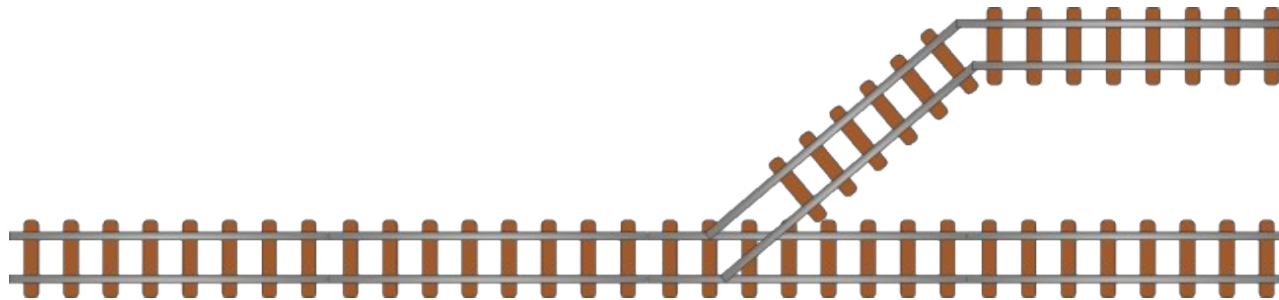
Simple Example



Signal Light

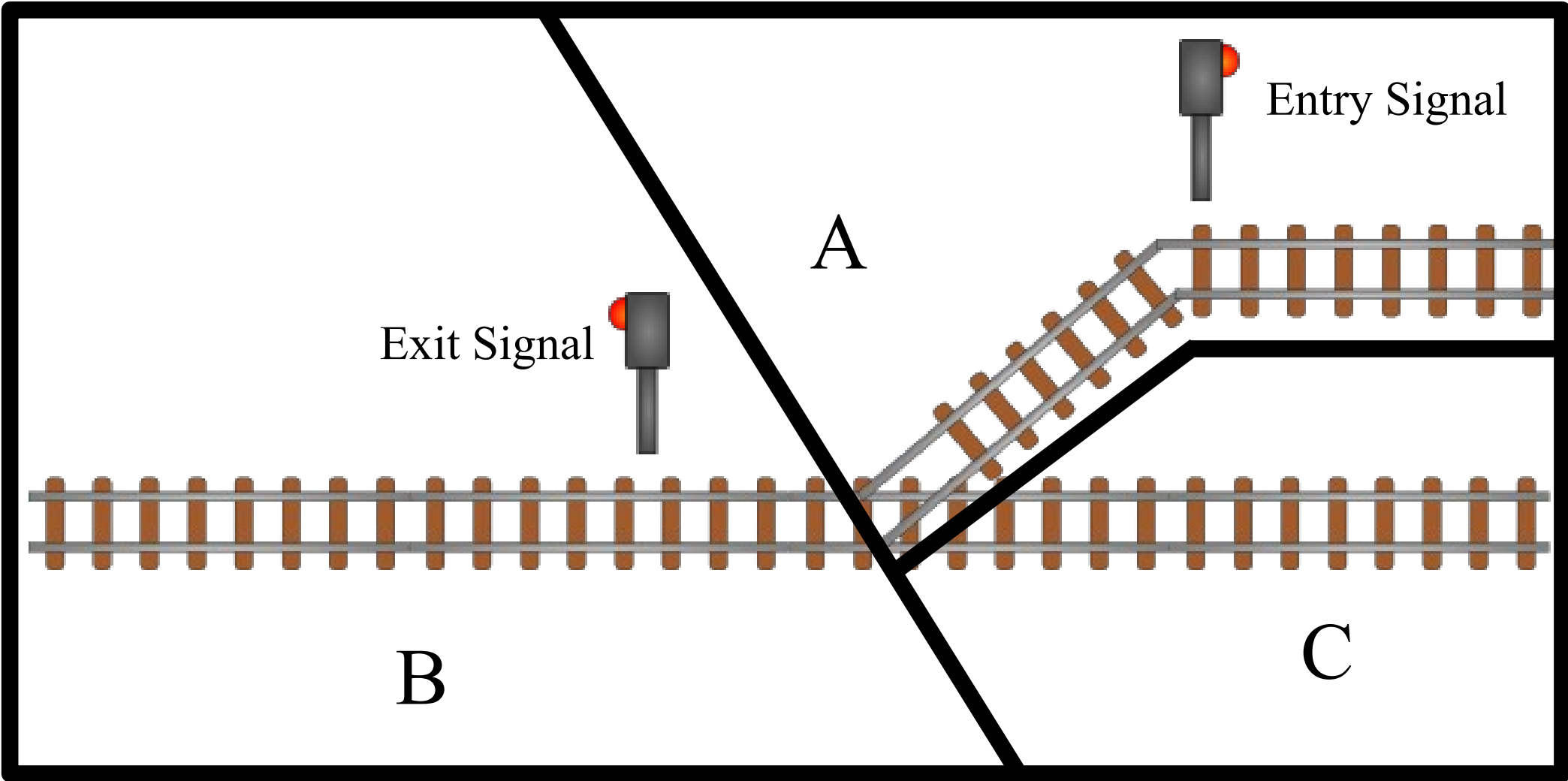


Train



Train Track

Train Track



■ Ins

- ♦ on_A : Is there a train on track segment A?
- ♦ on_B : Is there a train on track segment B?
- ♦ on_C : Is there a train on track segment C?
- ♦ ack_AB : Is track in the AB position?
- ♦ ack_BC : Is track in the BC position?

■ Outs

- ♦ grant_access : Should access light be green?
- ♦ grant_exit : Should exit light be green?
- ♦ do_AB : Should track switch in the AB position?
- ♦ do_BC : Should track switch in the BC position?

Lustre Model

```
node UMS (on_A, on_B, on_C, ack_AB, ack_BC: bool)
  returns (grant_access, grant_exit,
    do_AB, do_BC: bool);
var empty_section, only_on_B: bool;
let
  grant_access = empty_section and ack_AB;
  grant_exit = only_on_B and ack_BC;
  do_AB = not ack_AB and empty_section;
  do_BC = not ack_BC and only_on_B;
  empty_section = not (on_A or on_B or on_C);
  only_on_B = on_B and not (on_A or on_C);
tel
```

Verification Statements

```
node UMS_verif(on_A,on_B,on_C,
  ack_AB,ack_BC: bool)
  returns(property: bool);

var
  grant_access,grant_exit: bool;
  do_AB,do_BC: bool;
  no_collision,exclusive_req: bool;
  no_derail_AB,no_derail_BC: bool;
  empty_section, only_on_B: bool;

let
  empty_section = not(on_A or on_B or on_C);
  only_on_B = on_B and not(on_A or on_C);

  -- ASSERTIONS
  assert not(ack_AB and ack_BC);
  assert true ->
    always_from_to(ack_AB,ack_AB,do_BC);
  assert true ->
    always_from_to(ack_BC,ack_BC,do_AB);
  assert empty_section -> true;
```

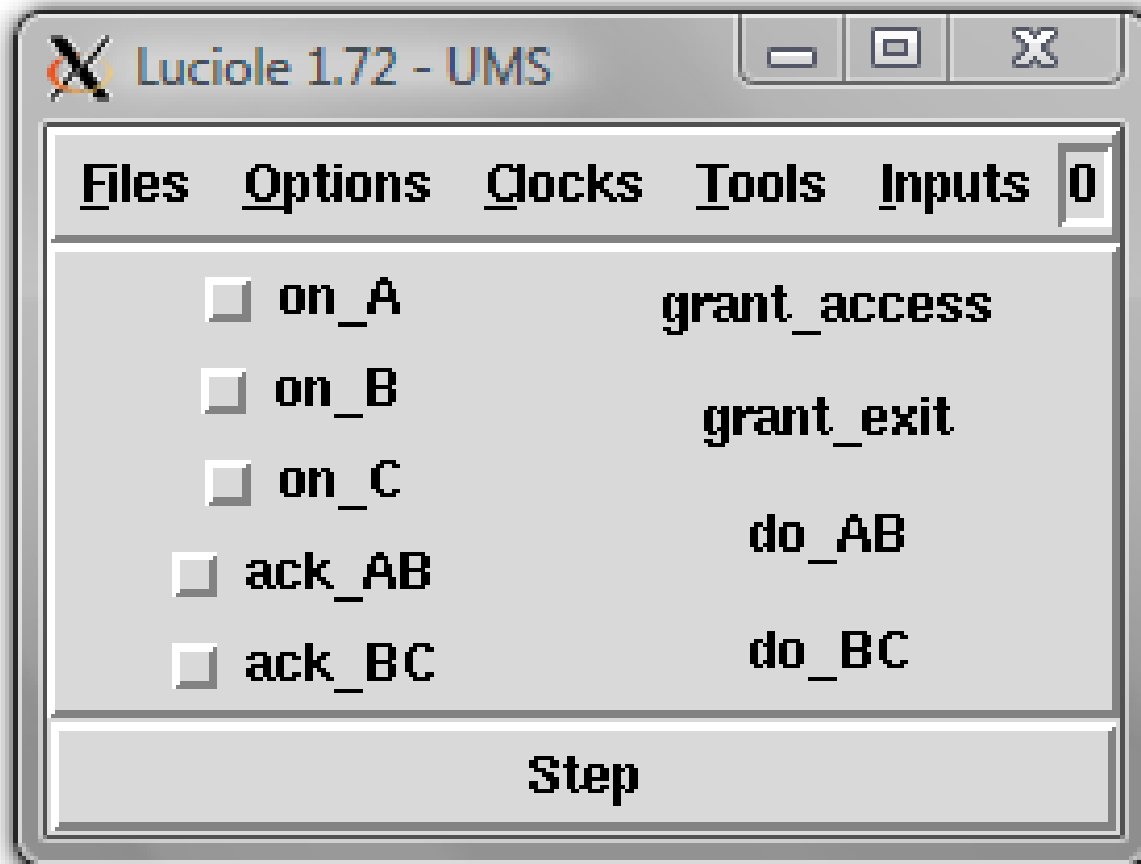
```
assert true -> implies(edge(not
  empty_section), pre grant_access);
assert true -> implies(edge(on_C), pre
  grant_exit);
assert true -> implies(edge(not on_A),on_B);
assert true -> implies(edge(not on_B), on_A
  or on_C);

-- UMS CALL
(grant_access,grant_exit,do_AB,do_BC) =
  UMS(on_A,on_B,on_C,ack_AB,ack_BC);

-- PROPERTIES
no_collision =
  implies(grant_access,empty_section);
exclusive_req = not(do_AB and do_BC);
no_derail_AB = always_from_to(ack_AB,
  grant_access, only_on_B);
no_derail_BC = always_from_to(ack_BC,
  grant_exit, empty_section);
property = no_collision and exclusive_req and
  no_derail_AB and no_derail_BC;

tel
```

Simulation



Implementation



- First created in 1982
- Commercially transformed in 1999
- Last open version of Esterel is 5.92, and was released in 2000
- A commercial version of Esterel is available from Esterel Technologies
- The Open Esterel tools were mostly developed by the Inria research center.

Lustre vs Esterel

Lustre

■ Declarative Language

- ◆ Describes **what** is to be computed.

```
Node ABRO(A,B,R: bool)
  returns (O: bool);
let
  O = R and (A or B);
tel
```

Esterel

■ Imperative Language

- ◆ Describes **how** this is to be computer.

```
module ABRO:
input A, B, R;
output O;

loop
  [ await A || await B ];
  emit O
each R

end module
```

Conclusion

- Lustre is a Synchronous Reactive Language
- It operates on streams (input and output)
- Models in Lustre can be Verified, Simulated and Execute
- I can draw cool trains
- Similarities between Lustre and Esterel