

Model Differences

How to specify and detect changes in graph-like models



Outline

Slide
2



Outline

- Challenges



Outline

- Challenges
- Plain Text Differences - GNU Diff



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- Plain Text Differences - GNU Diff
- XML-Differences Computation



- Challenges
- Plain Text Differences - GNU Diff
- XML-Differences Computation
- Project Idea



Challenges



Challenges



Challenges

- How to detect differences in models?



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 - ▶ Idea 1: Take a textual representation of the model and run *diff*



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 - ▶ Idea 2: Since models can be represented in XML use the X-Diff algorithm in order to detect changes



- How to detect differences in models?
 - ▶ Idea 1: Take a textual representation of the model and run *diff*
 - ▶ Idea 2: Since models can be represented in XML use the X-Diff algorithm in order to detect changes
 - ▶ Idea 3: MDE approach: Everything is a model! Use known difference algorithms and represent the difference as a model.



Where is the “real”/important for MDE differences?



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(10,10)



(15,12)



(12,20)



Model I

Challenges

Where is the “real”/important for MDE differences?

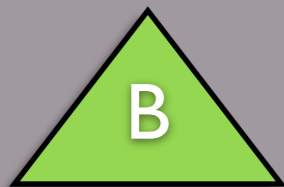
(10,10)



(15,12)



(12,20)

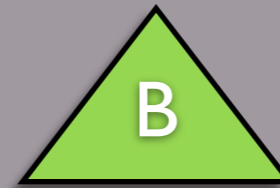


Model 1

(10,10)



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Model 2

Challenges

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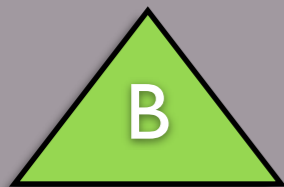
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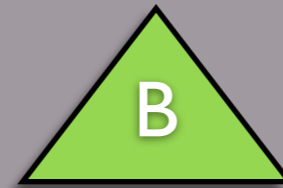
Model 1

=

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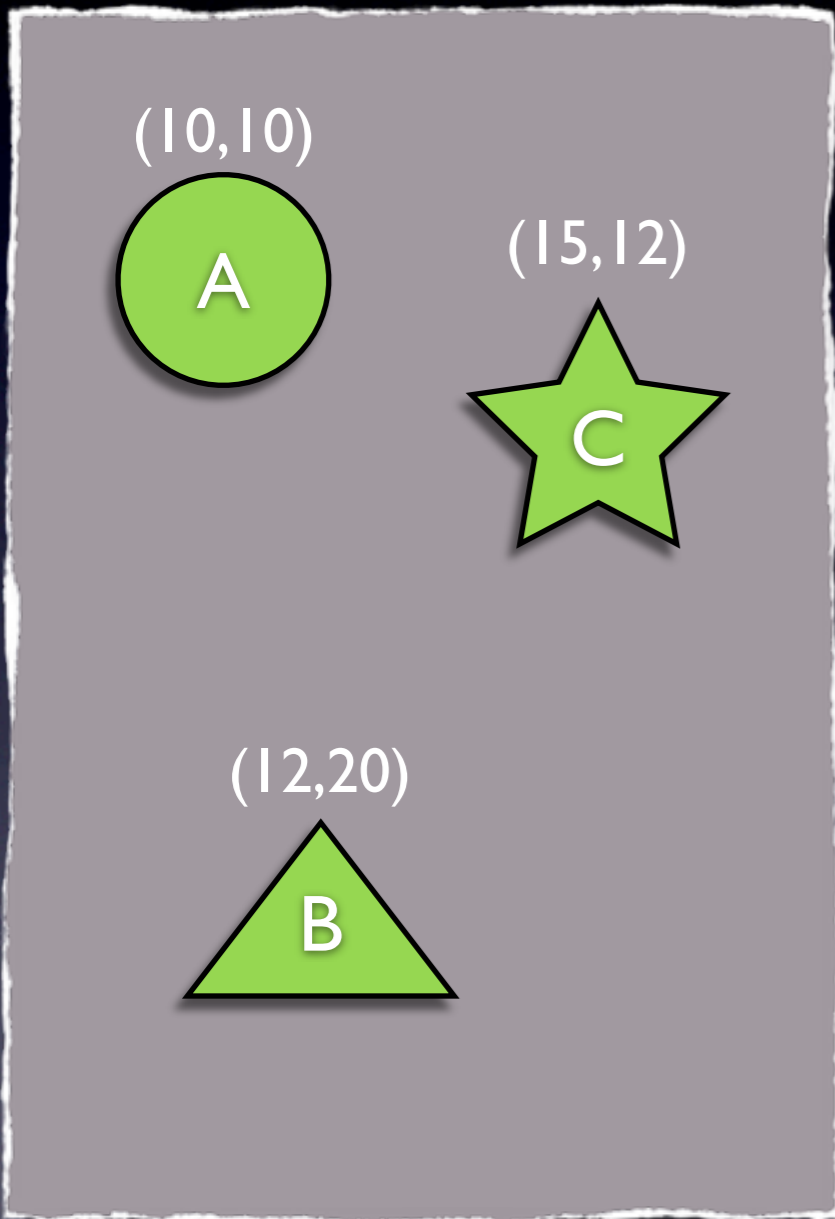
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Model 2

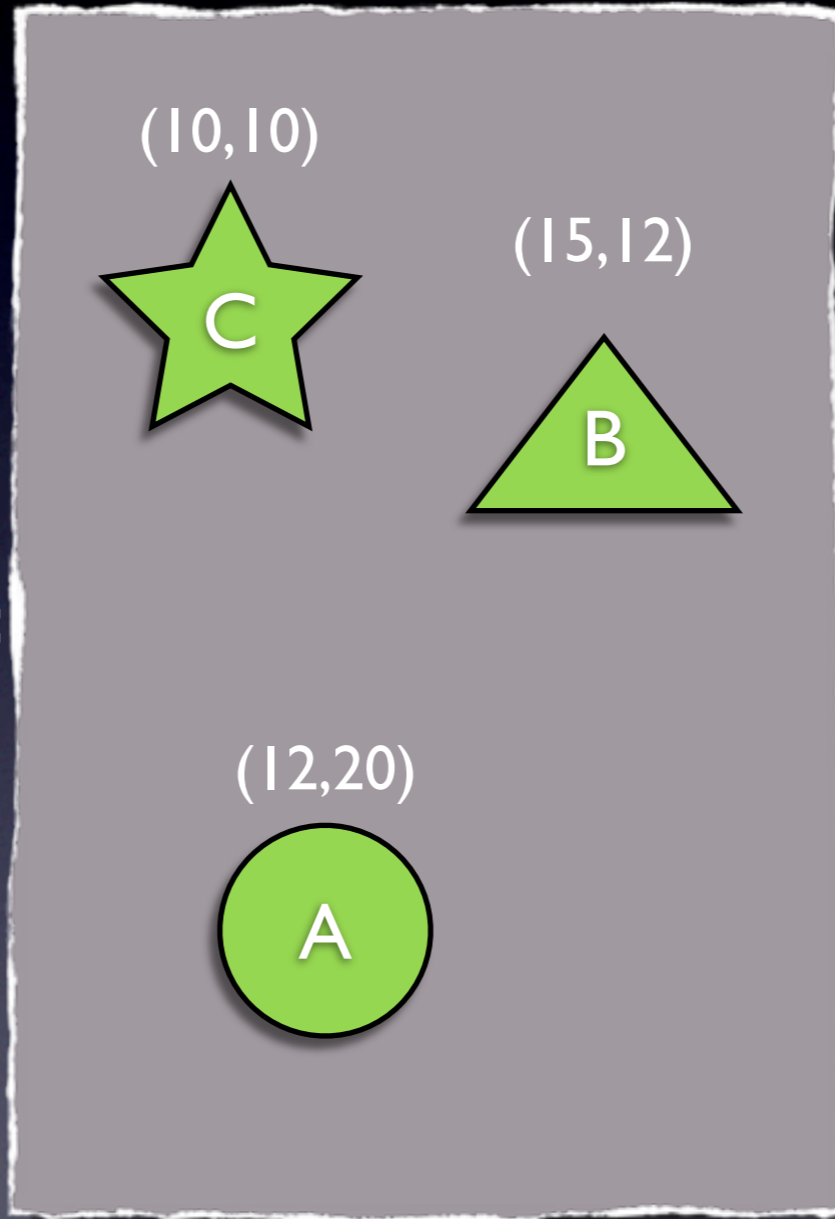
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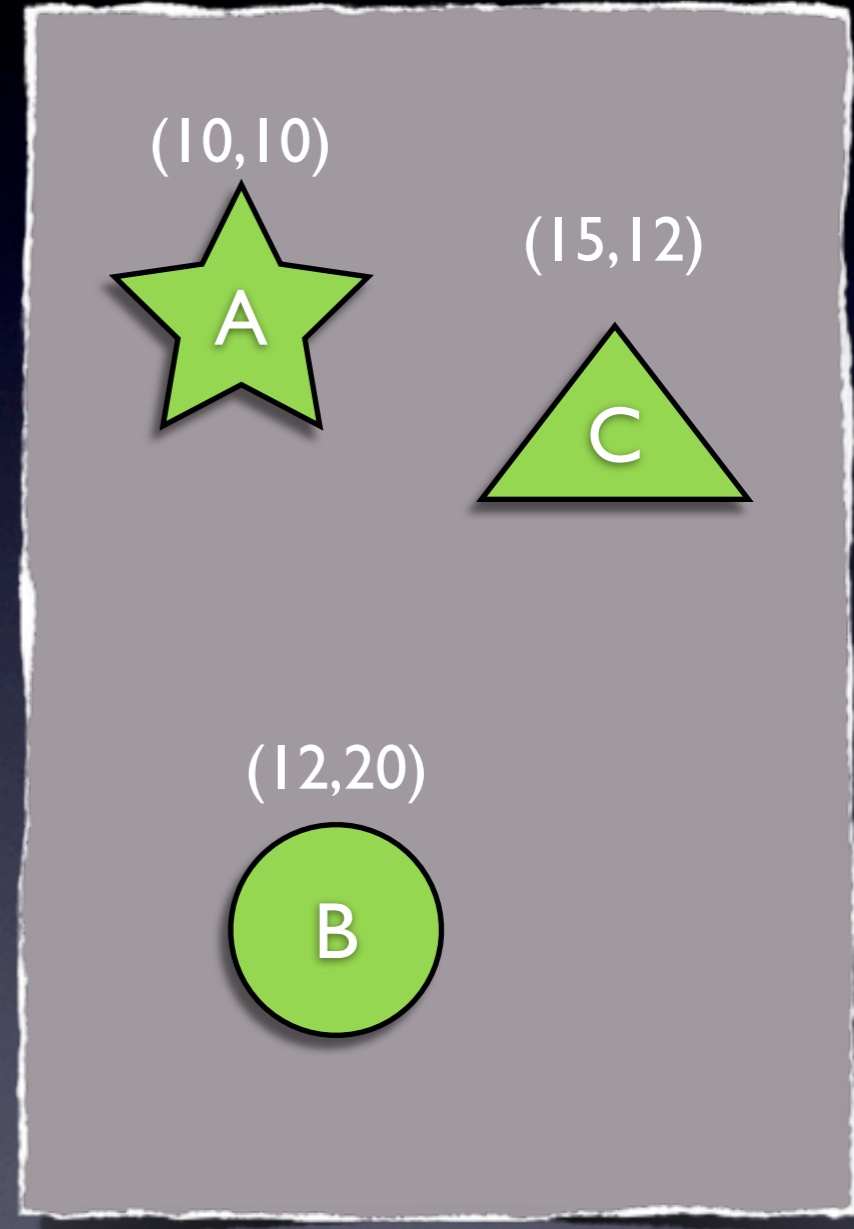


Model 1

=



Model 2

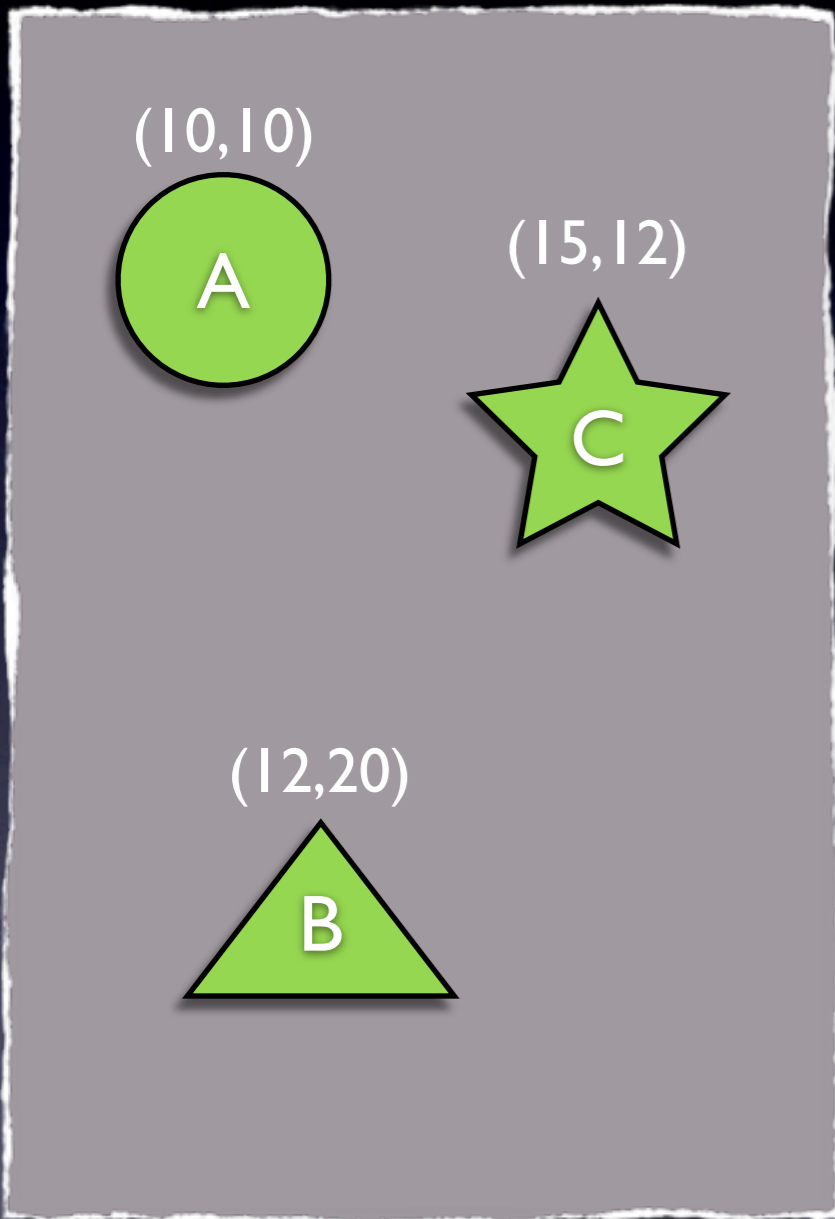


Model 3



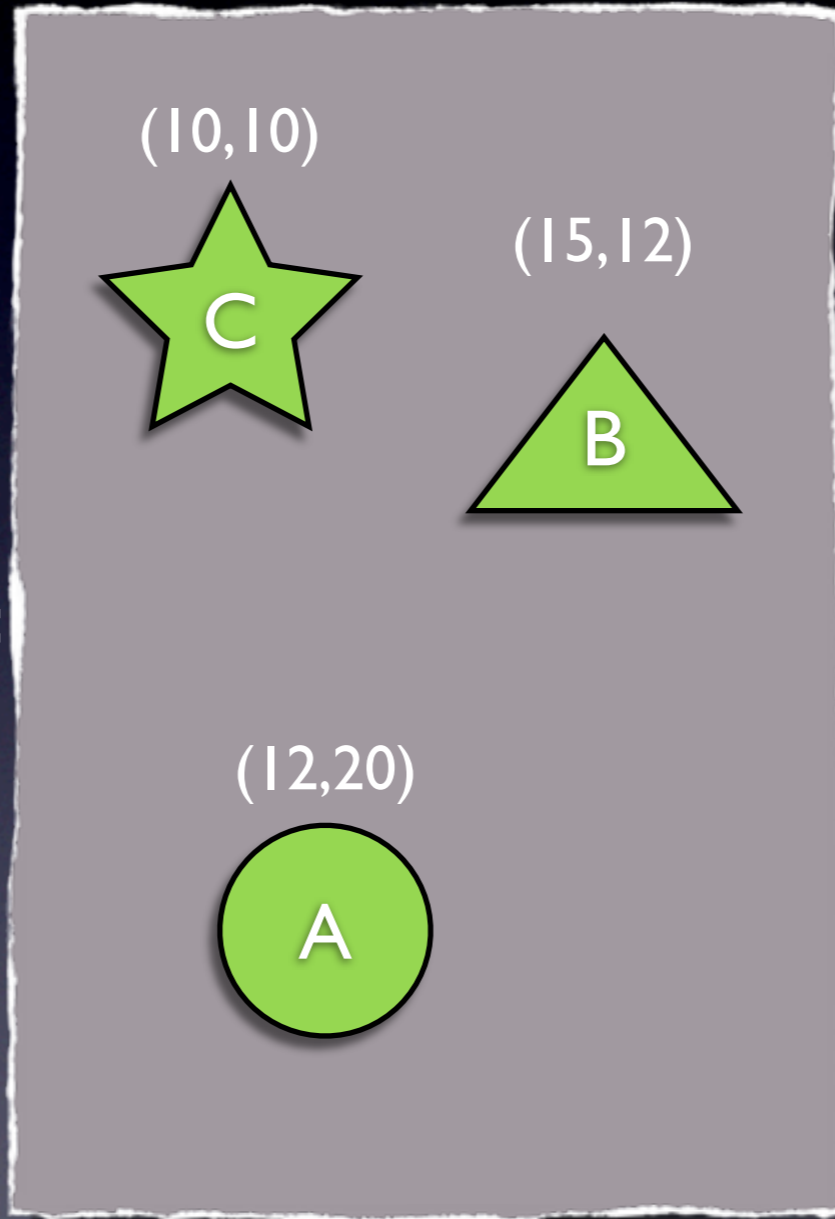
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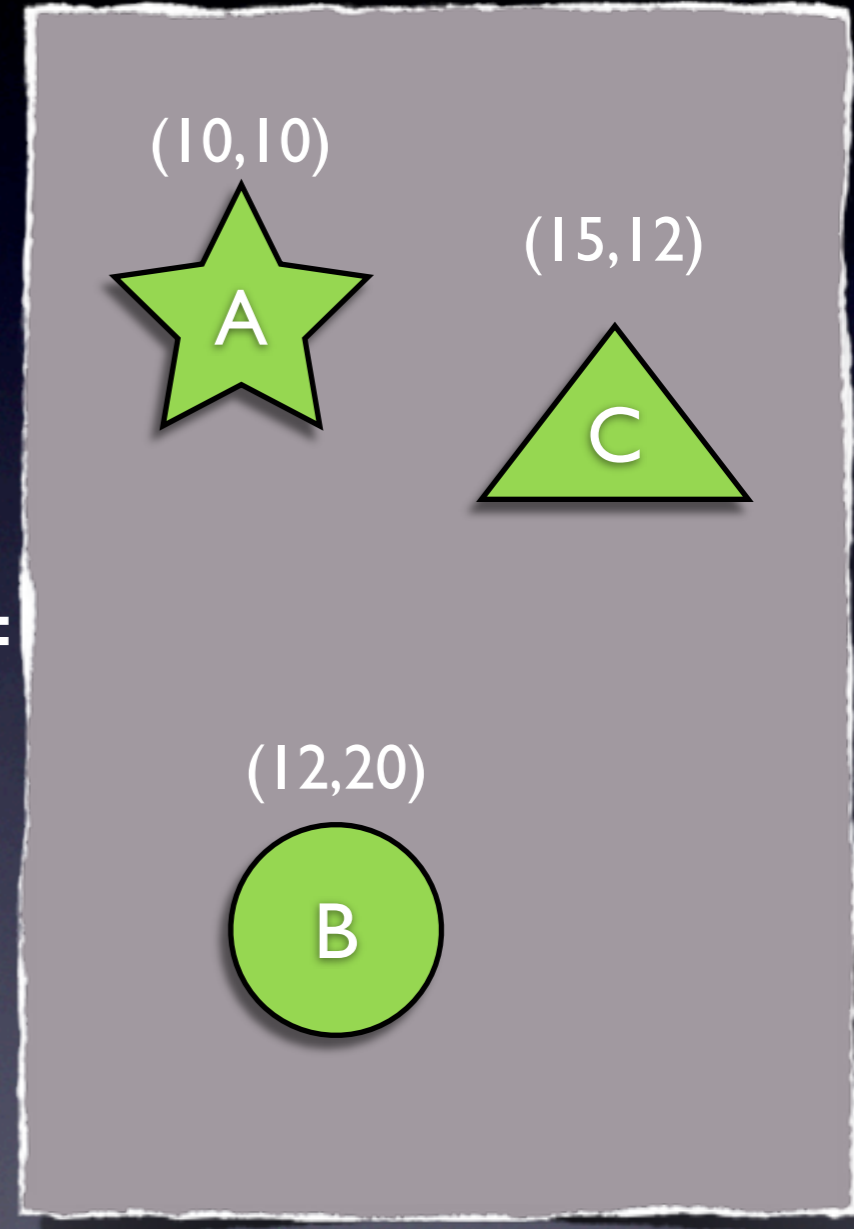
Model 1

=



Model 2

≠



Model 3



Plain Text Differences

GNU Diff



J. W. Hunt and M. D. McIlroy,

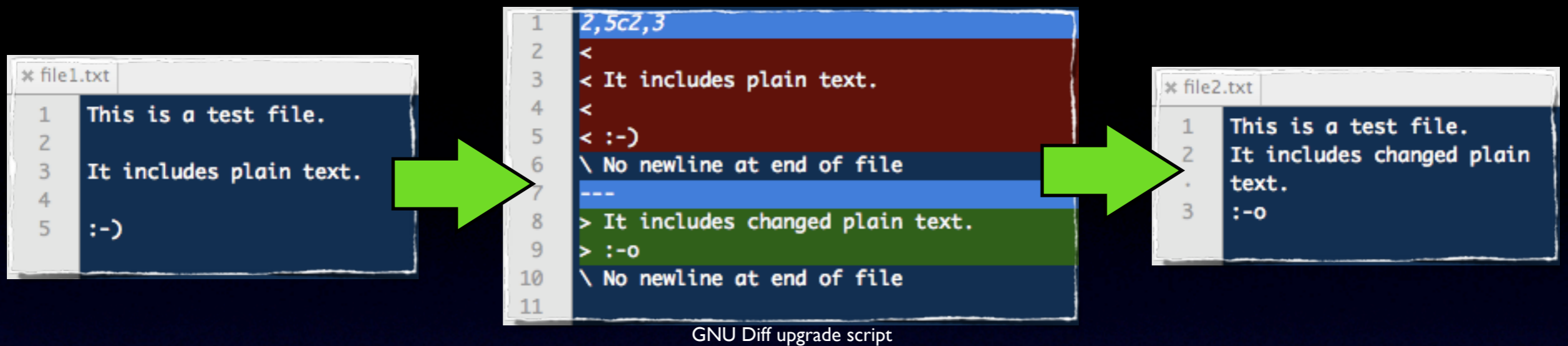
“An algorithm for differential file comparison”

Bell Telephone Laboratories CSTR #41 (1976)

- ▶ Detecting a difference in a plain text file is rather simple:
 - ▶ ***diff*** is used to compute the difference of two text strings (use of longest common subsequence algorithm) in $O(DN)$
 - ▶ Every single change in a text file will result a difference



What is a difference?

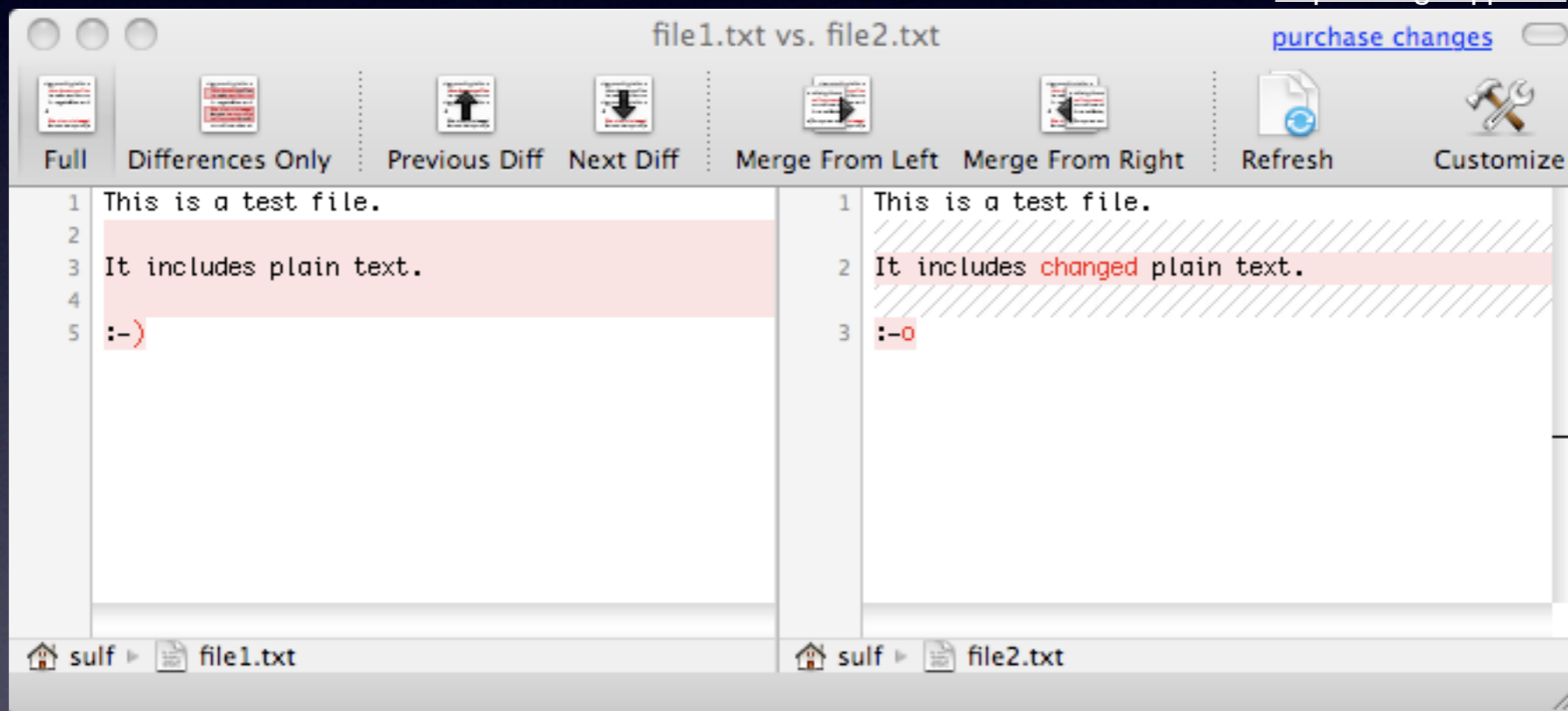


- We have two files/models/... and want to find the difference
- Difference is expressed as either
 - ▶ A script with add/delete/update directives describing the transformation from the source file/model/... to a target one
 - ▶ Graph coloring

Changes

- There are several tools that detect changes in a more graphical way:
- Example: Changes V.1.0

Source: <http://changesapp.com>



XML Differences

X-Diff



GNU diff on XML files

Slide
11

GNU Diff upgrade script



GNU diff on XML files

```
* book1.xml
1 <Books>
2   <Book>
3     <Title>Harry Potter and the Sorcerer's Stone</Title>
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```

vs.

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```
* book1-book2.diff
1 3,4c3,4
2 < <Title>Harry Potter and the Sorcerer's Stone</Title>
3 < <Price>$10.00</Price>
4 ---
5 > <Title>The adventures of Tom Sawyer</Title>
6 > <Price>$29.00</Price>
7 7,8c7,8
8 < <Title>The adventures of Tom Sawyer</Title>
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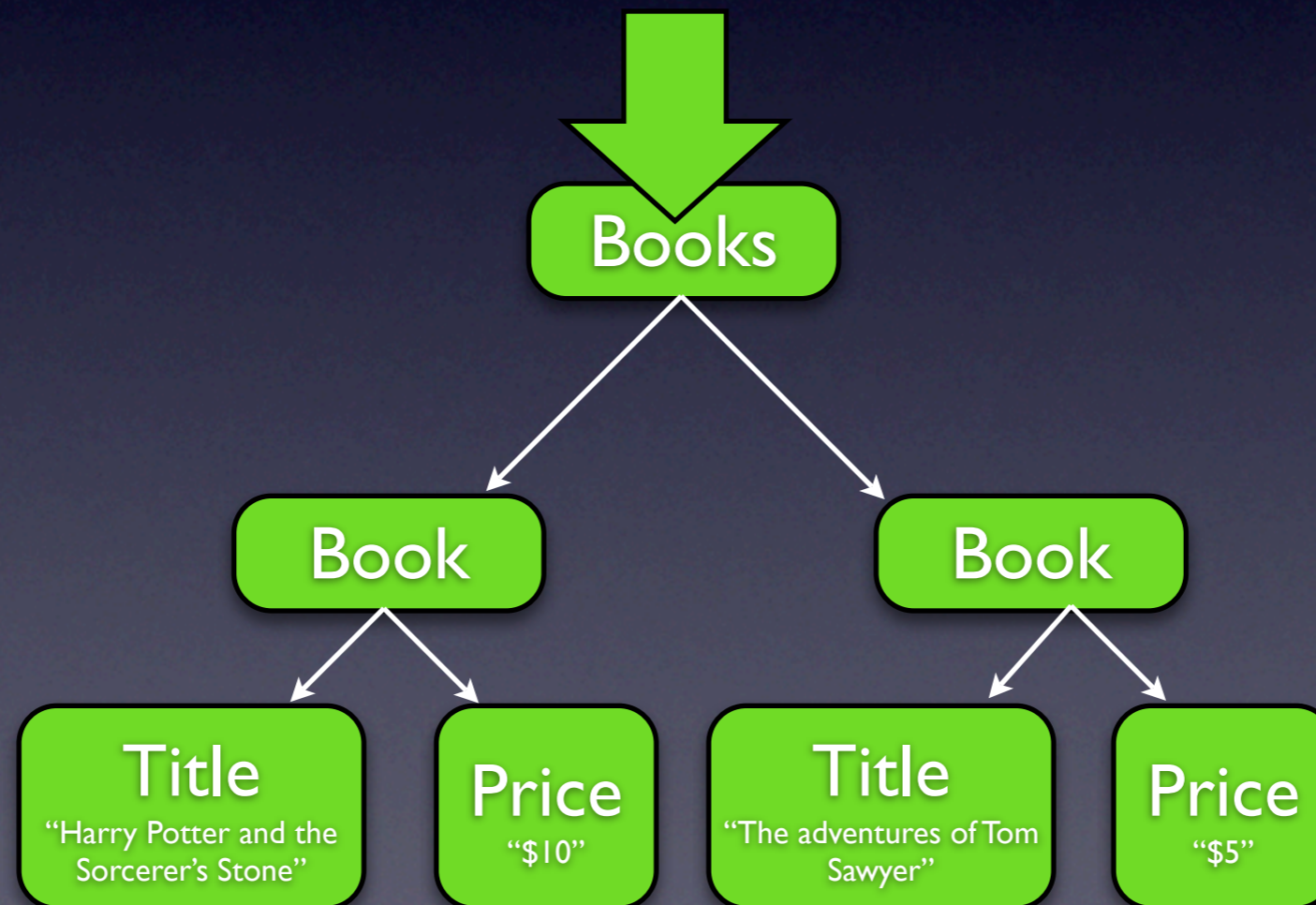


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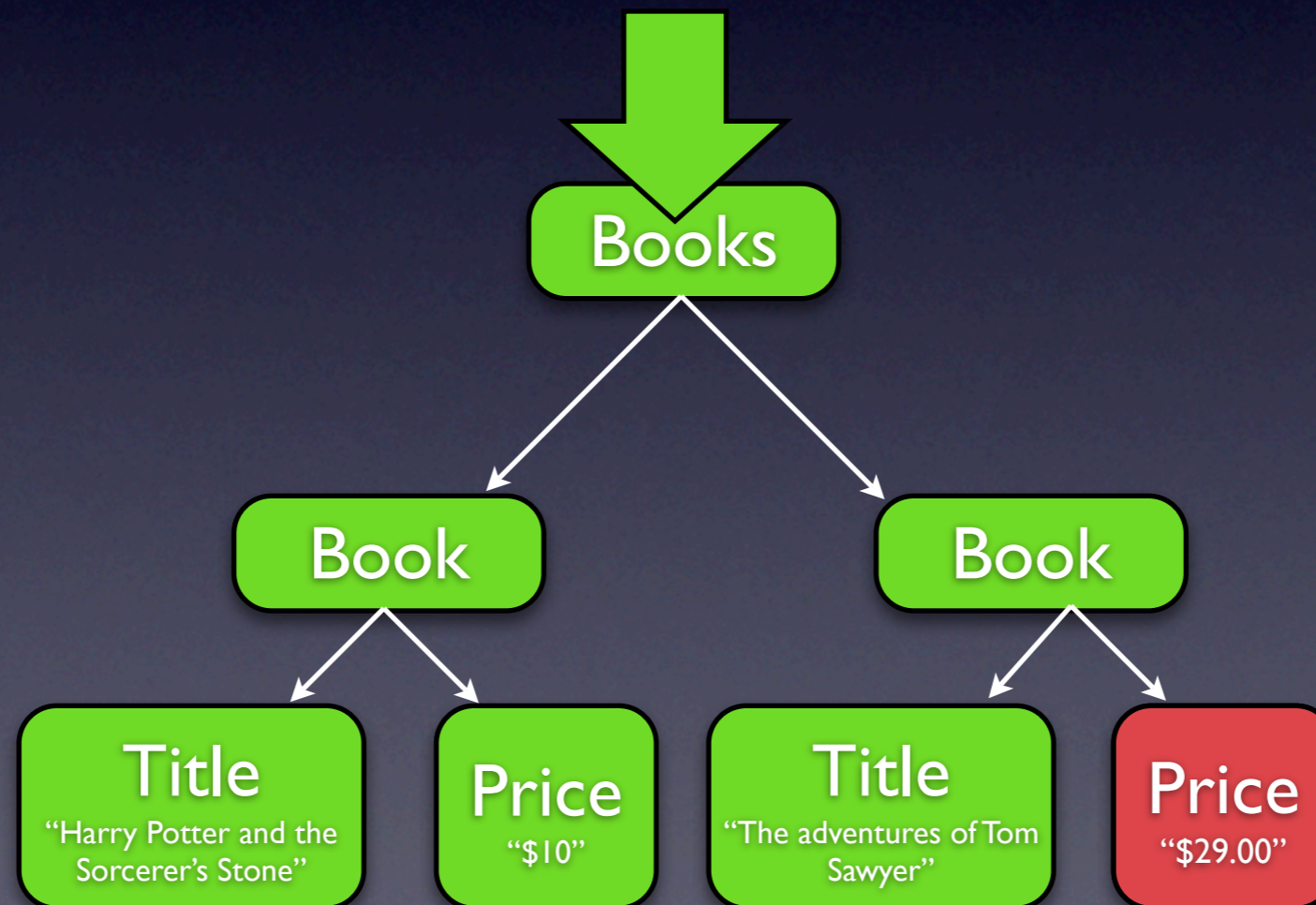


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Y. Wang, D.J. DeWitt and J. Cai

“An Effective Change Detection Algorithm for XML Documents”

University of Wisconsin (2003)

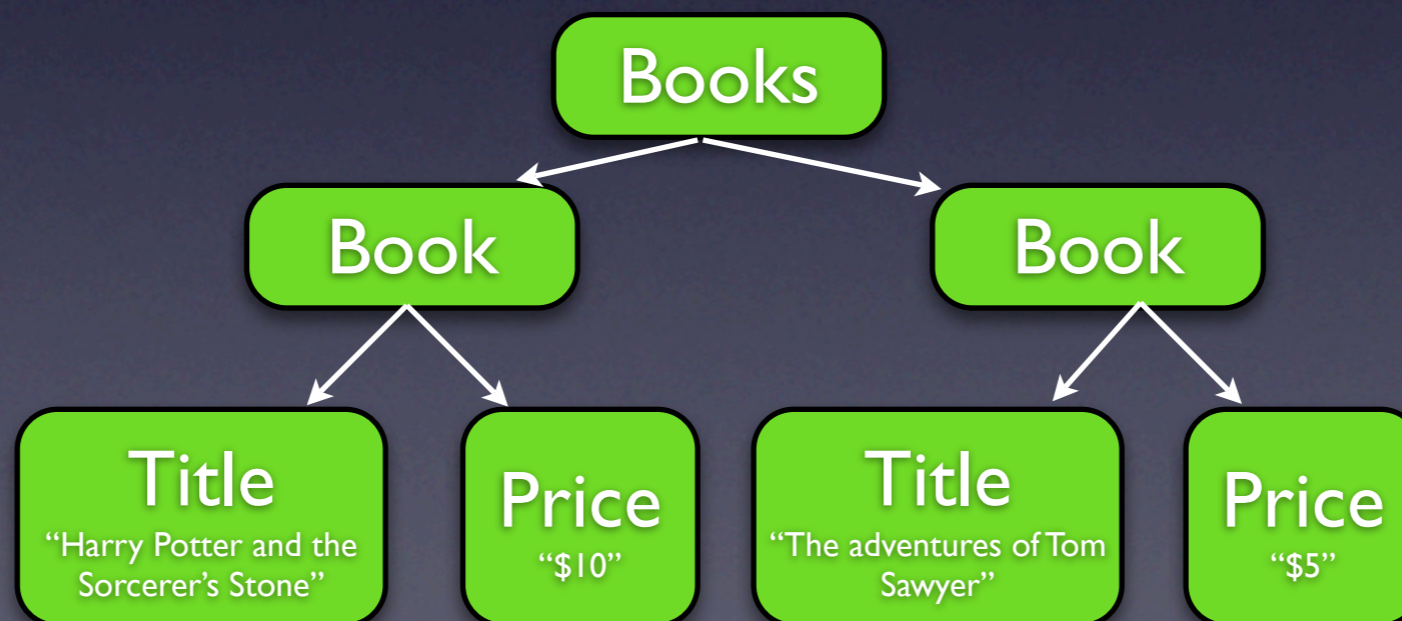
- XML structure is hierarchical and can be represented as a tree
- Unordered trees
 - ▶ only ancestor relationship is important
 - ▶ optimal change detection of unordered trees is NP complete^[1]
- Algorithm generates near optimal edit scripts
- Two trees are *isomorphic* if they are identical except for the ordering of siblings. X-Diff considers two trees as equivalent if they are *isomorphic*.

[1] K. Zhang, R. Statman, D. Shasha, “On the Editing Distance between Unordered Labeled Trees”, *Information Processing Letters*, 42: 133-139, 1992



Tree Definition

- A tree has three kinds of nodes:
 - ▶ **Element** nodes - non-leaf nodes with one label, *name*
 - ▶ **Text** nodes - leaf nodes with one label, *value*
 - ▶ **Attribute** nodes - leaf nodes with two labels, *name* and *value*



Algorithm

Slide
14



Algorithm

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- In order to compare edit scripts a cost model is introduced, which also affect the algorithm design.
 - ▶ X-Diff uses a simple cost model
- Unnecessary to compare each source node with any other target node
 - ▶ only nodes of the same type are matched



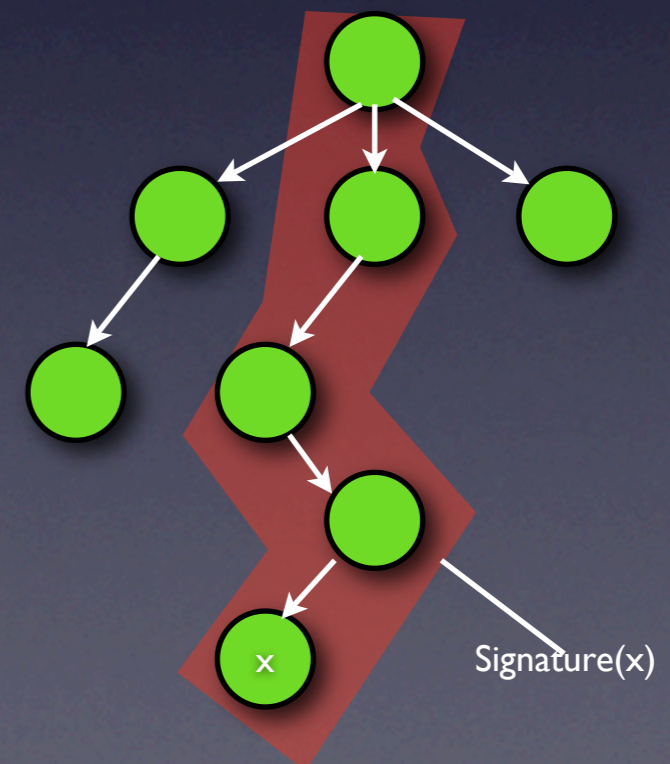
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 - ▶ text nodes should not be matched with element nodes or attribute nodes



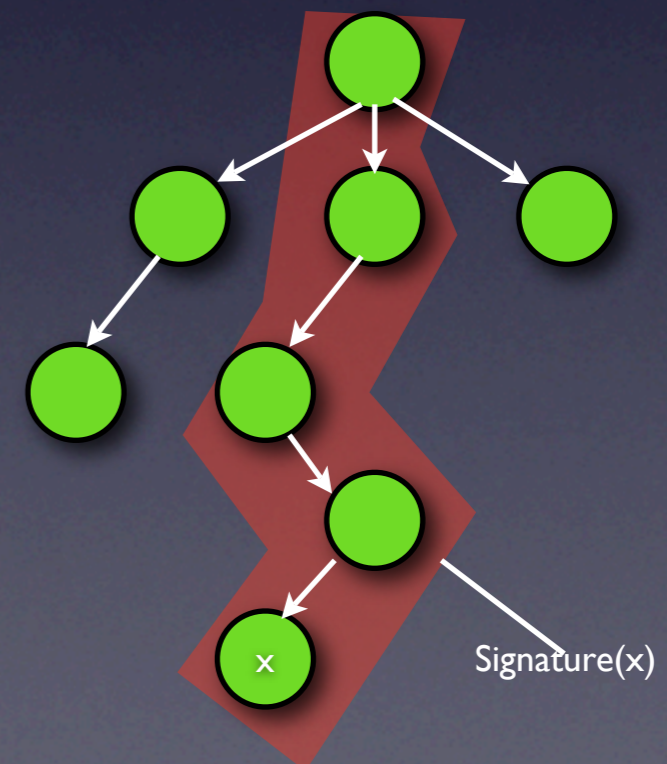
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 - ▶ Signature is introduced



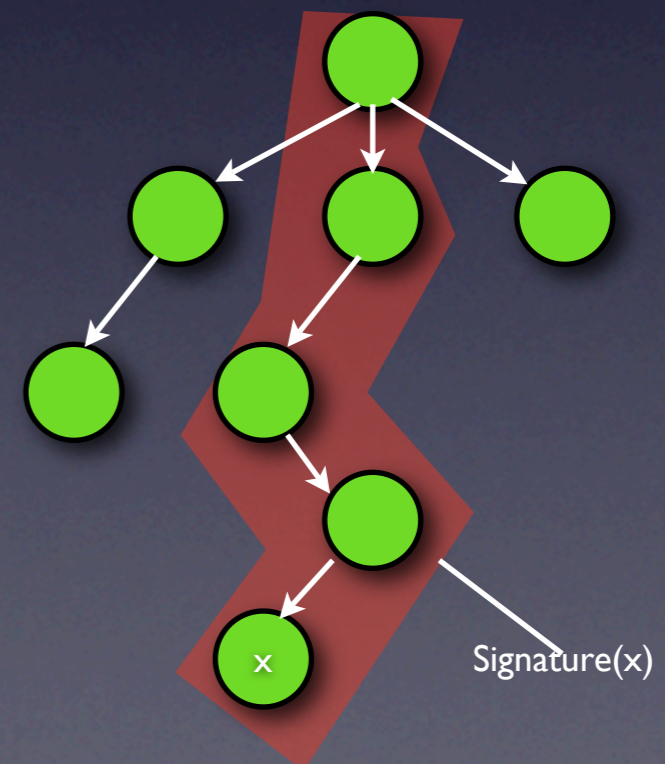
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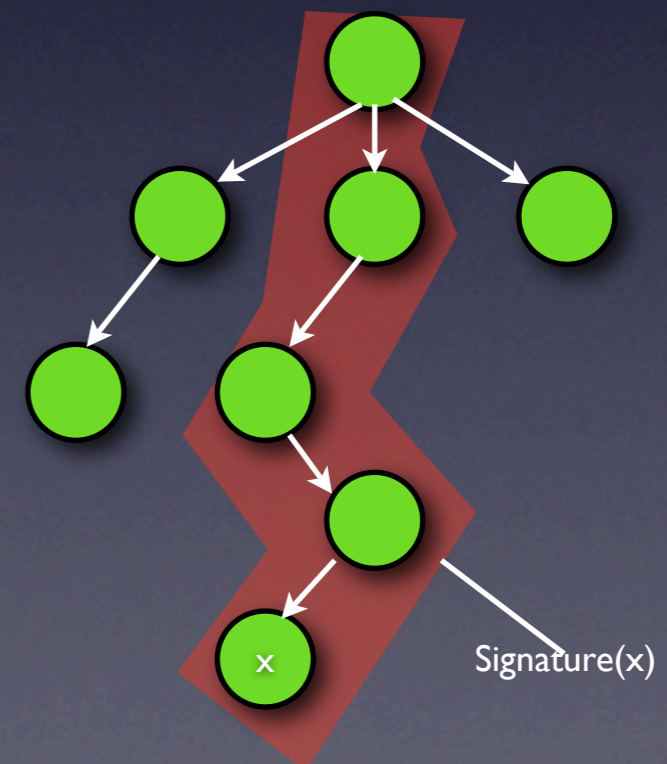
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- Based on minimum-Cost Matching an upgrade script is generated
- Algorithm only computes editing distances between nodes that have the same signature

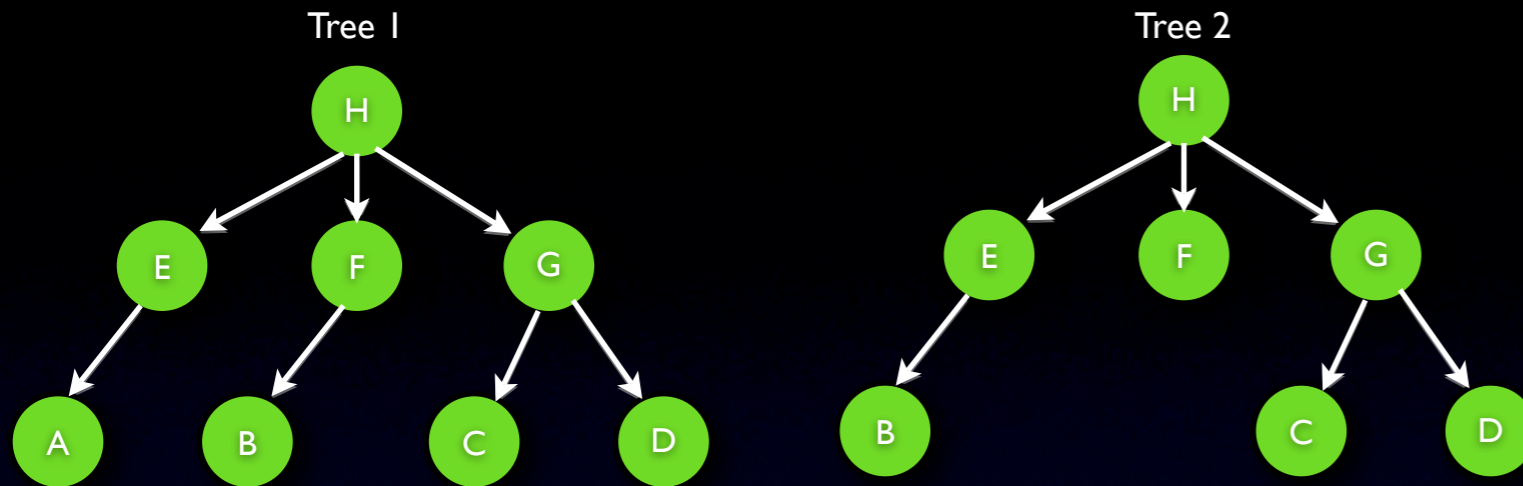


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 - ▶ Signature is introduced
- Based on minimum-Cost Matching an upgrade script is generated
- Algorithm only computes editing distances between nodes that have the same signature
 - ▶ Important to archive polynomial time complexity



Calculating minimum-Cost matching

Slide
15

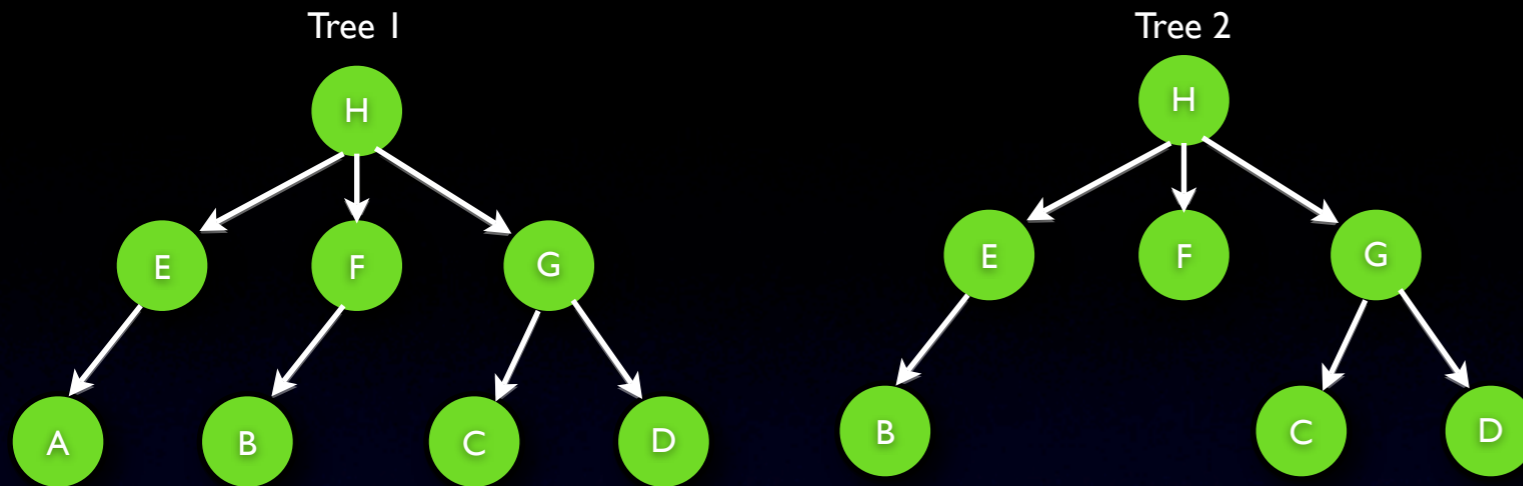


N1

N2

```
Input: Tree  $T_1$  and  $T_2$ .
Output: a minimum-cost matching  $M_{\min}(T_1, T_2)$ .
Initialize: set initial working sets
 $N_1 = \{\text{all leaf nodes in } T_1\}$ ,  $N_2 = \{\text{all leaf nodes in } T_2\}$ .
Set the Distance Table  $DT = \{\}$ .
/* Step 1: Reduce matching space */
Filter out next-level subtrees that have equal XHash values.
/* Step 2: compute editing distance for  $(T_1 \rightarrow T_2)$  */
DO {
  For every node  $x$  in  $N_1$ 
    For every node  $y$  in  $N_2$ 
      If  $\text{Signature}(x) = \text{Signature}(y)$ 
        Compute  $\text{Dist}(x, y)$ ;
        Save matching  $(x, y)$  with  $\text{Dist}(x, y)$  in  $DT$ .
      Set  $N_1 = \{\text{parent nodes of previous nodes in } N_1\}$ ;
       $N_2 = \{\text{parent nodes of previous nodes in } N_2\}$ .
  } While (both  $N_1$  and  $N_2$  are not empty).
/* Step 3: mark matchings on  $T_1$  and  $T_2$ . */
Set  $M_{\min}(T_1, T_2) = \{\}$ 
If  $\text{Signature}(\text{Root}(T_1)) \neq \text{Signature}(\text{Root}(T_2))$ 
  Return; /*  $M_{\min}(T_1, T_2) = \{\}$  */
Else
  Add  $(\text{Root}(T_1), \text{Root}(T_2))$  to  $M_{\min}(T_1, T_2)$ .
  For every non-leaf node mapping  $(x, y) \in M_{\min}(T_1, T_2)$ 
    Retrieve matchings between their child nodes that
    are stored in  $DT$ .
    Add child node matchings into  $M_{\min}(T_1, T_2)$ .
```

Calculating minimum-Cost matching



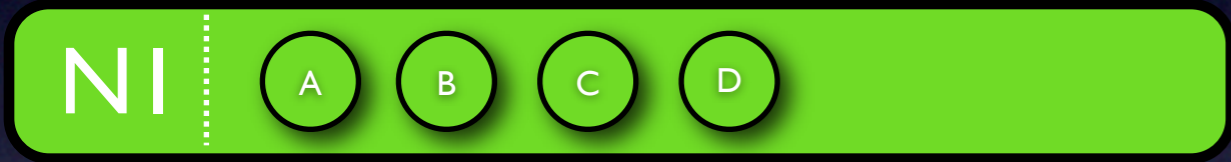
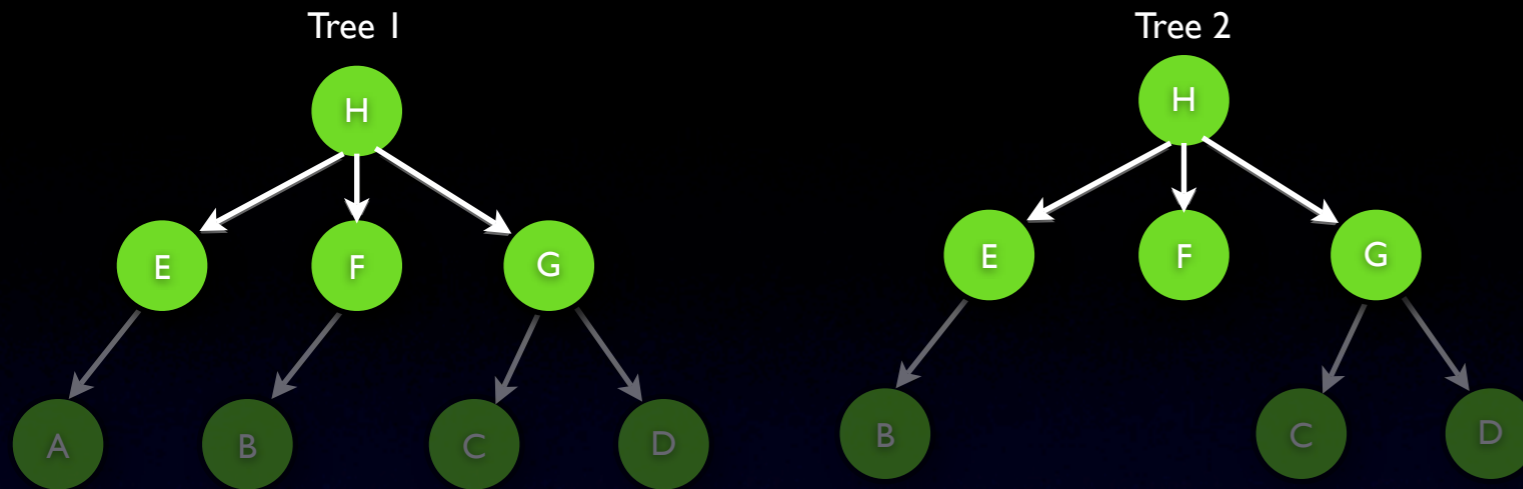
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N2

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Input: Tree T1 and T2.
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/* Step 2: compute editing distance for (T1 → T2) */
DO {
  For every node x in N1
    For every node y in N2
      If Signature(x) = Signature(y)
        Compute Dist(x, y);
        Save matching (x, y) with Dist(x, y) in DT.
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/* Step 3: mark matchings on T1 and T2. */
Set Mmin(T1, T2) = {}
If Signature(Root(T1)) ≠ Signature(Root(T2))
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  Add (Root(T1), Root(T2)) to Mmin(T1, T2).
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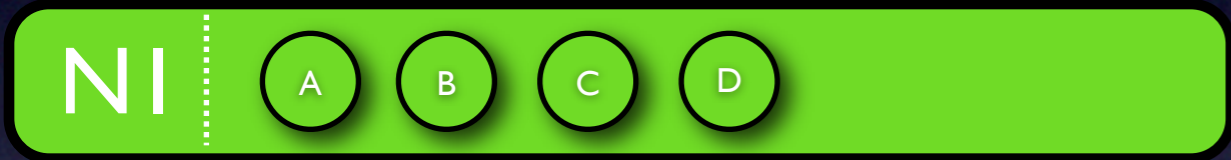
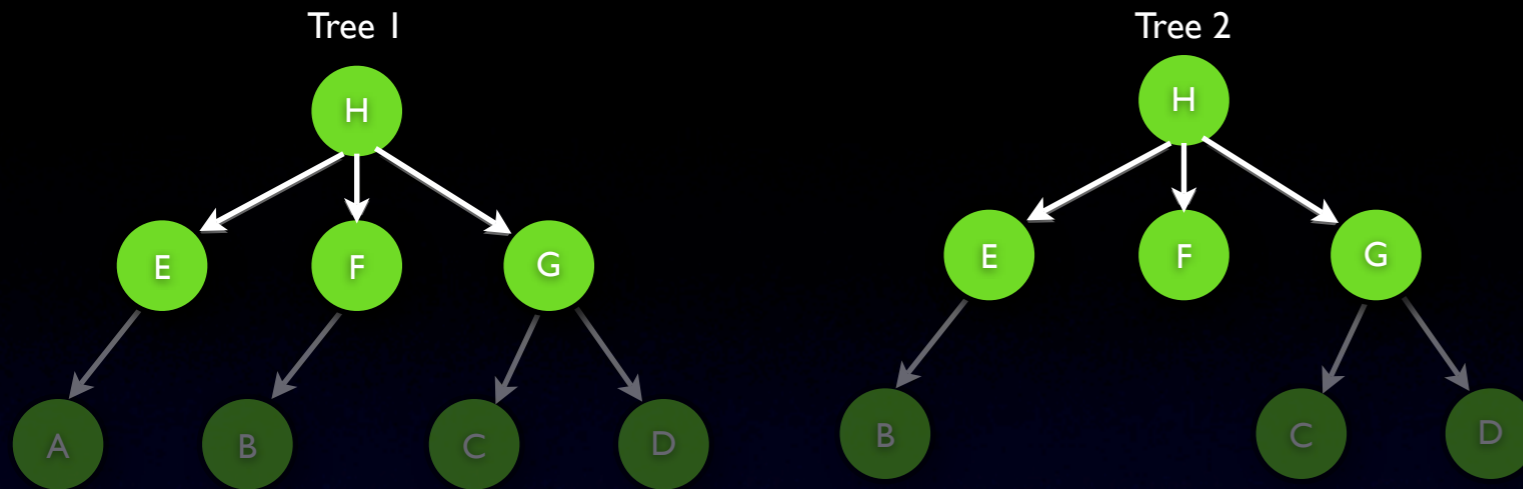
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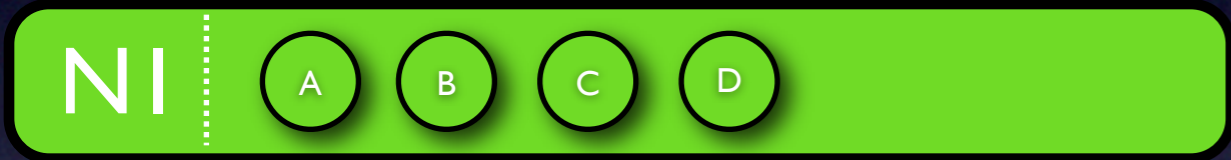
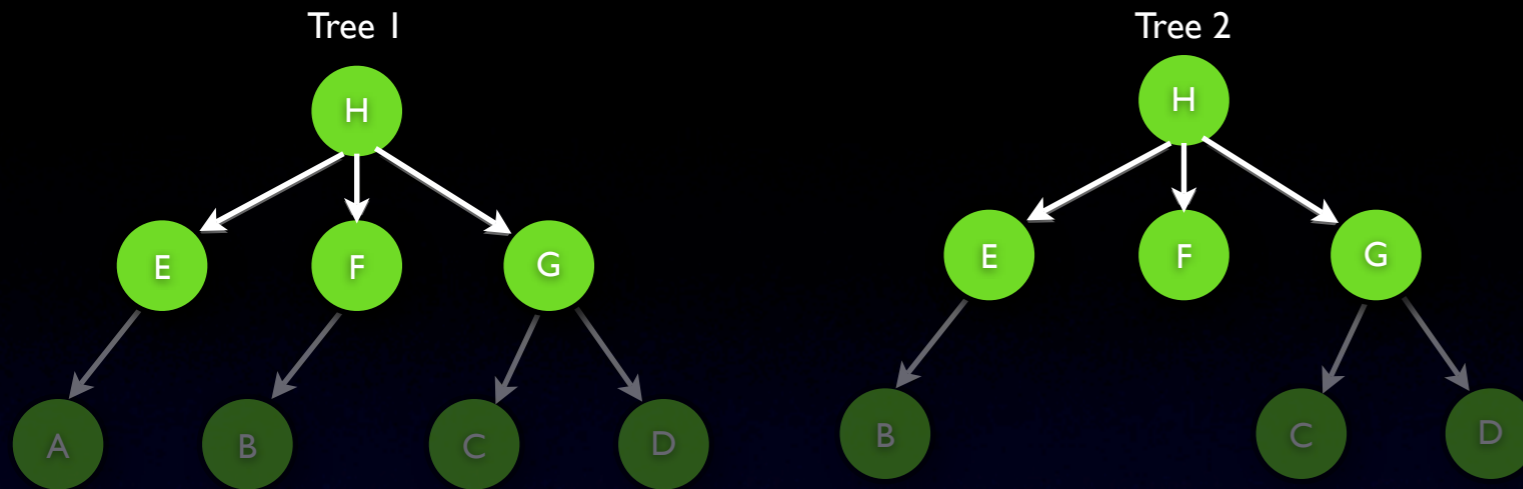


$\text{dist}(A,B) = 1$

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```



Calculating minimum-Cost matching

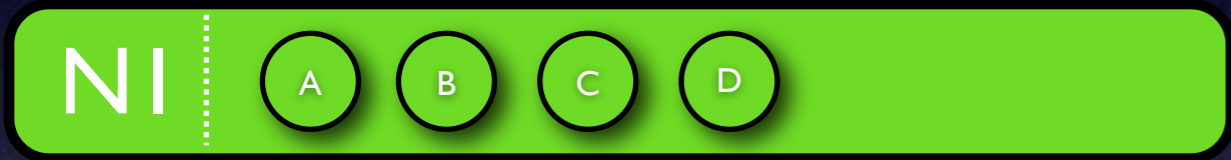
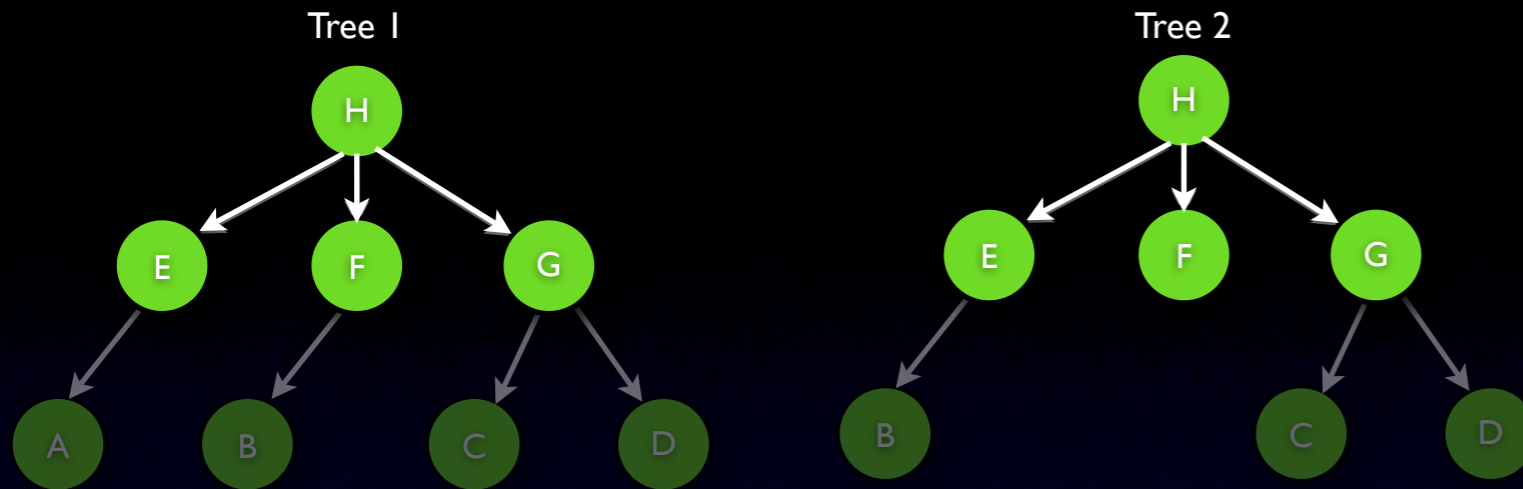


dist(A,B) = 1
dist(C,C) = 0

```
Input: Tree T1 and T2.
Output: a minimum-cost matching Mmin(T1, T2).
Initialize: set initial working sets
  N1 = {all leaf nodes in T1}, N2 = {all leaf nodes in T2}.
  Set the Distance Table DT = {}.
/* Step 1: Reduce matching space */
Filter out next-level subtrees that have equal XHash values.
/* Step 2: compute editing distance for (T1 → T2) */
DO {
  For every node x in N1
    For every node y in N2
      If Signature(x) = Signature(y)
        Compute Dist(x, y);
        Save matching (x, y) with Dist(x, y) in DT.
      Set N1 = {parent nodes of previous nodes in N1};
      N2 = {parent nodes of previous nodes in N2}.
} While (both N1 and N2 are not empty).
/* Step 3: mark matchings on T1 and T2. */
Set Mmin(T1, T2) = {}
If Signature(Root(T1)) ≠ Signature(Root(T2))
  Return; /* Mmin(T1, T2) = {} */
Else
  Add (Root(T1), Root(T2)) to Mmin(T1, T2).
  For every non-leaf node mapping (x, y) ∈ Mmin(T1, T2)
    Retrieve matchings between their child nodes that
    are stored in DT.
    Add child node matchings into Mmin(T1, T2).
```



Calculating minimum-Cost matching

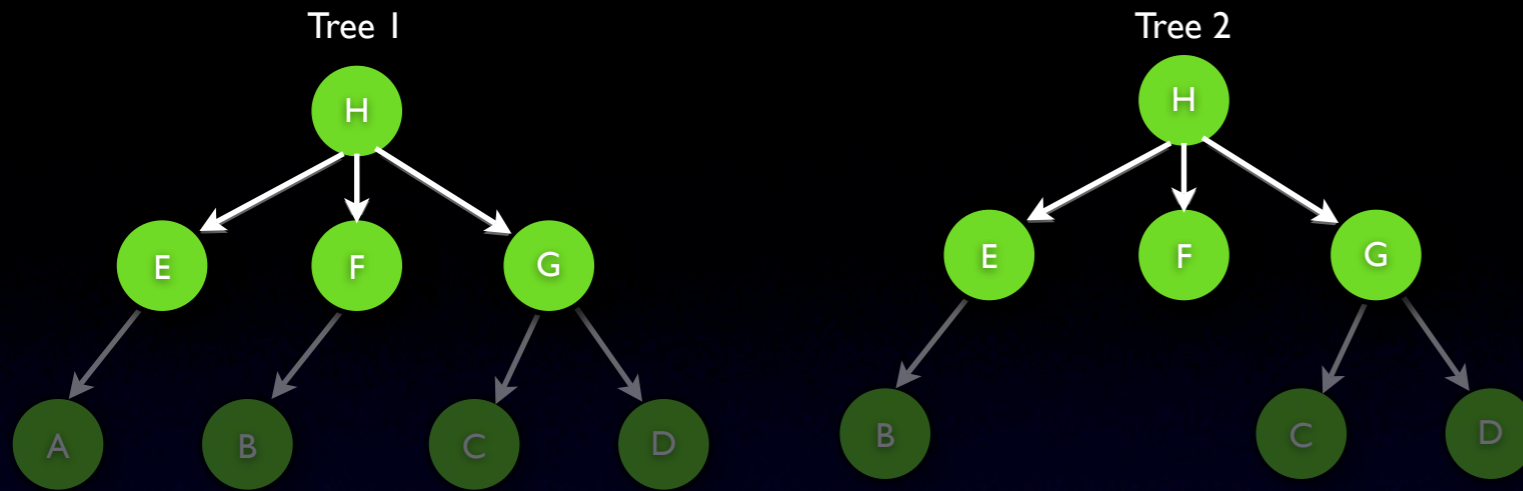


dist(A,B) = 1
dist(C,C) = 0
dist(D,D) = 0

```
Input: Tree T1 and T2.
Output: a minimum-cost matching Mmin(T1, T2).
Initialize: set initial working sets
  N1 = {all leaf nodes in T1}, N2 = {all leaf nodes in T2}.
  Set the Distance Table DT = {}.
/* Step 1: Reduce matching space */
Filter out next-level subtrees that have equal XHash values.
/* Step 2: compute editing distance for (T1 → T2) */
DO {
  For every node x in N1
    For every node y in N2
      If Signature(x) = Signature(y)
        Compute Dist(x, y);
        Save matching (x, y) with Dist(x, y) in DT.
      Set N1 = {parent nodes of previous nodes in N1};
      N2 = {parent nodes of previous nodes in N2}.
} While (both N1 and N2 are not empty).
/* Step 3: mark matchings on T1 and T2. */
Set Mmin(T1, T2) = {}
If Signature(Root(T1)) ≠ Signature(Root(T2))
  Return; /* Mmin(T1, T2) = {} */
Else
  Add (Root(T1), Root(T2)) to Mmin(T1, T2).
  For every non-leaf node mapping (x, y) ∈ Mmin(T1, T2)
    Retrieve matchings between their child nodes that
    are stored in DT.
    Add child node matchings into Mmin(T1, T2).
```



Calculating minimum-Cost matching



N1

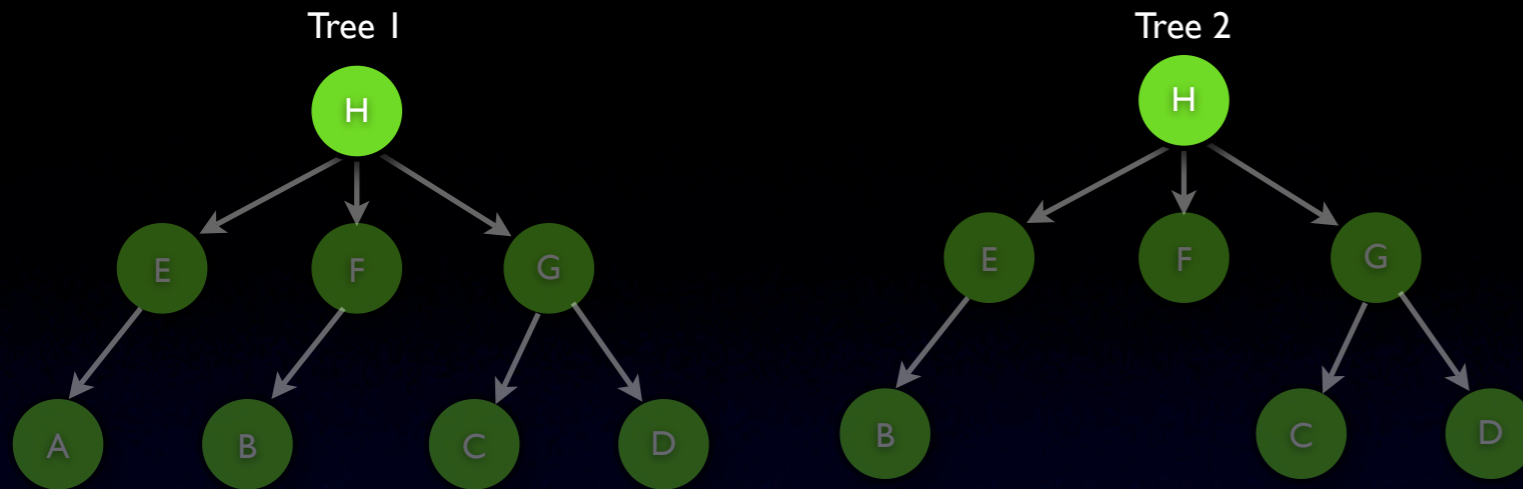
N2

dist(A,B) = 1
dist(C,C) = 0
dist(D,D) = 0

```
Input: Tree T1 and T2.
Output: a minimum-cost matching Mmin(T1, T2).
Initialize: set initial working sets
  N1 = {all leaf nodes in T1}, N2 = {all leaf nodes in T2}.
  Set the Distance Table DT = {}.
/* Step 1: Reduce matching space */
Filter out next-level subtrees that have equal XHash values.
/* Step 2: compute editing distance for (T1 → T2) */
DO {
  For every node x in N1
    For every node y in N2
      If Signature(x) = Signature(y)
        Compute Dist(x, y);
        Save matching (x, y) with Dist(x, y) in DT.
      Set N1 = {parent nodes of previous nodes in N1};
      Set N2 = {parent nodes of previous nodes in N2}.
  } While (both N1 and N2 are not empty).
/* Step 3: mark matchings on T1 and T2. */
Set Mmin(T1, T2) = {}
If Signature(Root(T1)) ≠ Signature(Root(T2))
  Return; /* Mmin(T1, T2) = {} */
Else
  Add (Root(T1), Root(T2)) to Mmin(T1, T2).
  For every non-leaf node mapping (x, y) ∈ Mmin(T1, T2)
    Retrieve matchings between their child nodes that
    are stored in DT.
    Add child node matchings into Mmin(T1, T2).
```



Calculating minimum-Cost matching

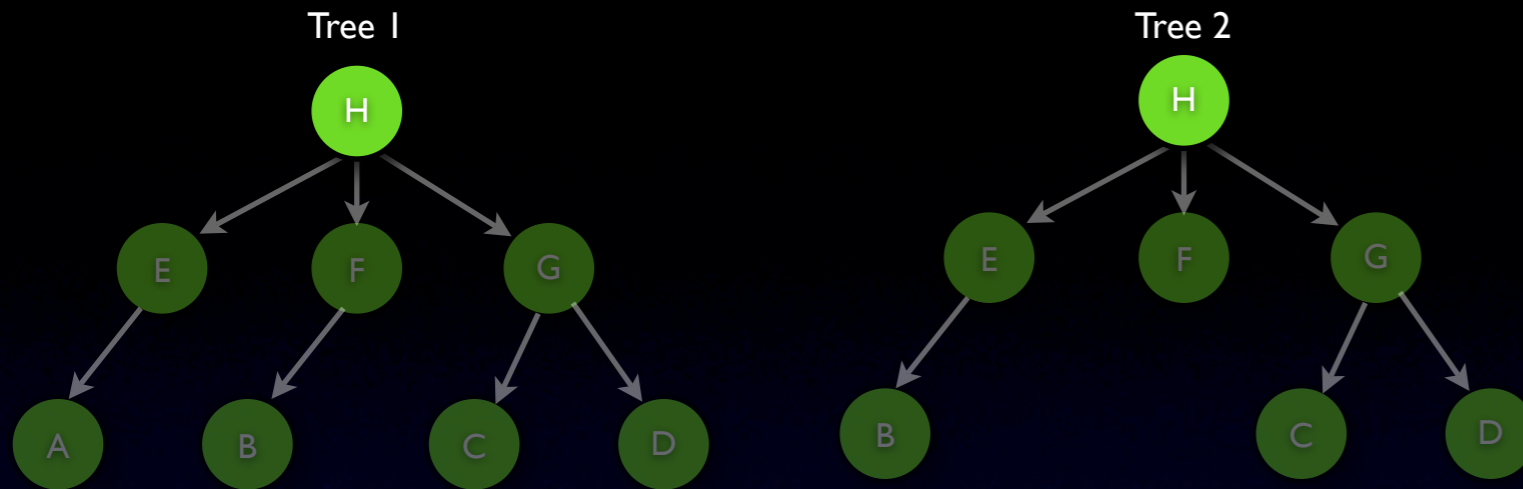


dist(A,B) = 1
dist(C,C) = 0
dist(D,D) = 0

```
Input: Tree T1 and T2.
Output: a minimum-cost matching Mmin(T1, T2).
Initialize: set initial working sets
  N1 = {all leaf nodes in T1}, N2 = {all leaf nodes in T2}.
  Set the Distance Table DT = {}.
/* Step 1: Reduce matching space */
Filter out next-level subtrees that have equal XHash values.
/* Step 2: compute editing distance for (T1 → T2) */
DO {
  For every node x in N1
    For every node y in N2
      If Signature(x) = Signature(y)
        Compute Dist(x, y);
        Save matching (x, y) with Dist(x, y) in DT.
      Set N1 = {parent nodes of previous nodes in N1};
      N2 = {parent nodes of previous nodes in N2}.
} While (both N1 and N2 are not empty).
/* Step 3: mark matchings on T1 and T2. */
Set Mmin(T1, T2) = {}
If Signature(Root(T1)) ≠ Signature(Root(T2))
  Return; /* Mmin(T1, T2) = {} */
Else
  Add (Root(T1), Root(T2)) to Mmin(T1, T2).
  For every non-leaf node mapping (x, y) ∈ Mmin(T1, T2)
    Retrieve matchings between their child nodes that
    are stored in DT.
    Add child node matchings into Mmin(T1, T2).
```



Calculating minimum-Cost matching

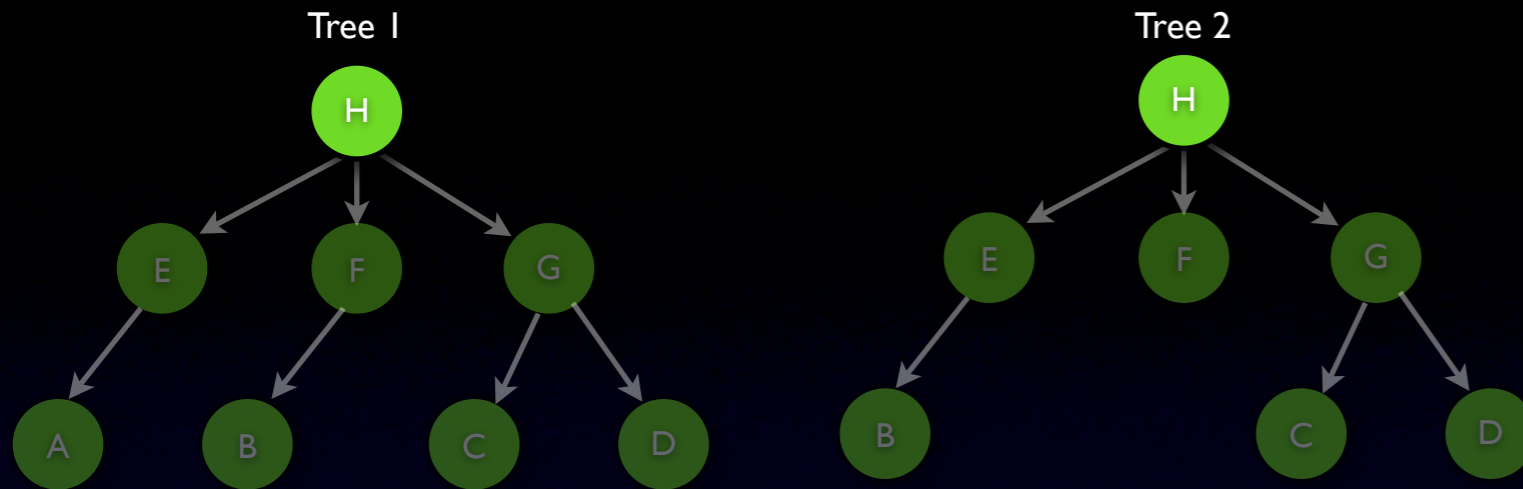


dist(A,B) = 1 dist(E,E) = 0
dist(C,C) = 0
dist(D,D) = 0

```
Input: Tree T1 and T2.
Output: a minimum-cost matching Mmin(T1, T2).
Initialize: set initial working sets
  N1 = {all leaf nodes in T1}, N2 = {all leaf nodes in T2}.
  Set the Distance Table DT = {}.
/* Step 1: Reduce matching space */
Filter out next-level subtrees that have equal XHash values.
/* Step 2: compute editing distance for (T1 → T2) */
DO {
  For every node x in N1
    For every node y in N2
      If Signature(x) = Signature(y)
        Compute Dist(x, y);
        Save matching (x, y) with Dist(x, y) in DT.
      Set N1 = {parent nodes of previous nodes in N1};
      N2 = {parent nodes of previous nodes in N2}.
  } While (both N1 and N2 are not empty).
/* Step 3: mark matchings on T1 and T2. */
Set Mmin(T1, T2) = {}
If Signature(Root(T1)) ≠ Signature(Root(T2))
  Return; /* Mmin(T1, T2) = {} */
Else
  Add (Root(T1), Root(T2)) to Mmin(T1, T2).
  For every non-leaf node mapping (x, y) ∈ Mmin(T1, T2)
    Retrieve matchings between their child nodes that
    are stored in DT.
    Add child node matchings into Mmin(T1, T2).
```



Calculating minimum-Cost matching

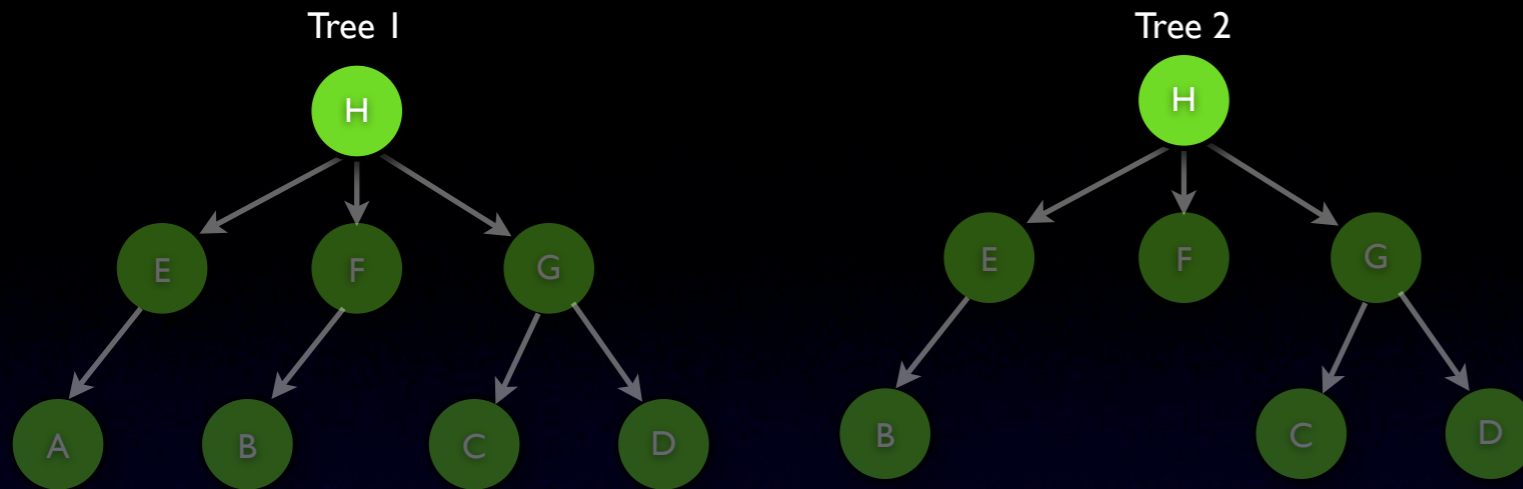


dist(A,B) = 1 dist(E,E) = 0
dist(C,C) = 0 dist(F,F) = 0
dist(D,D) = 0

```
Input: Tree T1 and T2.
Output: a minimum-cost matching Mmin(T1, T2).
Initialize: set initial working sets
  N1 = {all leaf nodes in T1}, N2 = {all leaf nodes in T2}.
  Set the Distance Table DT = {}.
/* Step 1: Reduce matching space */
Filter out next-level subtrees that have equal XHash values.
/* Step 2: compute editing distance for (T1 → T2) */
DO {
  For every node x in N1
    For every node y in N2
      If Signature(x) = Signature(y)
        Compute Dist(x, y);
        Save matching (x, y) with Dist(x, y) in DT.
      Set N1 = {parent nodes of previous nodes in N1};
      N2 = {parent nodes of previous nodes in N2}.
} While (both N1 and N2 are not empty).
/* Step 3: mark matchings on T1 and T2. */
Set Mmin(T1, T2) = {}
If Signature(Root(T1)) ≠ Signature(Root(T2))
  Return; /* Mmin(T1, T2) = {} */
Else
  Add (Root(T1), Root(T2)) to Mmin(T1, T2).
  For every non-leaf node mapping (x, y) ∈ Mmin(T1, T2)
    Retrieve matchings between their child nodes that
    are stored in DT.
    Add child node matchings into Mmin(T1, T2).
```



Calculating minimum-Cost matching



N1

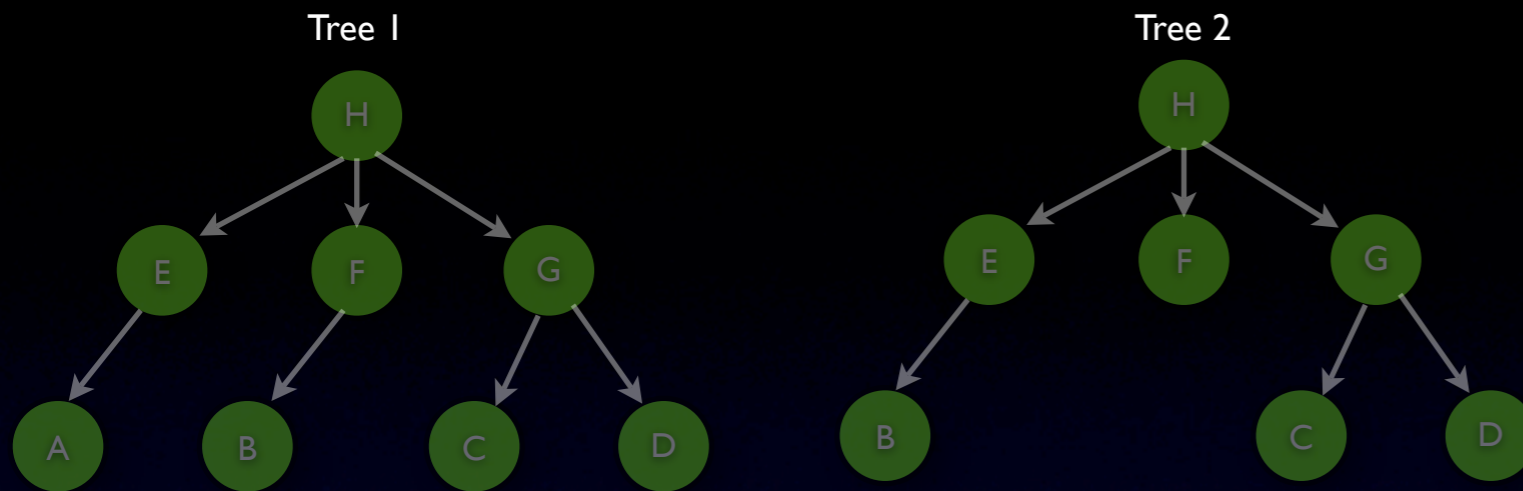
N2

dist(A,B) = 1 dist(E,E) = 0
dist(C,C) = 0 dist(F,F) = 0
dist(D,D) = 0 dist(G,G) = 0

```
Input: Tree T1 and T2.
Output: a minimum-cost matching Mmin(T1, T2).
Initialize: set initial working sets
  N1 = {all leaf nodes in T1}, N2 = {all leaf nodes in T2}.
  Set the Distance Table DT = {}.
/* Step 1: Reduce matching space */
Filter out next-level subtrees that have equal XHash values.
/* Step 2: compute editing distance for (T1 → T2) */
DO {
  For every node x in N1
    For every node y in N2
      If Signature(x) = Signature(y)
        Compute Dist(x, y);
        Save matching (x, y) with Dist(x, y) in DT.
  Set N1 = {parent nodes of previous nodes in N1};
  Set N2 = {parent nodes of previous nodes in N2}.
} While (both N1 and N2 are not empty).
/* Step 3: mark matchings on T1 and T2. */
Set Mmin(T1, T2) = {}
If Signature(Root(T1)) ≠ Signature(Root(T2))
  Return; /* Mmin(T1, T2) = {} */
Else
  Add (Root(T1), Root(T2)) to Mmin(T1, T2).
  For every non-leaf node mapping (x, y) ∈ Mmin(T1, T2)
    Retrieve matchings between their child nodes that
    are stored in DT.
    Add child node matchings into Mmin(T1, T2).
```



Calculating minimum-Cost matching



N1 | H

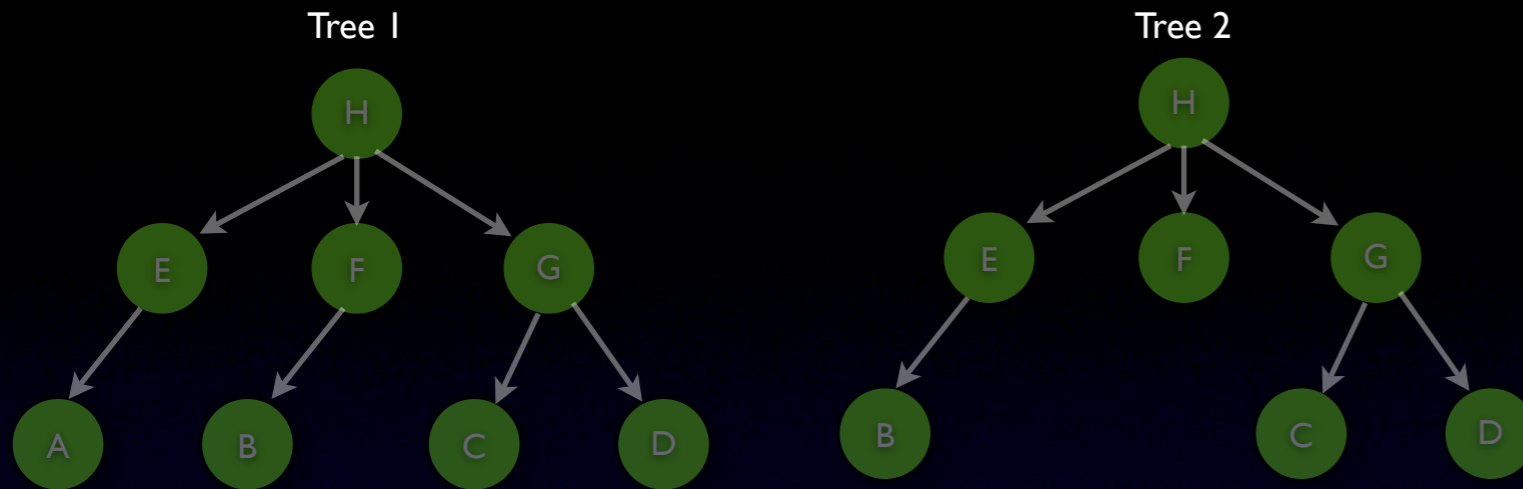
N2 | H

dist(A,B) = 1 dist(E,E) = 0
dist(C,C) = 0 dist(F,F) = 0
dist(D,D) = 0 dist(G,G) = 0

```
Input: Tree T1 and T2.
Output: a minimum-cost matching Mmin(T1, T2).
Initialize: set initial working sets
  N1 = {all leaf nodes in T1}, N2 = {all leaf nodes in T2}.
  Set the Distance Table DT = {}.
/* Step 1: Reduce matching space */
Filter out next-level subtrees that have equal XHash values.
/* Step 2: compute editing distance for (T1 → T2) */
DO {
  For every node x in N1
    For every node y in N2
      If Signature(x) = Signature(y)
        Compute Dist(x, y);
        Save matching (x, y) with Dist(x, y) in DT.
      Set N1 = {parent nodes of previous nodes in N1};
      Set N2 = {parent nodes of previous nodes in N2}.
} While (both N1 and N2 are not empty).
/* Step 3: mark matchings on T1 and T2. */
Set Mmin(T1, T2) = {}
If Signature(Root(T1)) ≠ Signature(Root(T2))
  Return; /* Mmin(T1, T2) = {} */
Else
  Add (Root(T1), Root(T2)) to Mmin(T1, T2).
  For every non-leaf node mapping (x, y) ∈ Mmin(T1, T2)
    Retrieve matchings between their child nodes that
    are stored in DT.
    Add child node matchings into Mmin(T1, T2).
```



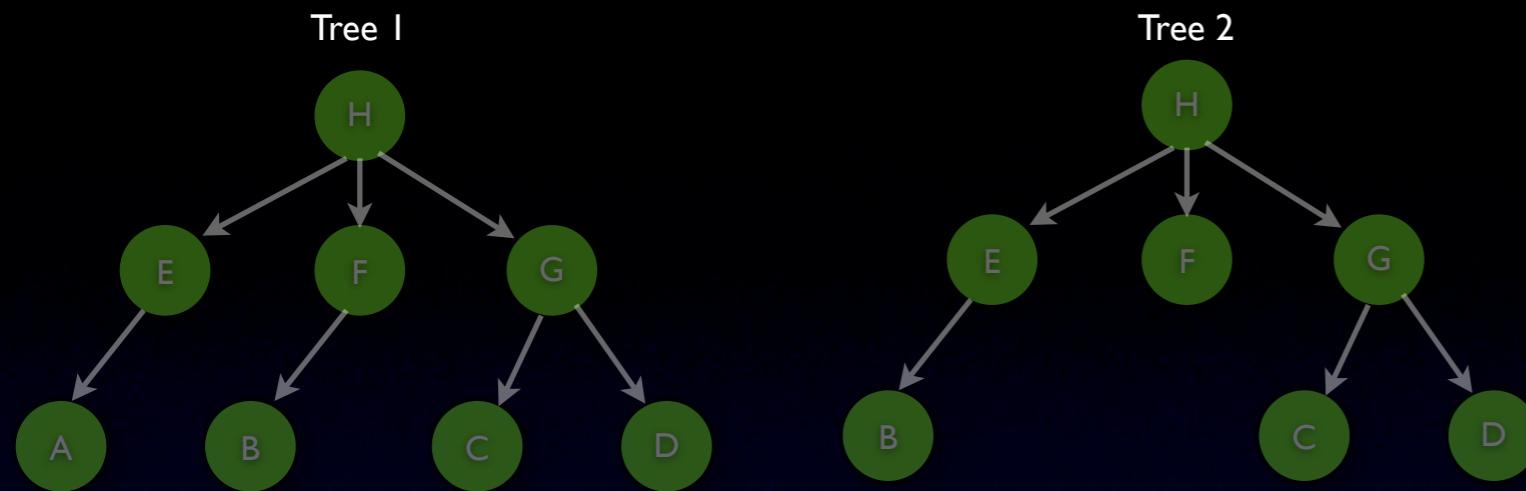
Calculating minimum-Cost matching



$\text{dist}(A,B) = 1$ $\text{dist}(E,E) = 0$ $\text{dist}(H,H) = 0$
 $\text{dist}(C,C) = 0$ $\text{dist}(F,F) = 0$
 $\text{dist}(D,D) = 0$ $\text{dist}(G,G) = 0$

```
Input: Tree  $T_1$  and  $T_2$ .
Output: a minimum-cost matching  $M_{\min}(T_1, T_2)$ .
Initialize: set initial working sets
 $N_1 = \{\text{all leaf nodes in } T_1\}$ ,  $N_2 = \{\text{all leaf nodes in } T_2\}$ .
Set the Distance Table  $DT = \{\}$ .
/* Step 1: Reduce matching space */
Filter out next-level subtrees that have equal XHash values.
/* Step 2: compute editing distance for  $(T_1 \rightarrow T_2)$  */
DO {
  For every node  $x$  in  $N_1$ 
    For every node  $y$  in  $N_2$ 
      If  $\text{Signature}(x) = \text{Signature}(y)$ 
        Compute  $\text{Dist}(x, y)$ ;
        Save matching  $(x, y)$  with  $\text{Dist}(x, y)$  in  $DT$ .
      Set  $N_1 = \{\text{parent nodes of previous nodes in } N_1\}$ ;
      Set  $N_2 = \{\text{parent nodes of previous nodes in } N_2\}$ .
} While (both  $N_1$  and  $N_2$  are not empty).
/* Step 3: mark matchings on  $T_1$  and  $T_2$ . */
Set  $M_{\min}(T_1, T_2) = \{\}$ 
If  $\text{Signature}(\text{Root}(T_1)) \neq \text{Signature}(\text{Root}(T_2))$ 
  Return; /*  $M_{\min}(T_1, T_2) = \{\}$  */
Else
  Add  $(\text{Root}(T_1), \text{Root}(T_2))$  to  $M_{\min}(T_1, T_2)$ .
  For every non-leaf node mapping  $(x, y) \in M_{\min}(T_1, T_2)$ 
    Retrieve matchings between their child nodes that
    are stored in  $DT$ .
    Add child node matchings into  $M_{\min}(T_1, T_2)$ .
```

Calculating minimum-Cost matching

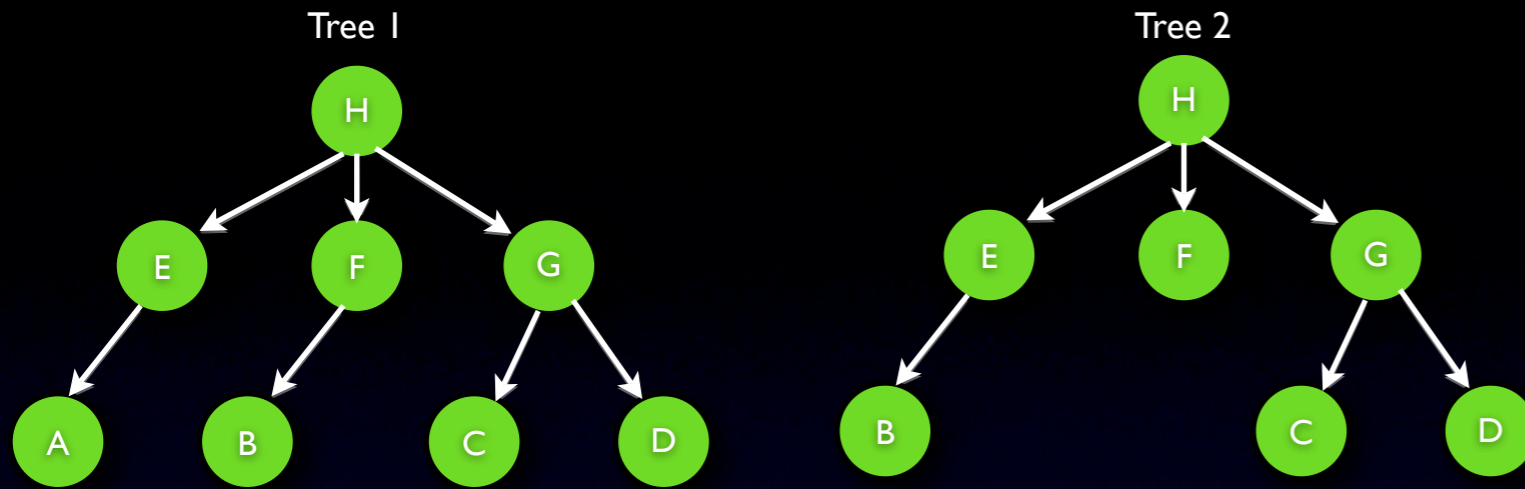


dist(A,B) = 1 dist(E,E) = 0 dist(H,H) = 0
dist(C,C) = 0 dist(F,F) = 0
dist(D,D) = 0 dist(G,G) = 0

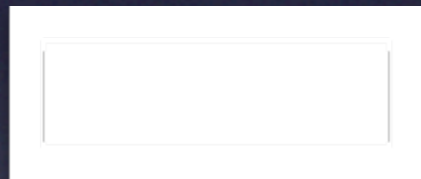
```
Input: Tree T1 and T2.
Output: a minimum-cost matching Mmin(T1, T2).
Initialize: set initial working sets
  N1 = {all leaf nodes in T1}, N2 = {all leaf nodes in T2}.
  Set the Distance Table DT = {}.
/* Step 1: Reduce matching space */
Filter out next-level subtrees that have equal XHash values.
/* Step 2: compute editing distance for (T1 → T2) */
DO {
  For every node x in N1
    For every node y in N2
      If Signature(x) = Signature(y)
        Compute Dist(x, y);
        Save matching (x, y) with Dist(x, y) in DT.
      Set N1 = {parent nodes of previous nodes in N1};
      N2 = {parent nodes of previous nodes in N2}.
  } While (both N1 and N2 are not empty).
/* Step 3: mark matchings on T1 and T2. */
Set Mmin(T1, T2) = {}
If Signature(Root(T1)) ≠ Signature(Root(T2))
  Return; /* Mmin(T1, T2) = {} */
Else
  Add (Root(T1), Root(T2)) to Mmin(T1, T2).
  For every non-leaf node mapping (x, y) ∈ Mmin(T1, T2)
    Retrieve matchings between their child nodes that
    are stored in DT.
    Add child node matchings into Mmin(T1, T2).
```



Creating the upgrade set

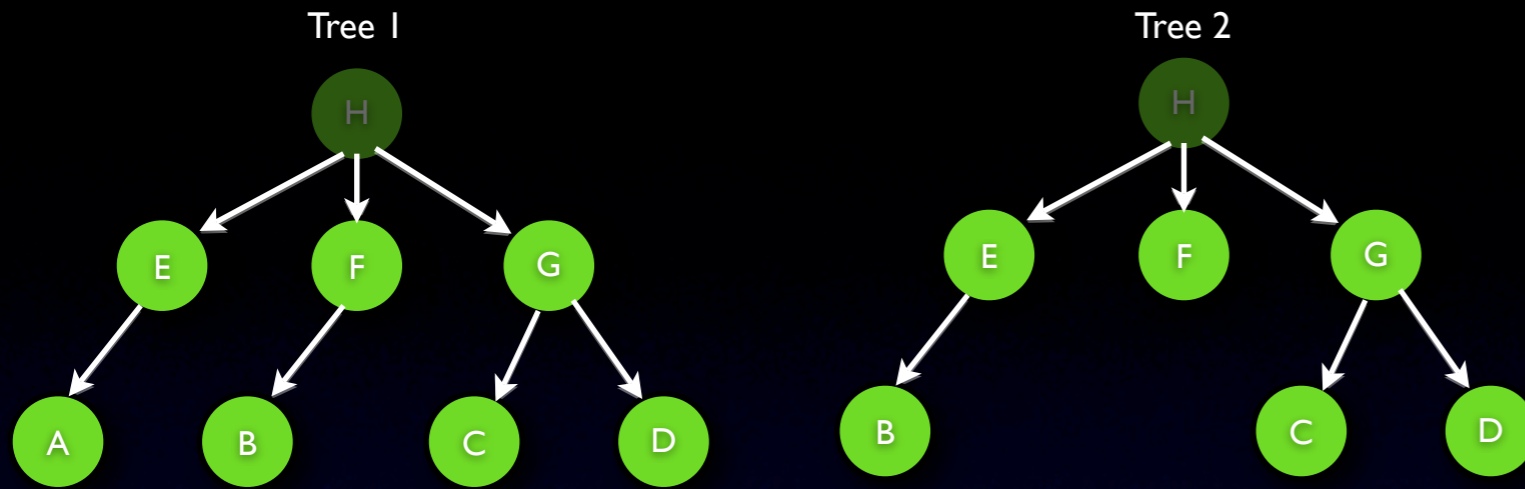


$\text{dist}(A,B) = 1$ $\text{dist}(E,E) = 0$ $\text{dist}(H,H) = 0$
 $\text{dist}(C,C) = 0$ $\text{dist}(F,F) = 0$
 $\text{dist}(D,D) = 0$ $\text{dist}(G,G) = 0$

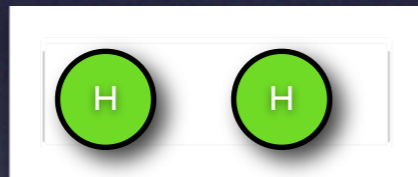


```
Input: Tree  $T_1$  and  $T_2$ , a minimum-cost matching  $M_{\min}(T_1, T_2)$ , the distance table DT.
Output: an edit script E.
Initialize: set E = Null;
 $x = \text{Root}(T_1)$ ,  $y = \text{Root}(T_2)$ .
If  $(x, y) \notin M_{\min}(T_1, T_2)$  /* Subtree deletion and insertion */
    Return "Delete( $T_1$ ), Insert( $T_2$ )".
Else if  $\text{Dist}(T_1, T_2) = 0$ 
    Return "";
Else {
    For every node pair  $(x_i, y_j) \in M_{\min}(T_1, T_2)$ ,  $x_i$  is a child
    node of  $x$ ,  $y_j$  is a child node of  $y$ .
        If  $x_i$  and  $y_j$  are leaf nodes
            If  $\text{Dist}(x_i, y_j) = 0$ 
                Return "";
            Else /* Update leaf node */
                Add Update( $x_i$ , Value( $y_j$ )) to E;
        Else /* Call subtree matching */
            Add EditScript( $T_{x_i}$ ,  $T_{y_j}$ ) to E;
    Return E;
    For every node  $x_i$  not in  $M_{\min}(T_1, T_2)$ 
        Add "Delete( $T_{x_i}$ )" to E;
    For every node  $y_j$  not in  $M_{\min}(T_1, T_2)$ 
        Add "Insert( $T_{y_j}$ )" to E;
    Return E }
```

Creating the upgrade set



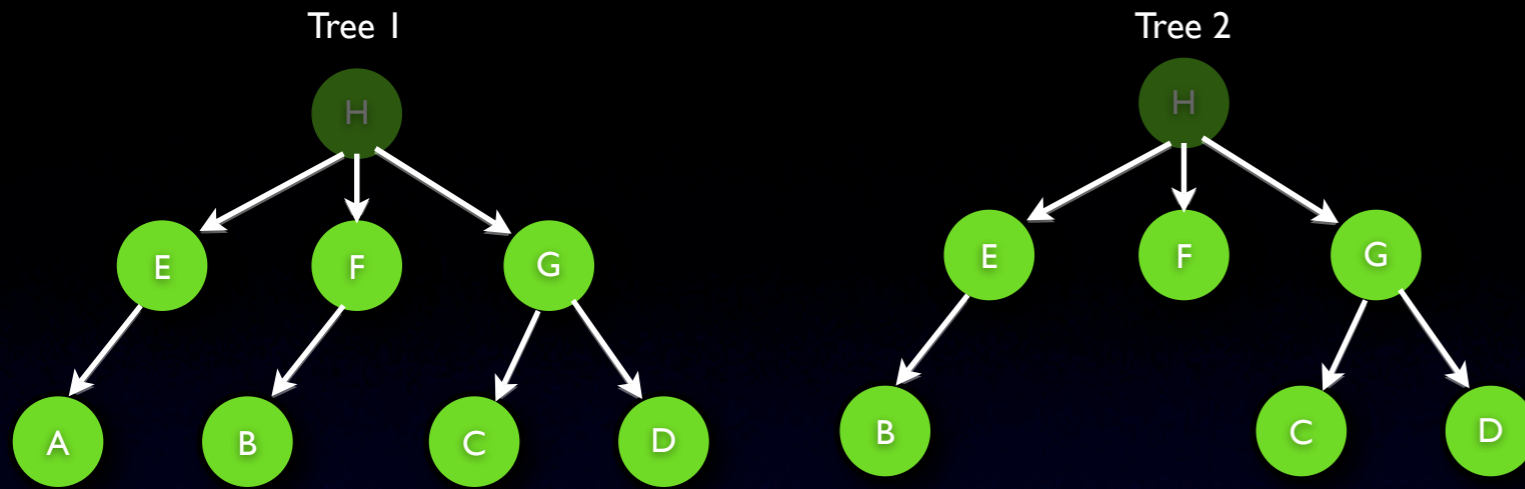
$\text{dist}(A,B) = 1$ $\text{dist}(E,E) = 0$ $\text{dist}(H,H) = 0$
 $\text{dist}(C,C) = 0$ $\text{dist}(F,F) = 0$
 $\text{dist}(D,D) = 0$ $\text{dist}(G,G) = 0$



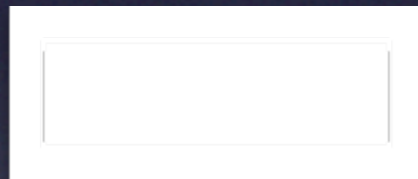
```

Input: Tree  $T_1$  and  $T_2$ , a minimum-cost matching  $M_{\min}(T_1, T_2)$ , the distance table  $DT$ .
Output: an edit script  $E$ .
Initialize: set  $E = \text{Null}$ ;
 $x = \text{Root}(T_1)$ ,  $y = \text{Root}(T_2)$ .
If  $(x, y) \notin M_{\min}(T_1, T_2)$  /* Subtree deletion and insertion */
    Return "Delete( $T_1$ ), Insert( $T_2$ )".
Else if  $\text{Dist}(T_1, T_2) = 0$ 
    Return "";
Else {
    For every node pair  $(x_i, y_j) \in M_{\min}(T_1, T_2)$ ,  $x_i$  is a child node of  $x$ ,  $y_j$  is a child node of  $y$ .
        If  $x_i$  and  $y_j$  are leaf nodes
            If  $\text{Dist}(x_i, y_j) = 0$ 
                Return "";
            Else /* Update leaf node */
                Add Update( $x_i$ , Value( $y_j$ )) to  $E$ ;
        Else /* Call subtree matching */
            Add EditScript( $T_{x_i}$ ,  $T_{y_j}$ ) to  $E$ ;
    Return  $E$ ;
    For every node  $x_i$  not in  $M_{\min}(T_1, T_2)$ 
        Add "Delete( $T_{x_i}$ )" to  $E$ ;
    For every node  $y_j$  not in  $M_{\min}(T_1, T_2)$ 
        Add "Insert( $T_{y_j}$ )" to  $E$ ;
    Return  $E$ ;
}
    
```

Creating the upgrade set

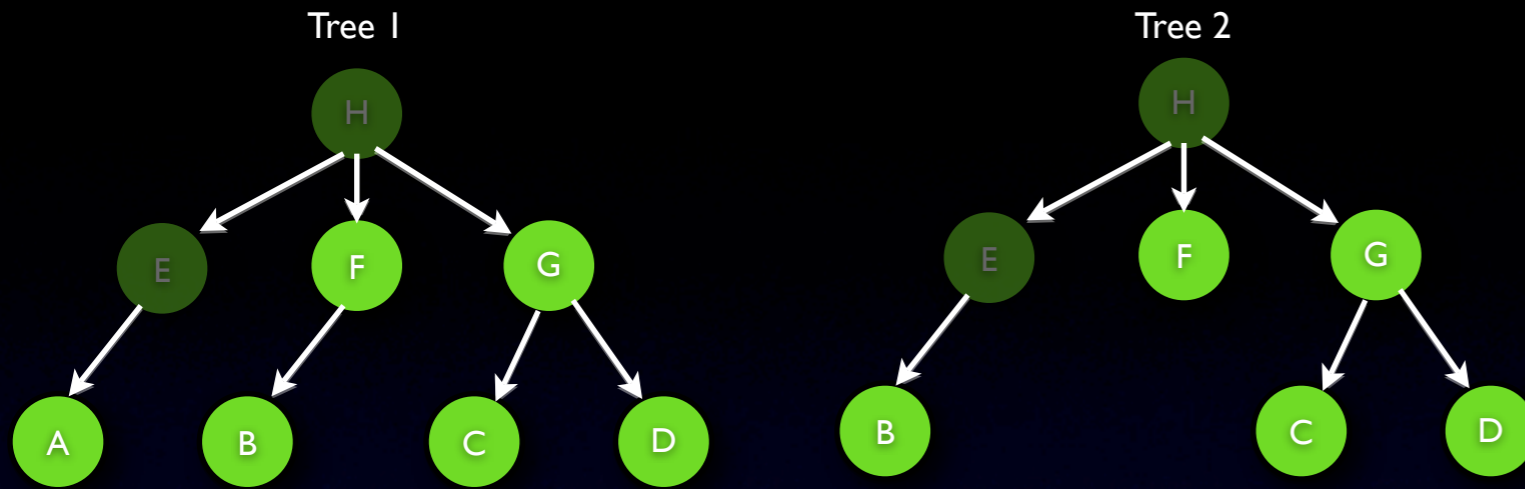


$\text{dist}(A,B) = 1$ $\text{dist}(E,E) = 0$ $\text{dist}(H,H) = 0$
 $\text{dist}(C,C) = 0$ $\text{dist}(F,F) = 0$
 $\text{dist}(D,D) = 0$ $\text{dist}(G,G) = 0$



```
Input: Tree  $T_1$  and  $T_2$ , a minimum-cost matching  $M_{\min}(T_1, T_2)$ , the distance table  $DT$ .
Output: an edit script  $E$ .
Initialize: set  $E = \text{Null}$ ;
 $x = \text{Root}(T_1)$ ,  $y = \text{Root}(T_2)$ .
If  $(x, y) \notin M_{\min}(T_1, T_2)$  /* Subtree deletion and insertion */
    Return "Delete( $T_1$ ), Insert( $T_2$ )".
Else if  $\text{Dist}(T_1, T_2) = 0$ 
    Return "";
Else {
    For every node pair  $(x_i, y_j) \in M_{\min}(T_1, T_2)$ ,  $x_i$  is a child
    node of  $x$ ,  $y_j$  is a child node of  $y$ .
    If  $x_i$  and  $y_j$  are leaf nodes
        If  $\text{Dist}(x_i, y_j) = 0$ 
            Return "";
        Else /* Update leaf node */
            Add Update( $x_i$ , Value( $y_j$ )) to  $E$ ;
    Else /* Call subtree matching */
        Add EditScript( $T_{x_i}$ ,  $T_{y_j}$ ) to  $E$ ;
    Return  $E$ ;
}
For every node  $x_i$  not in  $M_{\min}(T_1, T_2)$ 
    Add "Delete( $T_{x_i}$ )" to  $E$ ;
For every node  $y_j$  not in  $M_{\min}(T_1, T_2)$ 
    Add "Insert( $T_{y_j}$ )" to  $E$ ;
Return  $E$  }
```

Creating the upgrade set



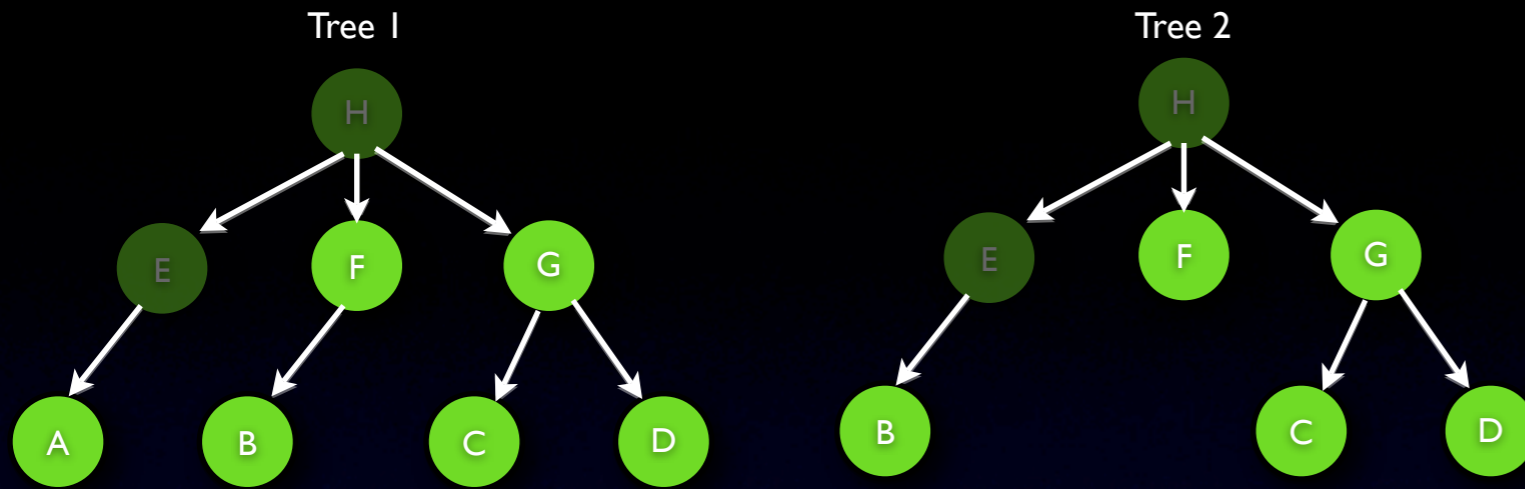
$\text{dist}(A,B) = 1$ $\text{dist}(E,E) = 0$ $\text{dist}(H,H) = 0$
 $\text{dist}(C,C) = 0$ $\text{dist}(F,F) = 0$
 $\text{dist}(D,D) = 0$ $\text{dist}(G,G) = 0$



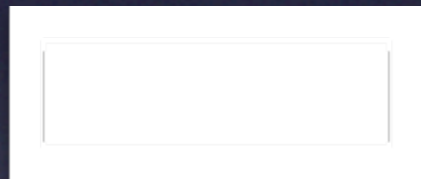
```
Input: Tree  $T_1$  and  $T_2$ , a minimum-cost matching  $M_{\min}(T_1, T_2)$ , the distance table  $DT$ .
Output: an edit script  $E$ .
Initialize: set  $E = \text{Null}$ ;
 $x = \text{Root}(T_1)$ ,  $y = \text{Root}(T_2)$ .
If  $(x, y) \notin M_{\min}(T_1, T_2)$  /* Subtree deletion and insertion */
  Return "Delete( $T_1$ ), Insert( $T_2$ )".
Else if  $\text{Dist}(T_1, T_2) = 0$ 
  Return "";
Else {
  For every node pair  $(x_i, y_j) \in M_{\min}(T_1, T_2)$ ,  $x_i$  is a child
  node of  $x$ ,  $y_j$  is a child node of  $y$ .
  If  $x_i$  and  $y_j$  are leaf nodes
    If  $\text{Dist}(x_i, y_j) = 0$ 
      Return "";
    Else /* Update leaf node */
      Add Update( $x_i$ , Value( $y_j$ )) to  $E$ ;
  Else /* Call subtree matching */
    Add EditScript( $T_{x_i}$ ,  $T_{y_j}$ ) to  $E$ ;
  Return  $E$ ;
  For every node  $x_i$  not in  $M_{\min}(T_1, T_2)$ 
    Add "Delete( $T_{x_i}$ )" to  $E$ ;
  For every node  $y_j$  not in  $M_{\min}(T_1, T_2)$ 
    Add "Insert( $T_{y_j}$ )" to  $E$ ;
  Return  $E$  }
```



Creating the upgrade set



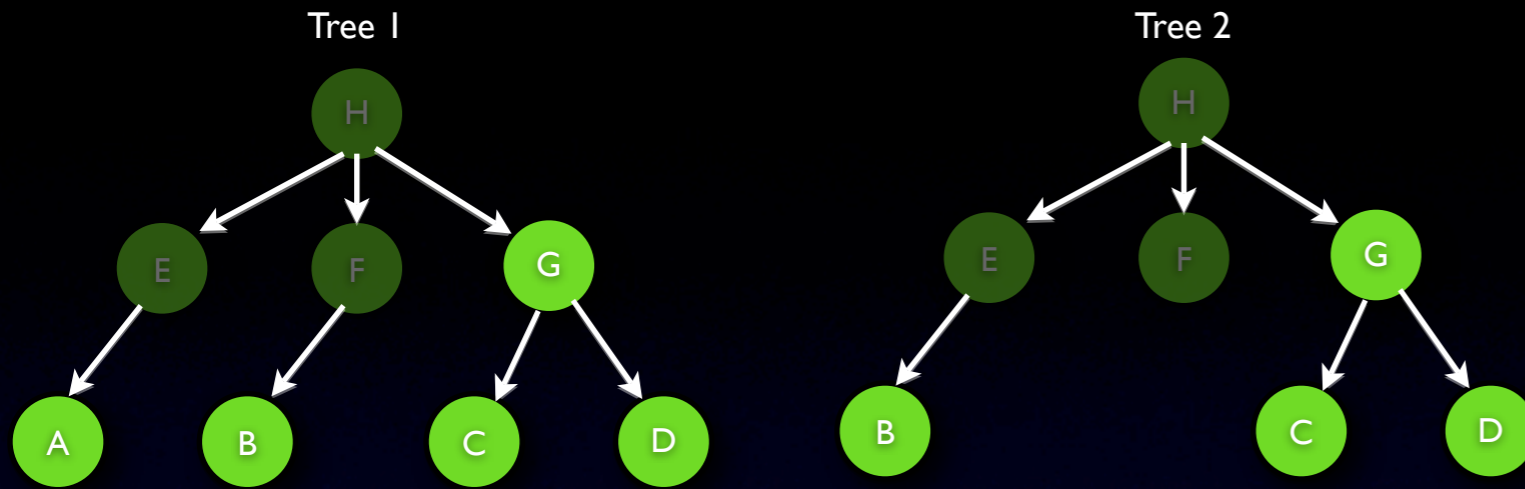
$\text{dist}(A,B) = 1$ $\text{dist}(E,E) = 0$ $\text{dist}(H,H) = 0$
 $\text{dist}(C,C) = 0$ $\text{dist}(F,F) = 0$
 $\text{dist}(D,D) = 0$ $\text{dist}(G,G) = 0$



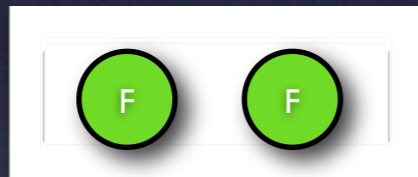
```

Input: Tree  $T_1$  and  $T_2$ , a minimum-cost matching  $M_{\min}(T_1, T_2)$ , the distance table  $DT$ .
Output: an edit script  $E$ .
Initialize: set  $E = \text{Null}$ ;
 $x = \text{Root}(T_1)$ ,  $y = \text{Root}(T_2)$ .
If  $(x, y) \notin M_{\min}(T_1, T_2)$  /* Subtree deletion and insertion */
    Return "Delete( $T_1$ ), Insert( $T_2$ )".
Else if  $\text{Dist}(T_1, T_2) = 0$ 
    Return "";
Else {
    For every node pair  $(x_i, y_j) \in M_{\min}(T_1, T_2)$ ,  $x_i$  is a child
    node of  $x$ ,  $y_j$  is a child node of  $y$ .
        If  $x_i$  and  $y_j$  are leaf nodes
            If  $\text{Dist}(x_i, y_j) = 0$ 
                Return "";
            Else /* Update leaf node */
                Add Update( $x_i$ , Value( $y_j$ )) to  $E$ ;
        Else /* Call subtree matching */
            Add EditScript( $T_{x_i}$ ,  $T_{y_j}$ ) to  $E$ ;
    Return  $E$ ;
    For every node  $x_i$  not in  $M_{\min}(T_1, T_2)$ 
        Add "Delete( $T_{x_i}$ )" to  $E$ ;
    For every node  $y_j$  not in  $M_{\min}(T_1, T_2)$ 
        Add "Insert( $T_{y_j}$ )" to  $E$ ;
    Return  $E$ ;
}
    
```

Creating the upgrade set



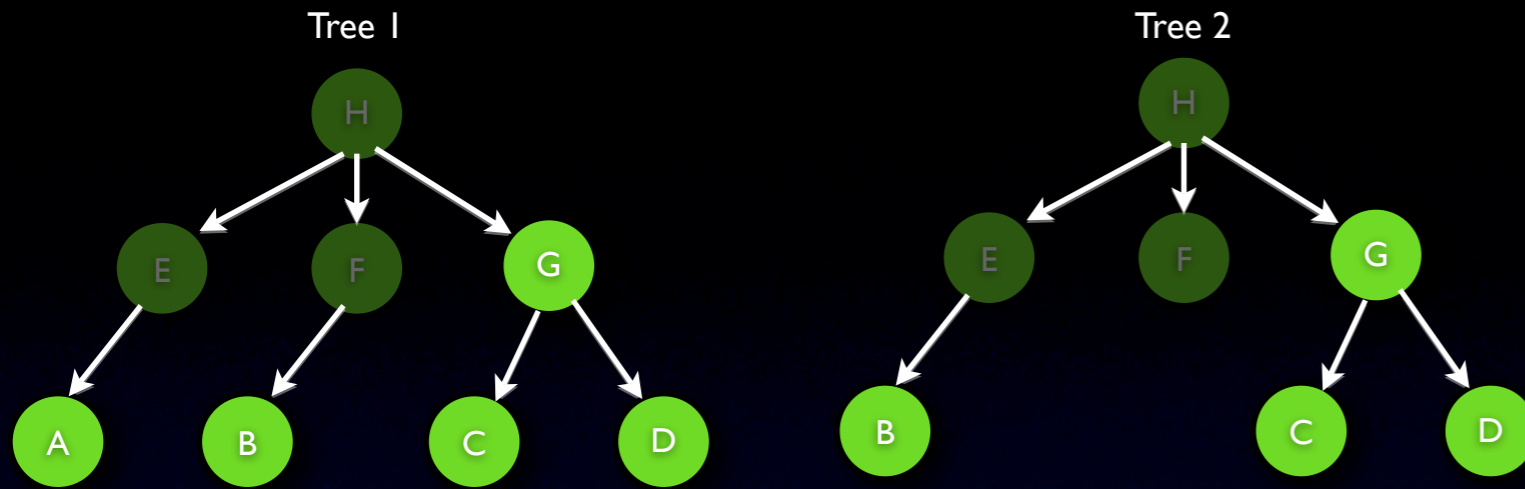
$\text{dist}(A,B) = 1$ $\text{dist}(E,E) = 0$ $\text{dist}(H,H) = 0$
 $\text{dist}(C,C) = 0$ $\text{dist}(F,F) = 0$
 $\text{dist}(D,D) = 0$ $\text{dist}(G,G) = 0$



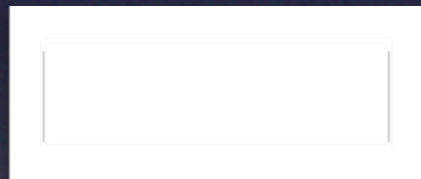
```

Input: Tree  $T_1$  and  $T_2$ , a minimum-cost matching  $M_{\min}(T_1, T_2)$ , the distance table DT.
Output: an edit script E.
Initialize: set E = Null;
 $x = \text{Root}(T_1)$ ,  $y = \text{Root}(T_2)$ .
If  $(x, y) \notin M_{\min}(T_1, T_2)$  /* Subtree deletion and insertion */
    Return "Delete( $T_1$ ), Insert( $T_2$ )".
Else if  $\text{Dist}(T_1, T_2) = 0$ 
    Return "";
Else {
    For every node pair  $(x_i, y_j) \in M_{\min}(T_1, T_2)$ ,  $x_i$  is a child node of x,  $y_j$  is a child node of y.
        If  $x_i$  and  $y_j$  are leaf nodes
            If  $\text{Dist}(x_i, y_j) = 0$ 
                Return "";
            Else /* Update leaf node */
                Add Update( $x_i$ , Value( $y_j$ )) to E;
        Else /* Call subtree matching */
            Add EditScript( $T_{x_i}$ ,  $T_{y_j}$ ) to E;
    Return E;
    For every node  $x_i$  not in  $M_{\min}(T_1, T_2)$ 
        Add "Delete( $T_{x_i}$ )" to E;
    For every node  $y_j$  not in  $M_{\min}(T_1, T_2)$ 
        Add "Insert( $T_{y_j}$ )" to E;
    Return E;
}
    
```

Creating the upgrade set

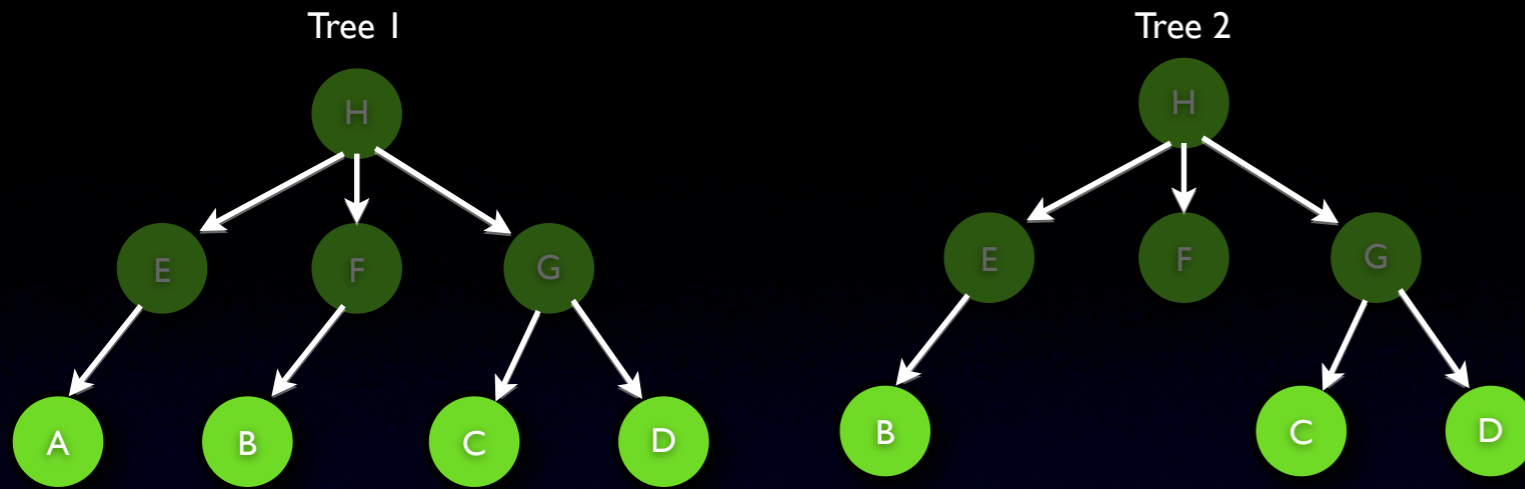


$\text{dist}(A,B) = 1$ $\text{dist}(E,E) = 0$ $\text{dist}(H,H) = 0$
 $\text{dist}(C,C) = 0$ $\text{dist}(F,F) = 0$
 $\text{dist}(D,D) = 0$ $\text{dist}(G,G) = 0$



```
Input: Tree  $T_1$  and  $T_2$ , a minimum-cost matching  $M_{\min}(T_1, T_2)$ , the distance table DT.  
Output: an edit script E.  
Initialize: set E = Null;  
 $x = \text{Root}(T_1)$ ,  $y = \text{Root}(T_2)$ .  
If  $(x, y) \notin M_{\min}(T_1, T_2)$  /* Subtree deletion and insertion */  
  Return "Delete( $T_1$ ), Insert( $T_2$ )".  
Else if  $\text{Dist}(T_1, T_2) = 0$   
  Return "";  
Else {  
  For every node pair  $(x_i, y_j) \in M_{\min}(T_1, T_2)$ ,  $x_i$  is a child  
  node of  $x$ ,  $y_j$  is a child node of  $y$ .  
  If  $x_i$  and  $y_j$  are leaf nodes  
    If  $\text{Dist}(x_i, y_j) = 0$   
      Return "";  
    Else /* Update leaf node */  
      Add Update( $x_i$ , Value( $y_j$ )) to E;  
  Else /* Call subtree matching */  
    Add EditScript( $T_{x_i}$ ,  $T_{y_j}$ ) to E;  
  Return E;  
  For every node  $x_i$  not in  $M_{\min}(T_1, T_2)$   
    Add "Delete( $T_{x_i}$ )" to E;  
  For every node  $y_j$  not in  $M_{\min}(T_1, T_2)$   
    Add "Insert( $T_{y_j}$ )" to E;  
  Return E };
```

Creating the upgrade set



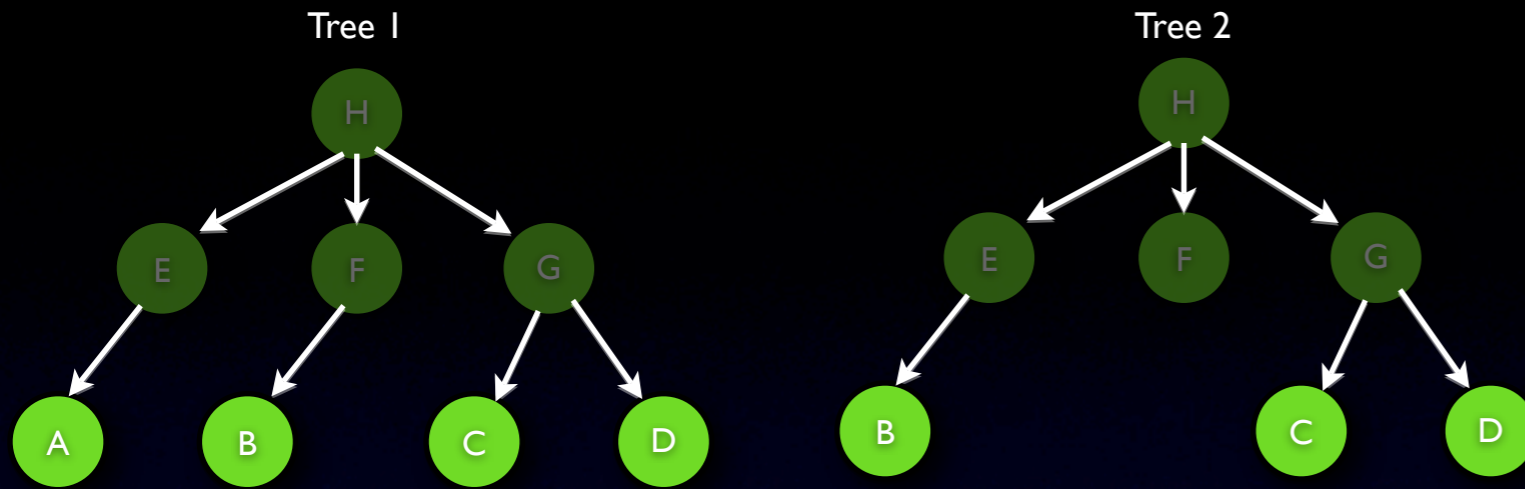
$\text{dist}(A,B) = 1$ $\text{dist}(E,E) = 0$ $\text{dist}(H,H) = 0$
 $\text{dist}(C,C) = 0$ $\text{dist}(F,F) = 0$
 $\text{dist}(D,D) = 0$ $\text{dist}(G,G) = 0$



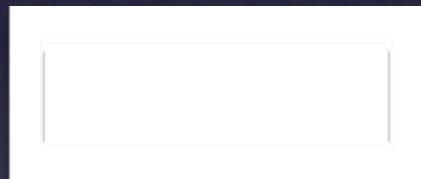
```

Input: Tree  $T_1$  and  $T_2$ , a minimum-cost matching  $M_{\min}(T_1, T_2)$ , the distance table  $DT$ .
Output: an edit script  $E$ .
Initialize: set  $E = \text{Null}$ ;
 $x = \text{Root}(T_1)$ ,  $y = \text{Root}(T_2)$ .
If  $(x, y) \notin M_{\min}(T_1, T_2)$  /* Subtree deletion and insertion */
    Return "Delete( $T_1$ ), Insert( $T_2$ )".
Else if  $\text{Dist}(T_1, T_2) = 0$ 
    Return "";
Else {
    For every node pair  $(x_i, y_j) \in M_{\min}(T_1, T_2)$ ,  $x_i$  is a child
    node of  $x$ ,  $y_j$  is a child node of  $y$ .
        If  $x_i$  and  $y_j$  are leaf nodes
            If  $\text{Dist}(x_i, y_j) = 0$ 
                Return "";
            Else /* Update leaf node */
                Add Update( $x_i$ , Value( $y_j$ )) to  $E$ ;
        Else /* Call subtree matching */
            Add EditScript( $T_{x_i}$ ,  $T_{y_j}$ ) to  $E$ ;
    Return  $E$ ;
    For every node  $x_i$  not in  $M_{\min}(T_1, T_2)$ 
        Add "Delete( $T_{x_i}$ )" to  $E$ ;
    For every node  $y_j$  not in  $M_{\min}(T_1, T_2)$ 
        Add "Insert( $T_{y_j}$ )" to  $E$ ;
    Return  $E$ ;
}
    
```

Creating the upgrade set

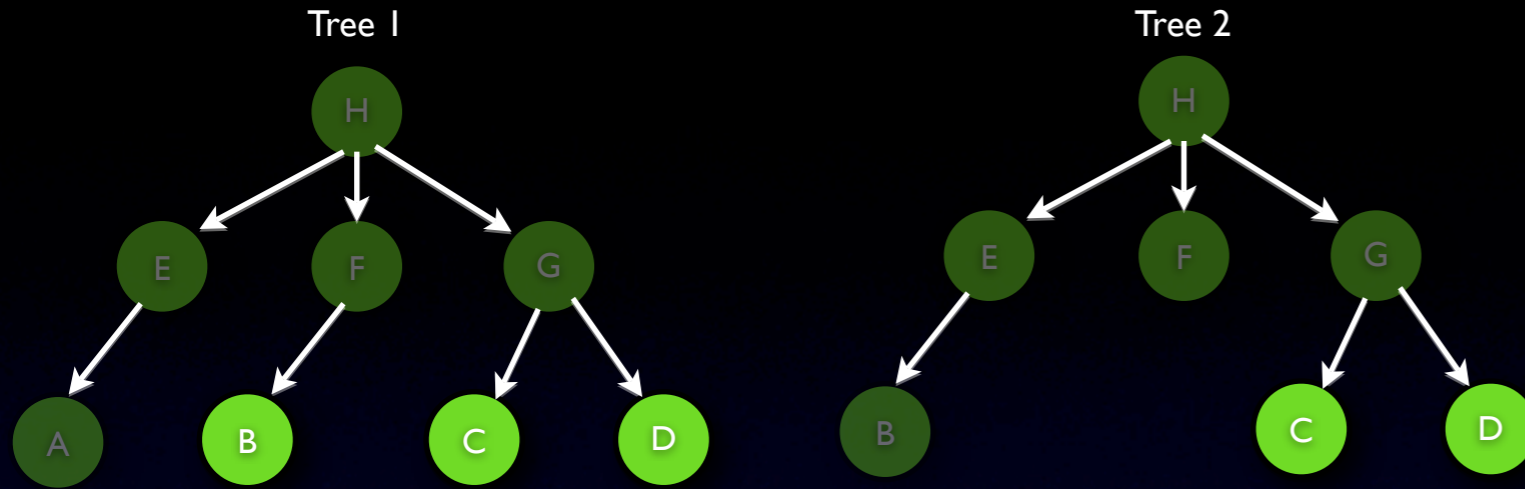


$\text{dist}(A,B) = 1$ $\text{dist}(E,E) = 0$ $\text{dist}(H,H) = 0$
 $\text{dist}(C,C) = 0$ $\text{dist}(F,F) = 0$
 $\text{dist}(D,D) = 0$ $\text{dist}(G,G) = 0$

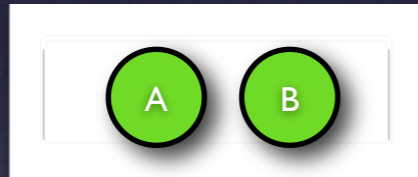


```
Input: Tree  $T_1$  and  $T_2$ , a minimum-cost matching  $M_{\min}(T_1, T_2)$ , the distance table  $DT$ .
Output: an edit script  $E$ .
Initialize: set  $E = \text{Null}$ ;
 $x = \text{Root}(T_1)$ ,  $y = \text{Root}(T_2)$ .
If  $(x, y) \notin M_{\min}(T_1, T_2)$  /* Subtree deletion and insertion */
    Return "Delete( $T_1$ ), Insert( $T_2$ )".
Else if  $\text{Dist}(T_1, T_2) = 0$ 
    Return "";
Else {
    For every node pair  $(x_i, y_j) \in M_{\min}(T_1, T_2)$ ,  $x_i$  is a child
    node of  $x$ ,  $y_j$  is a child node of  $y$ .
        If  $x_i$  and  $y_j$  are leaf nodes
            If  $\text{Dist}(x_i, y_j) = 0$ 
                Return "";
            Else /* Update leaf node */
                Add Update( $x_i$ , Value( $y_j$ )) to  $E$ ;
        Else /* Call subtree matching */
            Add EditScript( $T_{x_i}$ ,  $T_{y_j}$ ) to  $E$ ;
    Return  $E$ ;
For every node  $x_i$  not in  $M_{\min}(T_1, T_2)$ 
    Add "Delete( $T_{x_i}$ )" to  $E$ ;
For every node  $y_j$  not in  $M_{\min}(T_1, T_2)$ 
    Add "Insert( $T_{y_j}$ )" to  $E$ ;
Return  $E$  }
```

Creating the upgrade set



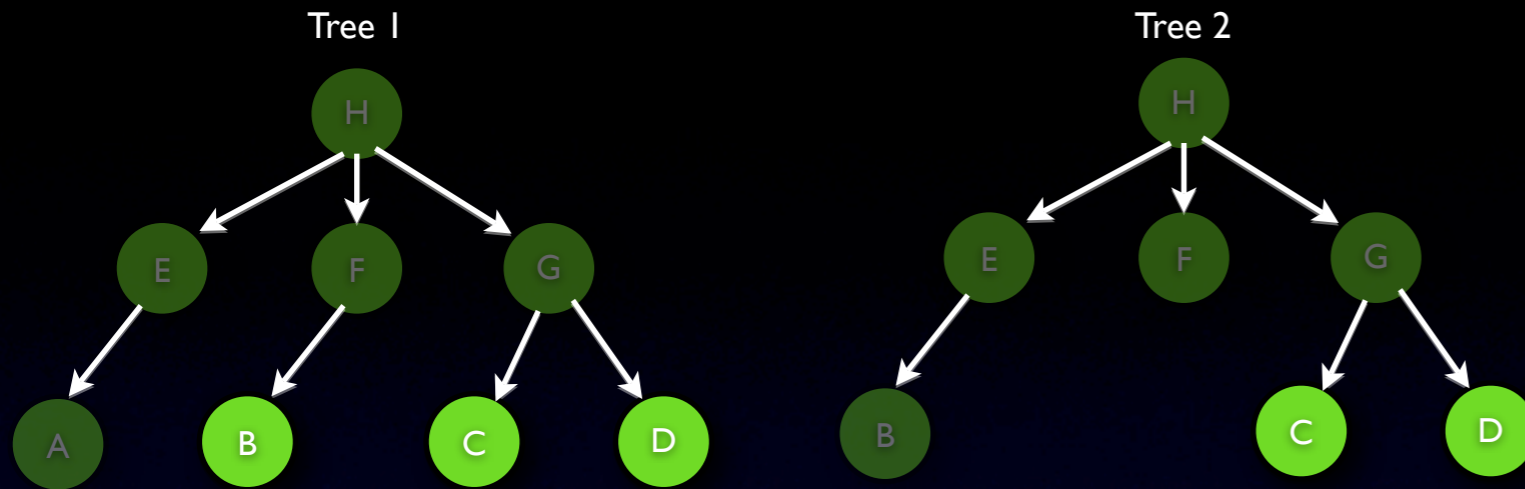
$\text{dist}(A,B) = 1$ $\text{dist}(E,E) = 0$ $\text{dist}(H,H) = 0$
 $\text{dist}(C,C) = 0$ $\text{dist}(F,F) = 0$
 $\text{dist}(D,D) = 0$ $\text{dist}(G,G) = 0$



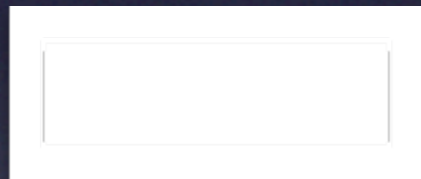
update(A,B)

```
Input: Tree  $T_1$  and  $T_2$ , a minimum-cost matching  $M_{\min}(T_1, T_2)$ , the distance table DT.  
Output: an edit script E.  
Initialize: set E = Null;  
 $x = \text{Root}(T_1)$ ,  $y = \text{Root}(T_2)$ .  
If  $(x, y) \notin M_{\min}(T_1, T_2)$  /* Subtree deletion and insertion */  
  Return "Delete( $T_1$ ), Insert( $T_2$ )".  
Else if  $\text{Dist}(T_1, T_2) = 0$   
  Return "";  
Else {  
  For every node pair  $(x_i, y_j) \in M_{\min}(T_1, T_2)$ ,  $x_i$  is a child node of  $x$ ,  $y_j$  is a child node of  $y$ .  
  If  $x_i$  and  $y_j$  are leaf nodes  
    If  $\text{Dist}(x_i, y_j) = 0$   
      Return "";  
    Else /* Update leaf node */  
      Add Update( $x_i$ , Value( $y_j$ )) to E;  
  Else /* Call subtree matching */  
    Add EditScript( $T_{x_i}$ ,  $T_{y_j}$ ) to E;  
  Return E;  
  For every node  $x_i$  not in  $M_{\min}(T_1, T_2)$   
    Add "Delete( $T_{x_i}$ )" to E;  
  For every node  $y_j$  not in  $M_{\min}(T_1, T_2)$   
    Add "Insert( $T_{y_j}$ )" to E;  
  Return E };
```

Creating the upgrade set



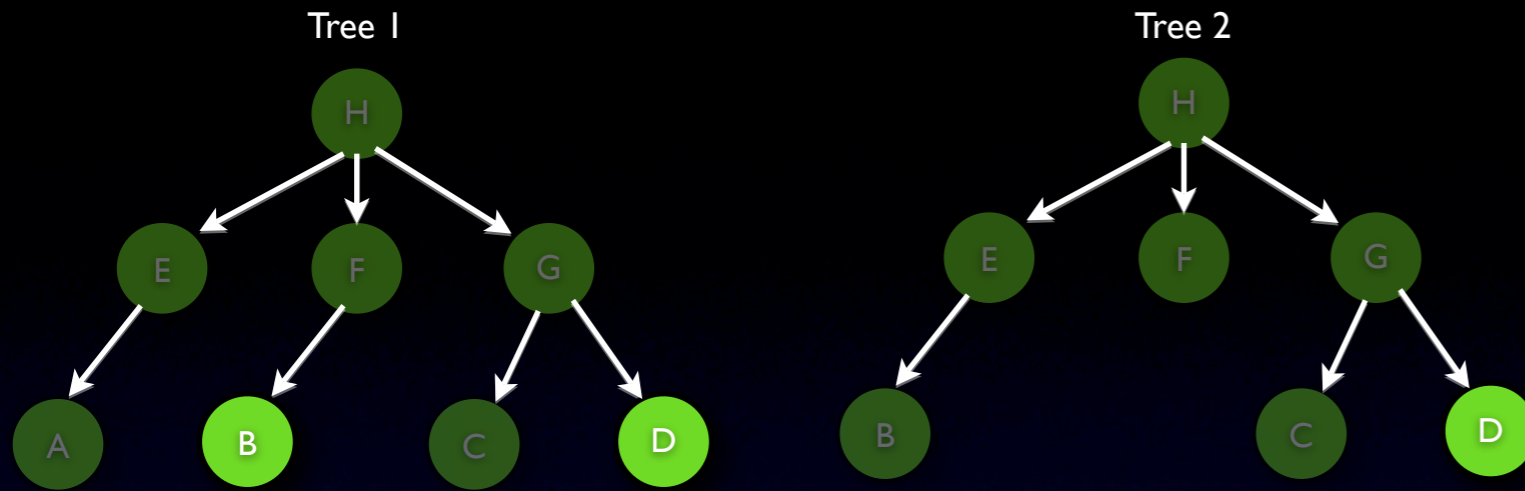
dist(A,B) = 1 dist(E,E) = 0 dist(H,H) = 0
dist(C,C) = 0 dist(F,F) = 0
dist(D,D) = 0 dist(G,G) = 0



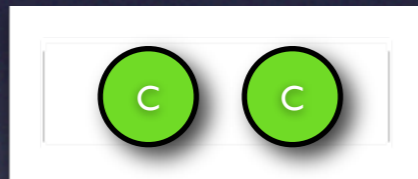
update(A,B)

```
Input: Tree T1 and T2, a minimum-cost matching Mmin(T1, T2), the distance table DT.  
Output: an edit script E.  
Initialize: set E = Null;  
x = Root(T1), y = Root(T2).  
If (x, y) ∉ Mmin(T1, T2) /* Subtree deletion and insertion */  
    Return "Delete(T1), Insert(T2)".  
Else if Dist(T1, T2) = 0  
    Return "";  
Else {  
    For every node pair (xi, yj) ∈ Mmin(T1, T2), xi is a child  
    node of x, yj is a child node of y.  
        If xi and yj are leaf nodes  
            If Dist(xi, yj) = 0  
                Return "";  
            Else /* Update leaf node */  
                Add Update(xi, Value(yj)) to E;  
        Else /* Call subtree matching */  
            Add EditScript(Txi, Tyj) to E;  
    Return E;  
    For every node xi not in Mmin(T1, T2)  
        Add "Delete(Txi)" to E;  
    For every node yj not in Mmin(T1, T2)  
        Add "Insert(Tyj)" to E;  
    Return E };
```

Creating the upgrade set



$\text{dist}(A,B) = 1$ $\text{dist}(E,E) = 0$ $\text{dist}(H,H) = 0$
 $\text{dist}(C,C) = 0$ $\text{dist}(F,F) = 0$
 $\text{dist}(D,D) = 0$ $\text{dist}(G,G) = 0$

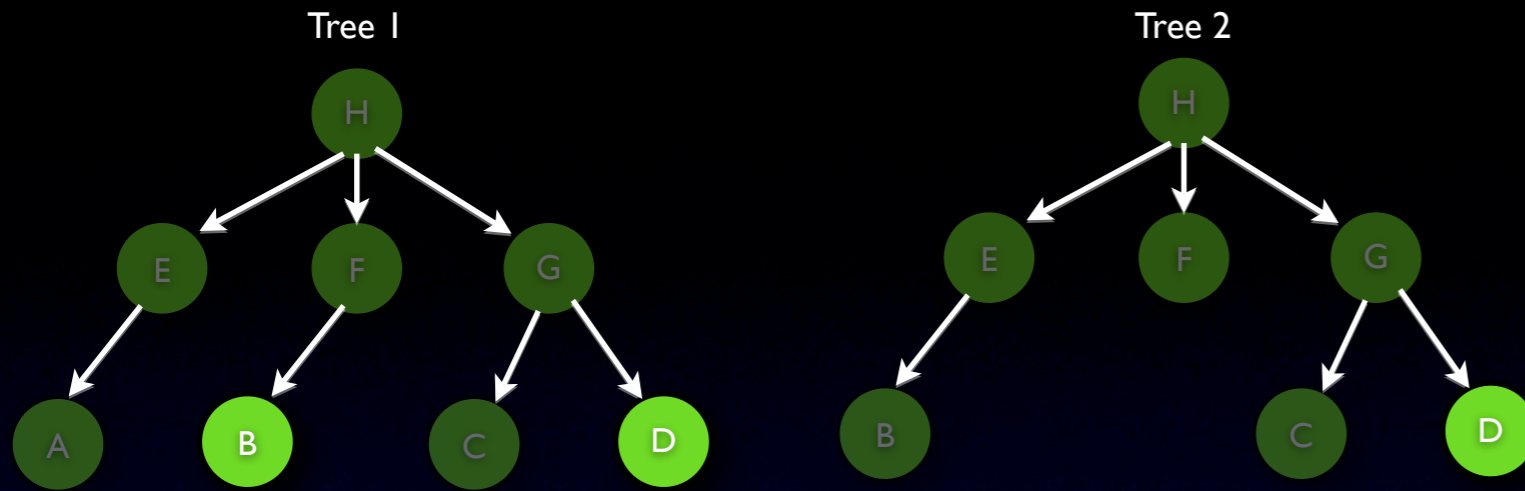


update(A,B)

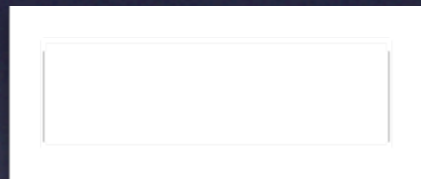
```

Input: Tree  $T_1$  and  $T_2$ , a minimum-cost matching  $M_{\min}(T_1, T_2)$ , the distance table DT.
Output: an edit script E.
Initialize: set E = Null;
 $x = \text{Root}(T_1)$ ,  $y = \text{Root}(T_2)$ .
If  $(x, y) \notin M_{\min}(T_1, T_2)$  /* Subtree deletion and insertion */
    Return "Delete( $T_1$ ), Insert( $T_2$ )".
Else if  $\text{Dist}(T_1, T_2) = 0$ 
    Return "";
Else {
    For every node pair  $(x_i, y_j) \in M_{\min}(T_1, T_2)$ ,  $x_i$  is a child node of  $x$ ,  $y_j$  is a child node of  $y$ .
        If  $x_i$  and  $y_j$  are leaf nodes
            If  $\text{Dist}(x_i, y_j) = 0$ 
                Return "";
            Else /* Update leaf node */
                Add Update( $x_i$ , Value( $y_j$ )) to E;
        Else /* Call subtree matching */
            Add EditScript( $T_{x_i}$ ,  $T_{y_j}$ ) to E;
    Return E;
    For every node  $x_i$  not in  $M_{\min}(T_1, T_2)$ 
        Add "Delete( $T_{x_i}$ )" to E;
    For every node  $y_j$  not in  $M_{\min}(T_1, T_2)$ 
        Add "Insert( $T_{y_j}$ )" to E;
    Return E;
}
    
```

Creating the upgrade set



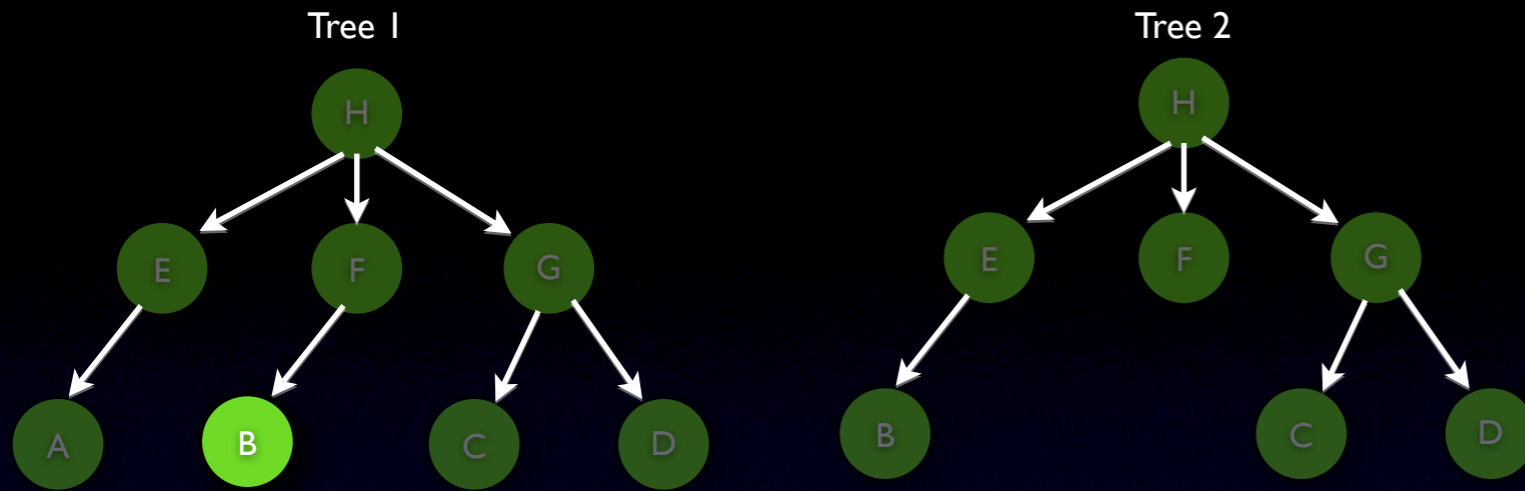
dist(A,B) = 1 dist(E,E) = 0 dist(H,H) = 0
dist(C,C) = 0 dist(F,F) = 0
dist(D,D) = 0 dist(G,G) = 0



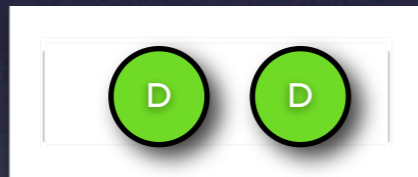
update(A,B)

```
Input: Tree T1 and T2, a minimum-cost matching Mmin(T1, T2), the distance table DT.  
Output: an edit script E.  
Initialize: set E = Null;  
x = Root(T1), y = Root(T2).  
If (x, y) ∉ Mmin(T1, T2) /* Subtree deletion and insertion */  
    Return "Delete(T1), Insert(T2)".  
Else if Dist(T1, T2) = 0  
    Return "";  
Else {  
    For every node pair (xi, yj) ∈ Mmin(T1, T2), xi is a child  
    node of x, yj is a child node of y.  
        If xi and yj are leaf nodes  
            If Dist(xi, yj) = 0  
                Return "";  
            Else /* Update leaf node */  
                Add Update(xi, Value(yj)) to E;  
        Else /* Call subtree matching */  
            Add EditScript(Txi, Tyj) to E;  
    Return E;  
    For every node xi not in Mmin(T1, T2)  
        Add "Delete(Txi)" to E;  
    For every node yj not in Mmin(T1, T2)  
        Add "Insert(Tyj)" to E;  
    Return E };
```

Creating the upgrade set



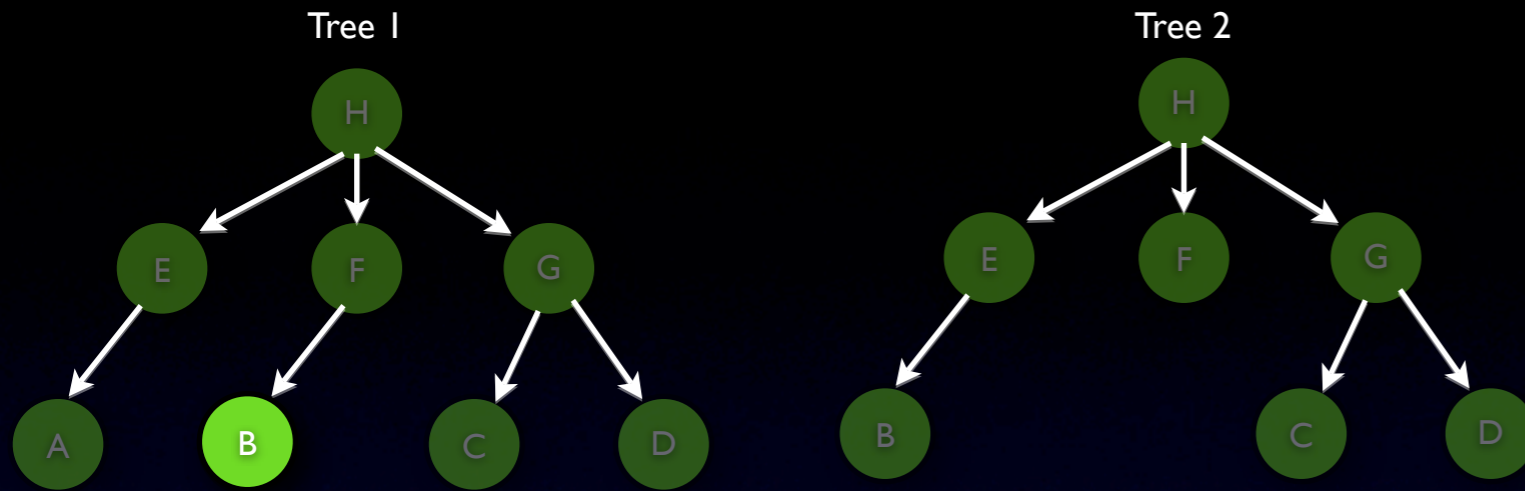
$\text{dist}(A,B) = 1$ $\text{dist}(E,E) = 0$ $\text{dist}(H,H) = 0$
 $\text{dist}(C,C) = 0$ $\text{dist}(F,F) = 0$
 $\text{dist}(D,D) = 0$ $\text{dist}(G,G) = 0$



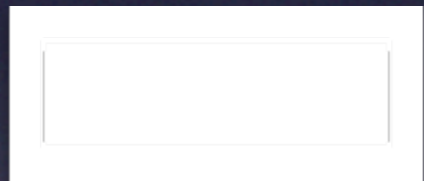
update(A,B)

```
Input: Tree  $T_1$  and  $T_2$ , a minimum-cost matching  $M_{\min}(T_1, T_2)$ , the distance table DT.  
Output: an edit script E.  
Initialize: set E = Null;  
 $x = \text{Root}(T_1)$ ,  $y = \text{Root}(T_2)$ .  
If  $(x, y) \notin M_{\min}(T_1, T_2)$  /* Subtree deletion and insertion */  
    Return "Delete( $T_1$ ), Insert( $T_2$ )".  
Else if  $\text{Dist}(T_1, T_2) = 0$   
    Return "";  
Else {  
    For every node pair  $(x_i, y_j) \in M_{\min}(T_1, T_2)$ ,  $x_i$  is a child  
    node of  $x$ ,  $y_j$  is a child node of  $y$ .  
    If  $x_i$  and  $y_j$  are leaf nodes  
        If  $\text{Dist}(x_i, y_j) = 0$   
            Return "";  
        Else /* Update leaf node */  
            Add Update( $x_i$ , Value( $y_j$ )) to E;  
    Else /* Call subtree matching */  
        Add EditScript( $T_{x_i}$ ,  $T_{y_j}$ ) to E;  
    Return E;  
    For every node  $x_i$  not in  $M_{\min}(T_1, T_2)$   
        Add "Delete( $T_{x_i}$ )" to E;  
    For every node  $y_j$  not in  $M_{\min}(T_1, T_2)$   
        Add "Insert( $T_{y_j}$ )" to E;  
    Return E };
```

Creating the upgrade set



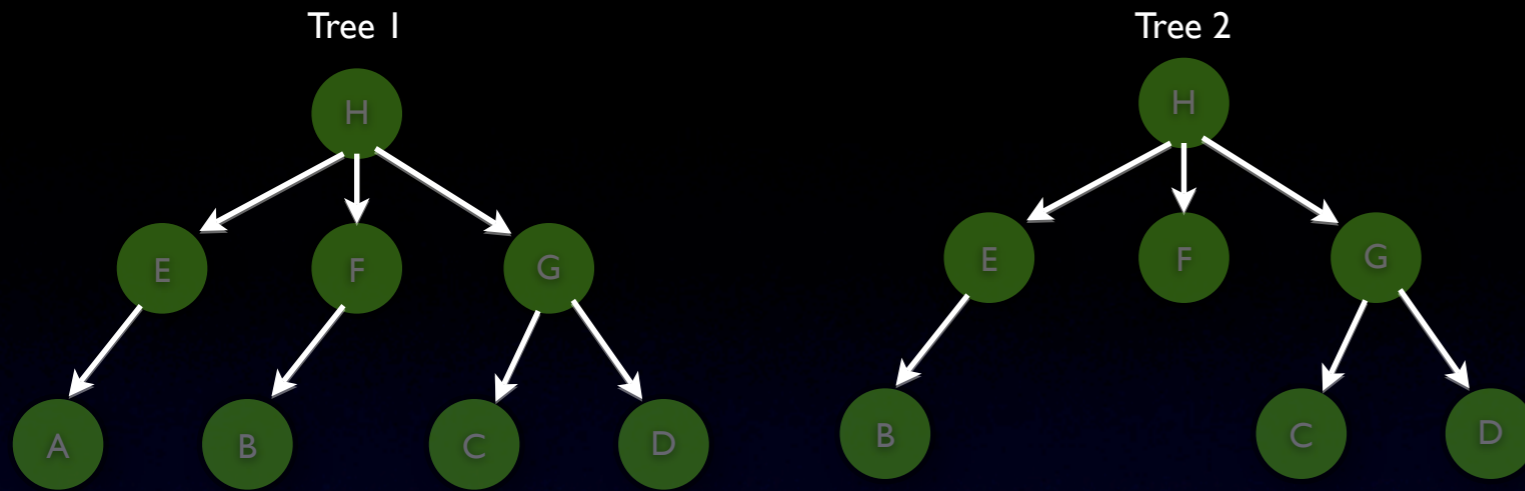
$\text{dist}(A,B) = 1$ $\text{dist}(E,E) = 0$ $\text{dist}(H,H) = 0$
 $\text{dist}(C,C) = 0$ $\text{dist}(F,F) = 0$
 $\text{dist}(D,D) = 0$ $\text{dist}(G,G) = 0$



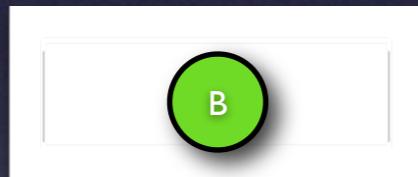
update(A,B)

```
Input: Tree  $T_1$  and  $T_2$ , a minimum-cost matching  $M_{\min}(T_1, T_2)$ , the distance table DT.  
Output: an edit script E.  
Initialize: set E = Null;  
 $x = \text{Root}(T_1)$ ,  $y = \text{Root}(T_2)$ .  
If  $(x, y) \notin M_{\min}(T_1, T_2)$  /* Subtree deletion and insertion */  
    Return "Delete( $T_1$ ), Insert( $T_2$ )".  
Else if  $\text{Dist}(T_1, T_2) = 0$   
    Return "";  
Else {  
    For every node pair  $(x_i, y_j) \in M_{\min}(T_1, T_2)$ ,  $x_i$  is a child node of  $x$ ,  $y_j$  is a child node of  $y$ .  
        If  $x_i$  and  $y_j$  are leaf nodes  
            If  $\text{Dist}(x_i, y_j) = 0$   
                Return "";  
            Else /* Update leaf node */  
                Add Update( $x_i$ , Value( $y_j$ )) to E;  
        Else /* Call subtree matching */  
            Add EditScript( $T_{x_i}$ ,  $T_{y_j}$ ) to E;  
    Return E;  
    For every node  $x_i$  not in  $M_{\min}(T_1, T_2)$   
        Add "Delete( $T_{x_i}$ )" to E;  
    For every node  $y_j$  not in  $M_{\min}(T_1, T_2)$   
        Add "Insert( $T_{y_j}$ )" to E;  
    Return E };
```

Creating the upgrade set



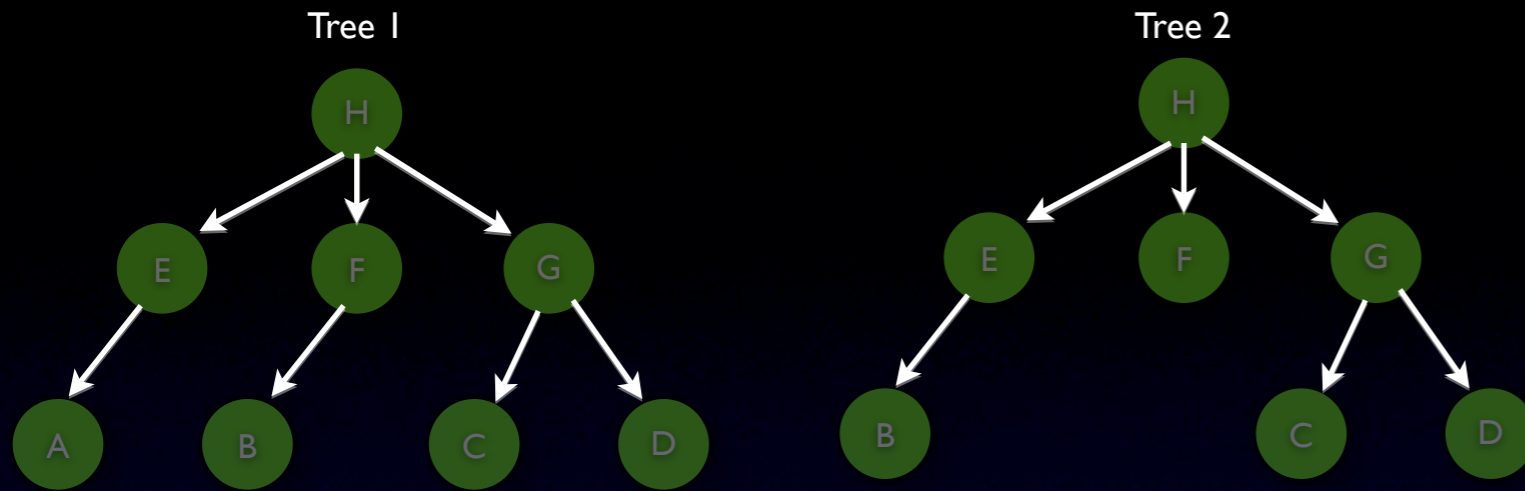
dist(A,B) = 1 dist(E,E) = 0 dist(H,H) = 0
dist(C,C) = 0 dist(F,F) = 0
dist(D,D) = 0 dist(G,G) = 0



update(A,B)
delete(B)

```
Input: Tree T1 and T2, a minimum-cost matching Mmin(T1, T2), the distance table DT.  
Output: an edit script E.  
Initialize: set E = Null;  
x = Root(T1), y = Root(T2).  
If (x, y) ∉ Mmin(T1, T2) /* Subtree deletion and insertion */  
    Return "Delete(T1), Insert(T2)".  
Else if Dist(T1, T2) = 0  
    Return "";  
Else {  
    For every node pair (xi, yj) ∈ Mmin(T1, T2), xi is a child  
    node of x, yj is a child node of y.  
        If xi and yj are leaf nodes  
            If Dist(xi, yj) = 0  
                Return "";  
            Else /* Update leaf node */  
                Add Update(xi, Value(yj)) to E;  
        Else /* Call subtree matching */  
            Add EditScript(Txi, Tyj) to E;  
    Return E;  
    For every node xi not in Mmin(T1, T2)  
        Add "Delete(Txi)" to E;  
    For every node yj not in Mmin(T1, T2)  
        Add "Insert(Tyj)" to E;  
    Return E };
```

Creating the upgrade set



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dist(C,C) = 0 dist(F,F) = 0
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        Else /* Call subtree matching */
            Add EditScript(Txi, Tyj) to E;
    Return E;
    For every node xi not in Mmin(T1, T2)
        Add "Delete(Txi)" to E;
    For every node yj not in Mmin(T1, T2)
        Add "Insert(Tyj)" to E;
    Return E; }
```



X-Diff Conclusion



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- Since we can represent a model in XML we have with this algorithm a better way to compute differences



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- However, in some cases additional model data has to be stored in the XML file
- We are in most of the cases not interested in all changes of the XML file, only the direct relevant ones from our model
- The plain XML diff is not sufficient for that



Project Idea

A Metamodel Independent Approach to Difference
Representation



A. Cicchetti, D.D. Ruscio and A. Pierantonio

“A Metamodel Independent Approach to Difference Representation”

University of Aquila, Italy (2007)

- In my project I would like to use the X-Diff algorithm in order to detect differences in models
- In order to refine the results I would like to propose a rule system which helps me specifying which differences are semantically relevant
- As a representation of this difference model I could use the information from the paper



Questions?

J. W. Hunt and M. D. McIlroy,

“An algorithm for differential file comparison”

Bell Telephone Laboratories CSTR #41 (1976)



Questions?

A. Cicchetti, D.D. Ruscio and A. Pierantonio

“A Metamodel Independent Approach to Difference Representation”

University of Aquila, Italy (2007)

