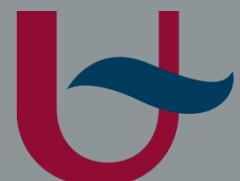


# Classic DEVS

An Introduction Using PythonPDEVS

Yentl Van Tendeloo, Hans Vangheluwe

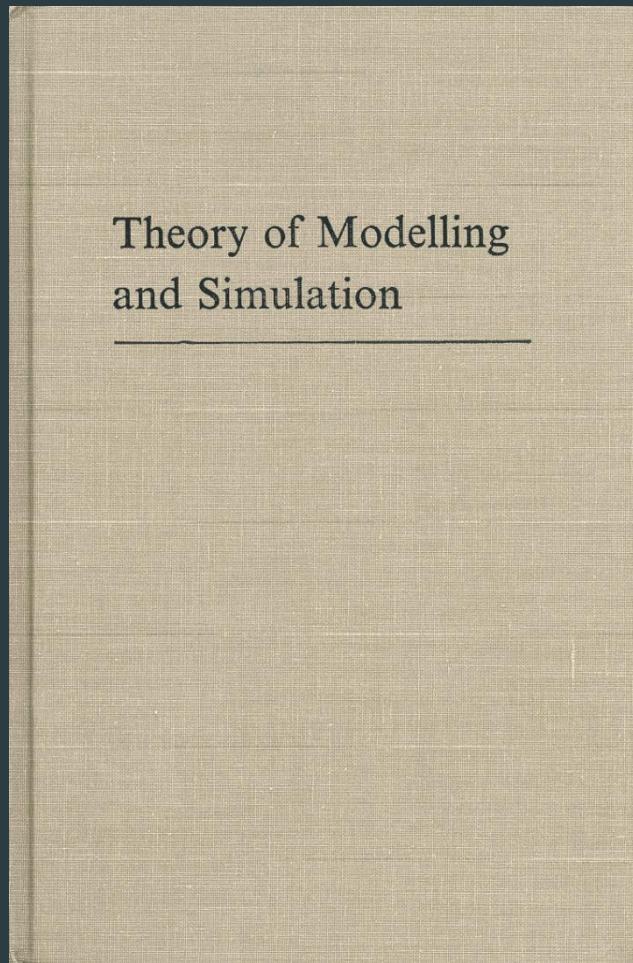


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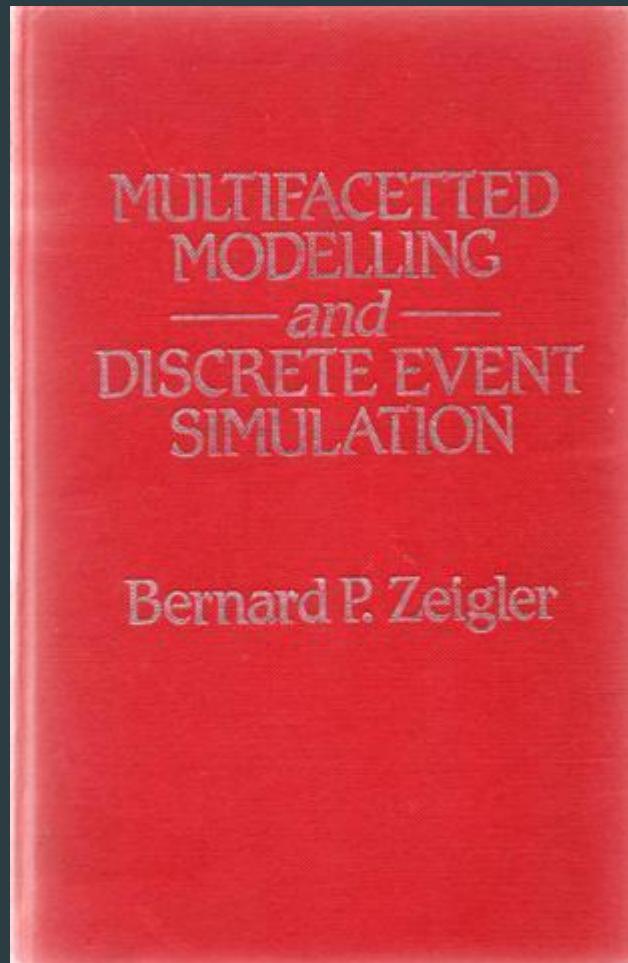


McGill

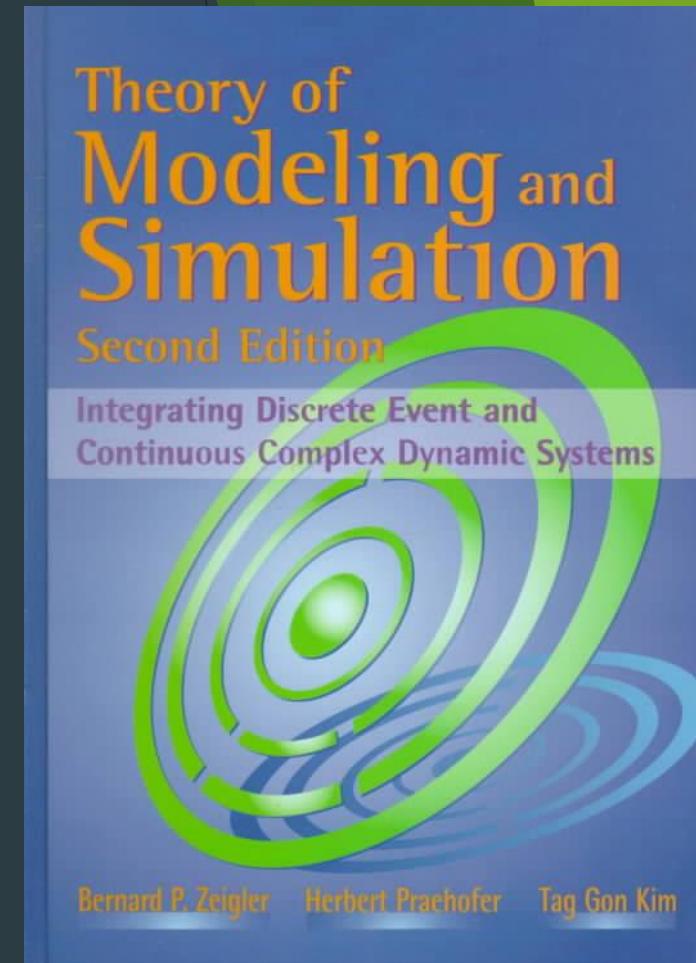
# Introduction



Bernard P. Zeigler.  
*Theory Of Modelling And Simulation.*  
1st ed. Wiley, 1976.



Bernard P. Zeigler.  
*Multifaceted Modelling and  
Discrete Event Simulation.*  
1st ed. Academic Press, 1984.



Bernard P. Zeigler, Herbert Praehofer,  
and Tag Gon Kim.  
*Theory Of Modelling And Simulation.*  
2nd ed. Academic Press, 2000.

## An overview of PythonPDEVS

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<sup>2</sup> McGill University, Canada

Hans Vangheluwe<sup>1,2</sup>

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[Hans.Vangheluwe@uantwerpen.be](mailto:Hans.Vangheluwe@uantwerpen.be)

Yentl Van Tendeloo and Hans Vangheluwe.  
*An Overview of PythonPDEVS.*  
In Proceedings of Journées DEVS  
Francophones (JDF), pages 59-66, 2016.

### Methodology

## An evaluation of DEVS simulation tools

Yentl Van Tendeloo<sup>1,\*</sup> and Hans Vangheluwe<sup>1,2,3\*</sup>

### Abstract

DEVS is a popular formalism for modeling complex dynamic systems using a discrete-event abstraction. Owing to its popularity, and the simplicity of the simulation kernel, a number of tools have been constructed by academia and industry. However, each of these tools has distinct design goals and a specific programming language implementation. Consequently, each supports a specific set of formalisms, combined with a specific set of features. Performance differs significantly between different tools. We provide an overview of the current state of eight different DEVS simulation tools: ADEVS, CD++, DEVS-Suite, MS4 Me, PowerDEVS, PythonPDEVS, VLE, and X-S-Y. We compare supported formalisms, compliance, features, and performance. This paper aims to help modelers in deciding which tools to use to solve their specific problems. It further aims to help tool builders, by showing the aspects of their tools that could be extended in future tool versions.



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1–19

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SAGE



Yentl Van Tendeloo and Hans Vangheluwe.  
*An Evaluation of DEVS Simulation Tools.*  
Simulation: Transactions of the Society  
for Modeling and Simulation International.  
2017, 93(2): 103-121



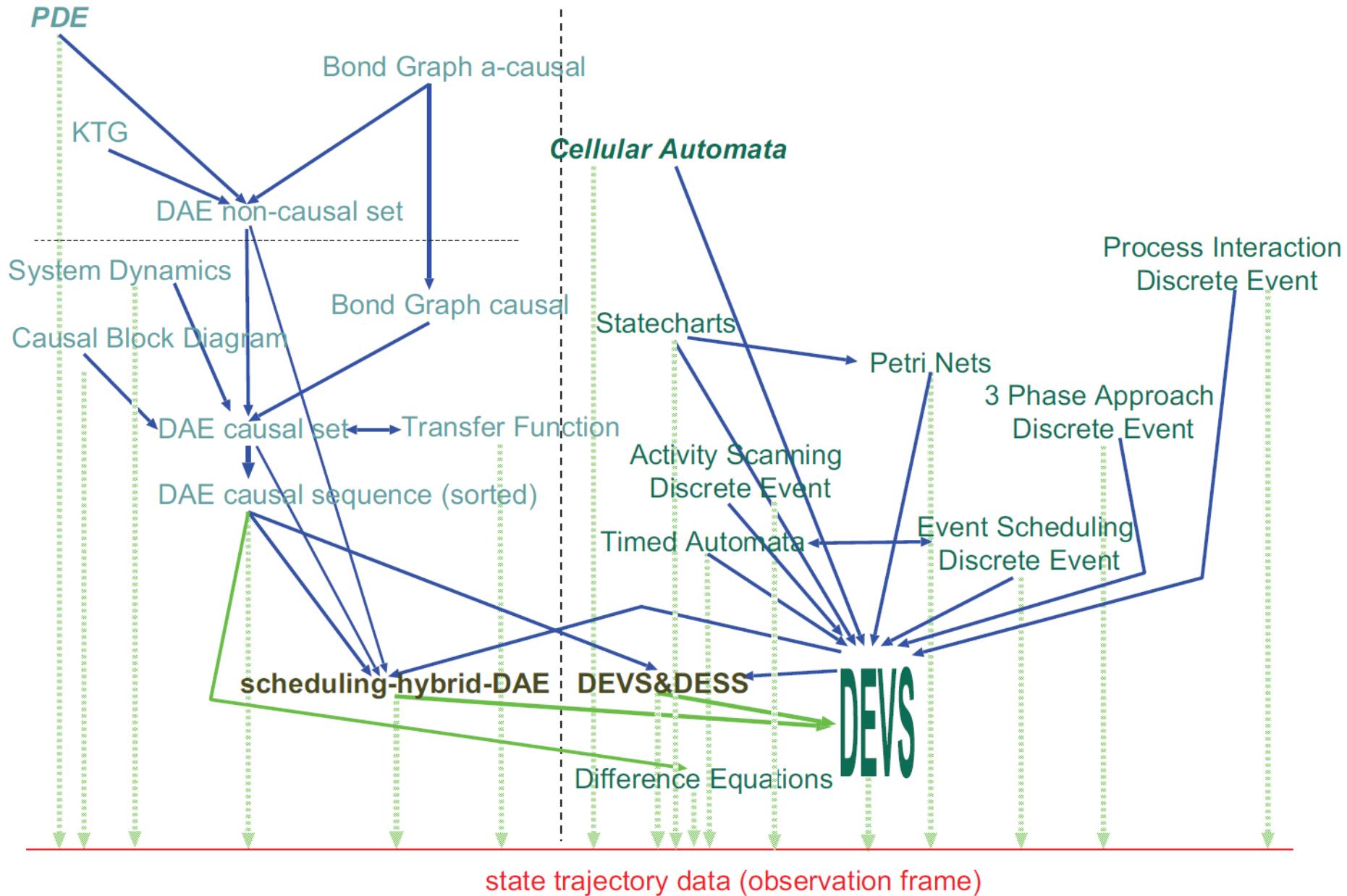
Our presentation uses initialized DEVS models, which contain an initial state. The initial state was left implicit in the original DEVS specification.

Sequential Discrete Event Language

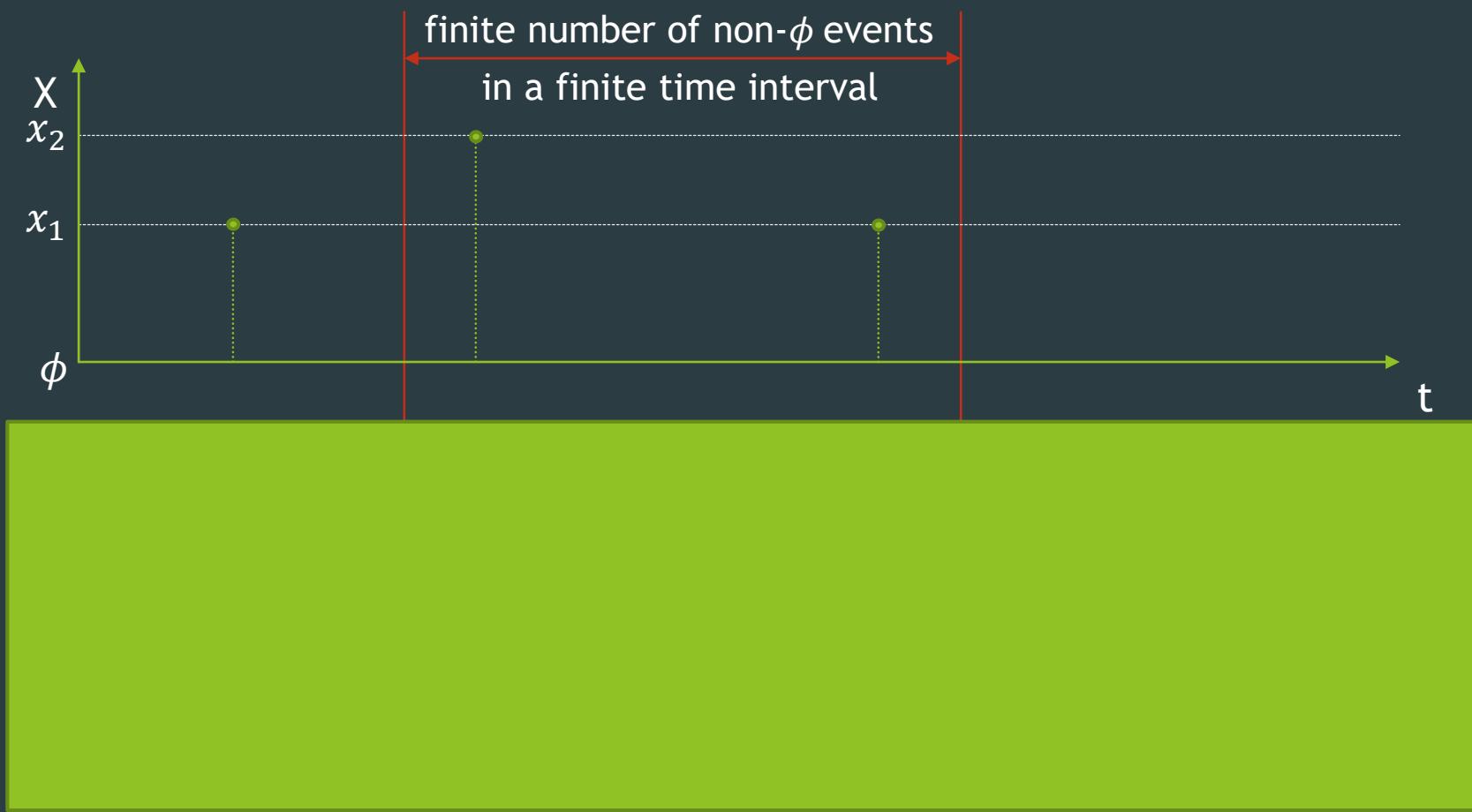


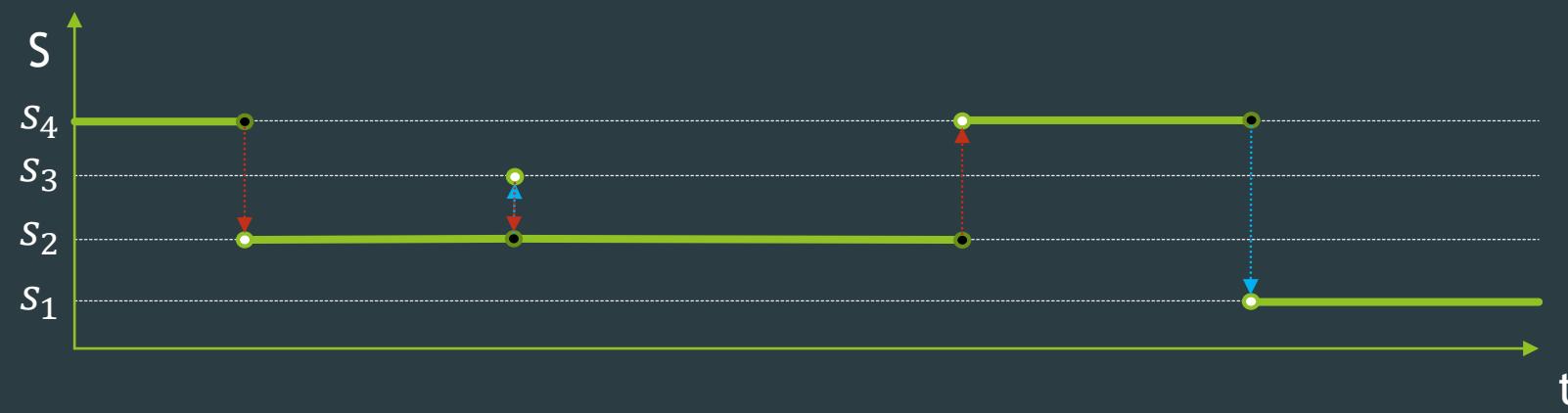
DEVS

= modular simulation assembly language



Vangheluwe, Hans. DEVS as a common denominator for multi-formalism hybrid systems modelling.  
 In proceedings of the International Symposium on Computer-Aided Control System Design, pp. 129-134. 2000.

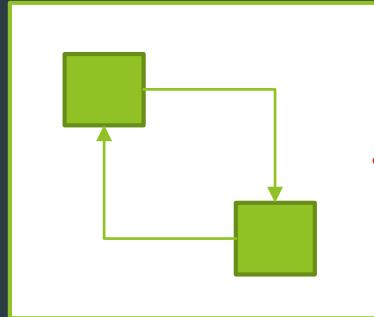




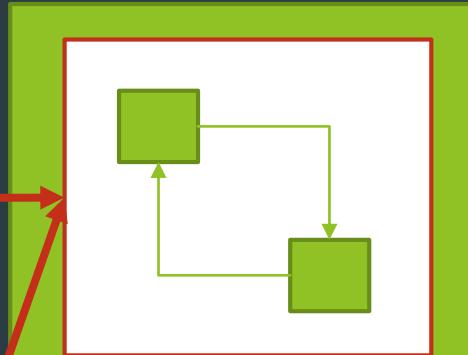


# Experimentation

# Simulation



Model

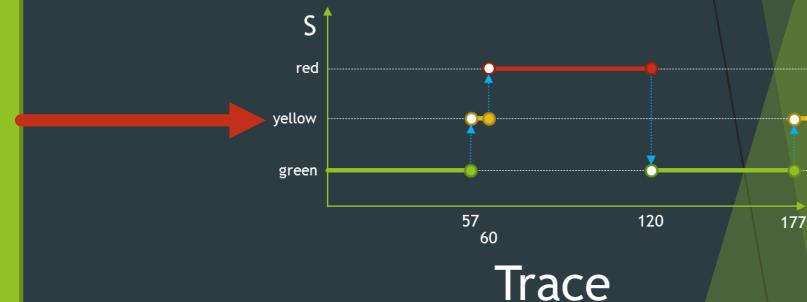


Model

$delay_{red} = 60s$   
 $delay_{yellow} = 3s$   
 $delay_{green} = 57s$   
 $q_{init,light1} = (green, 0)$   
 $q_{init,pol1} = (idle, 280)$   
 $cond_{termination} = (t_{sim} \geq t_{end})$   
 $t_{end} = 24h$



Solver



## Concrete Syntax



### simple\_experiment.py

```
from pypdevs.simulator import Simulator

from mymodel import MyModel

model = MyModel(\n    q_init_pol1 = ("idle", 280),\n    q_init_light1 = ("green", 0),\n    delay_red = 60,\n    delay_yellow = 3,\n    delay_green = 57\n)
simulator = Simulator(model)

simulator.setTerminationTime(24*60*60)
simulator.setClassicDEVS()
simulator.setVerbose()

simulator.simulate()
```

— Current Time: 0.00 —

INITIAL CONDITIONS in model <system.light>

Initial State: green

Next scheduled internal transition at time 57.00

INITIAL CONDITIONS in model <system.policeman>

Initial State: idle

Next scheduled internal transition at time 20.00

\_ Current Time: 20.00 \_\_\_\_\_

EXTERNAL TRANSITION in model <system.light>

Input Port Configuration:

port <interrupt>:  
toManual

New State: going\_manual

Next scheduled internal transition at time 20.0

INTERNAL TRANSITION in model <system.policeman>

New State: working

Output Port Configuration:

port <output>:  
go\_to\_work

Next scheduled internal transition at time 3620.00

\_ Current Time: 20.00 \_\_\_\_\_

INTERNAL TRANSITION in model <system.light>

Output Port Configuration:

port <observer>:

turn\_off

New State: manual

Next scheduled internal transition at time inf

— Current Time: 3620.00 —

---

EXTERNAL TRANSITION in model <system.light>

Input Port Configuration:

port <interrupt>:

toAuto

New State: going\_auto

Next scheduled internal transition at time 3620.00

INTERNAL TRANSITION in model <system.policeman>

New State: idle

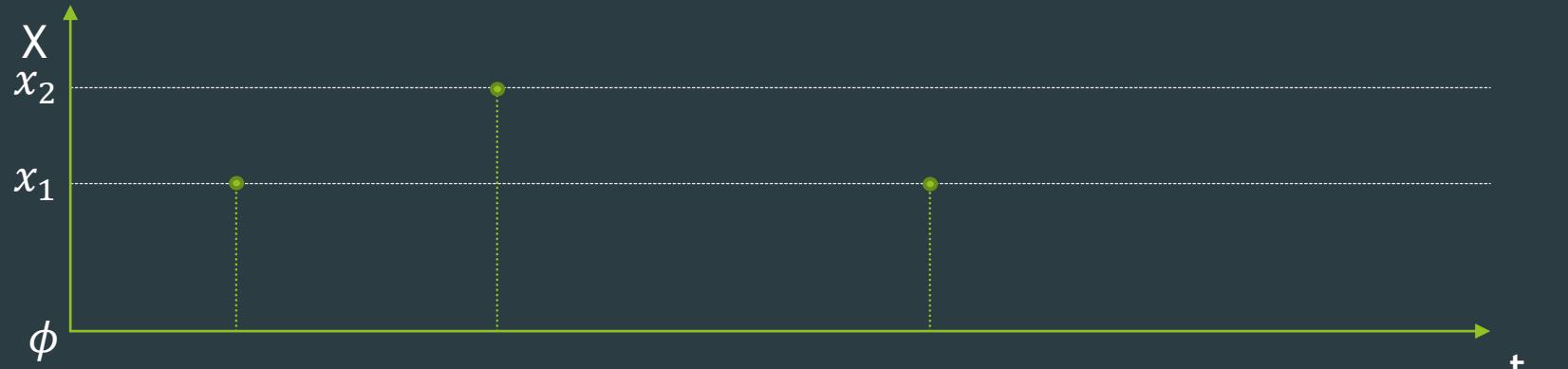
Output Port Configuration:

port <output>:

take\_break

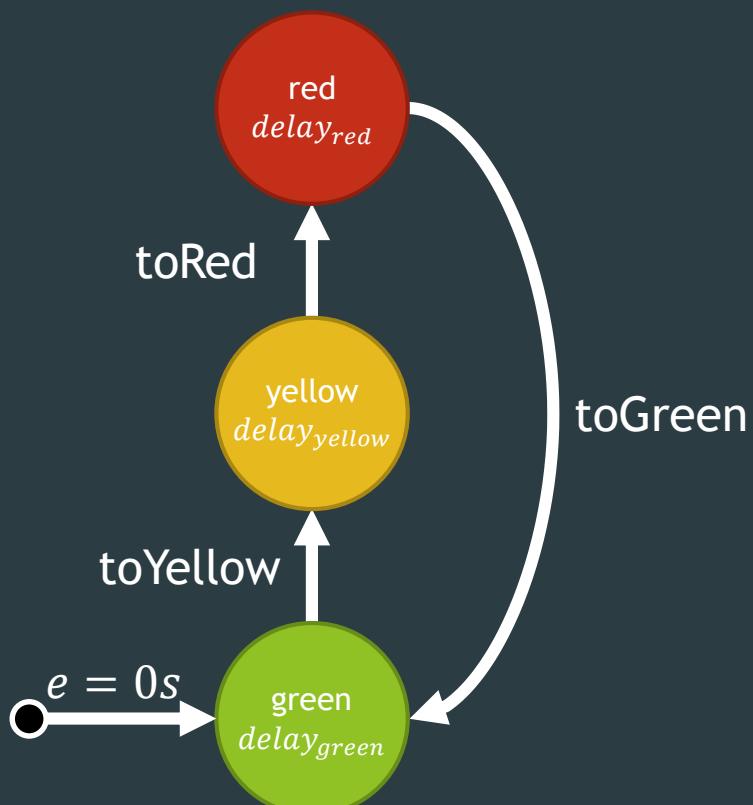
Next scheduled internal transition at time 3920.00

# Atomic Models

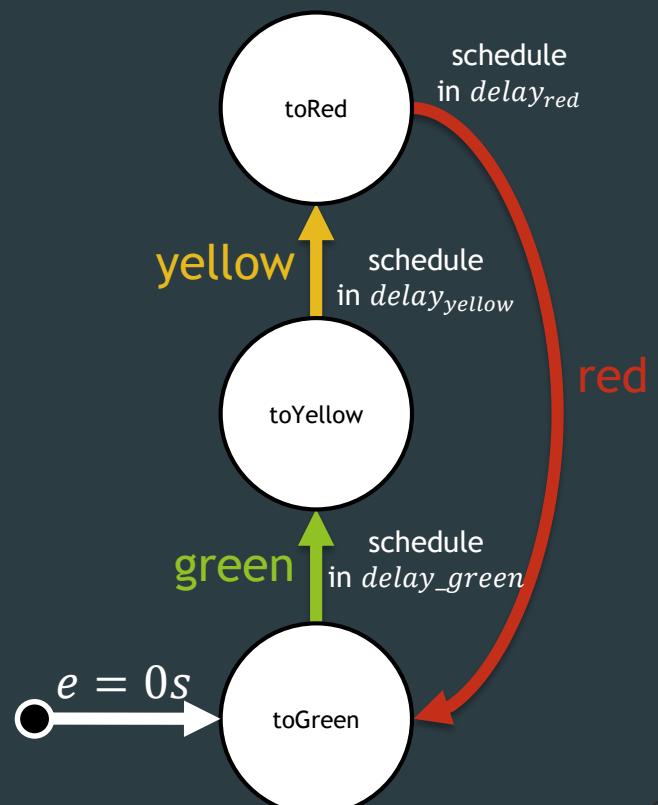


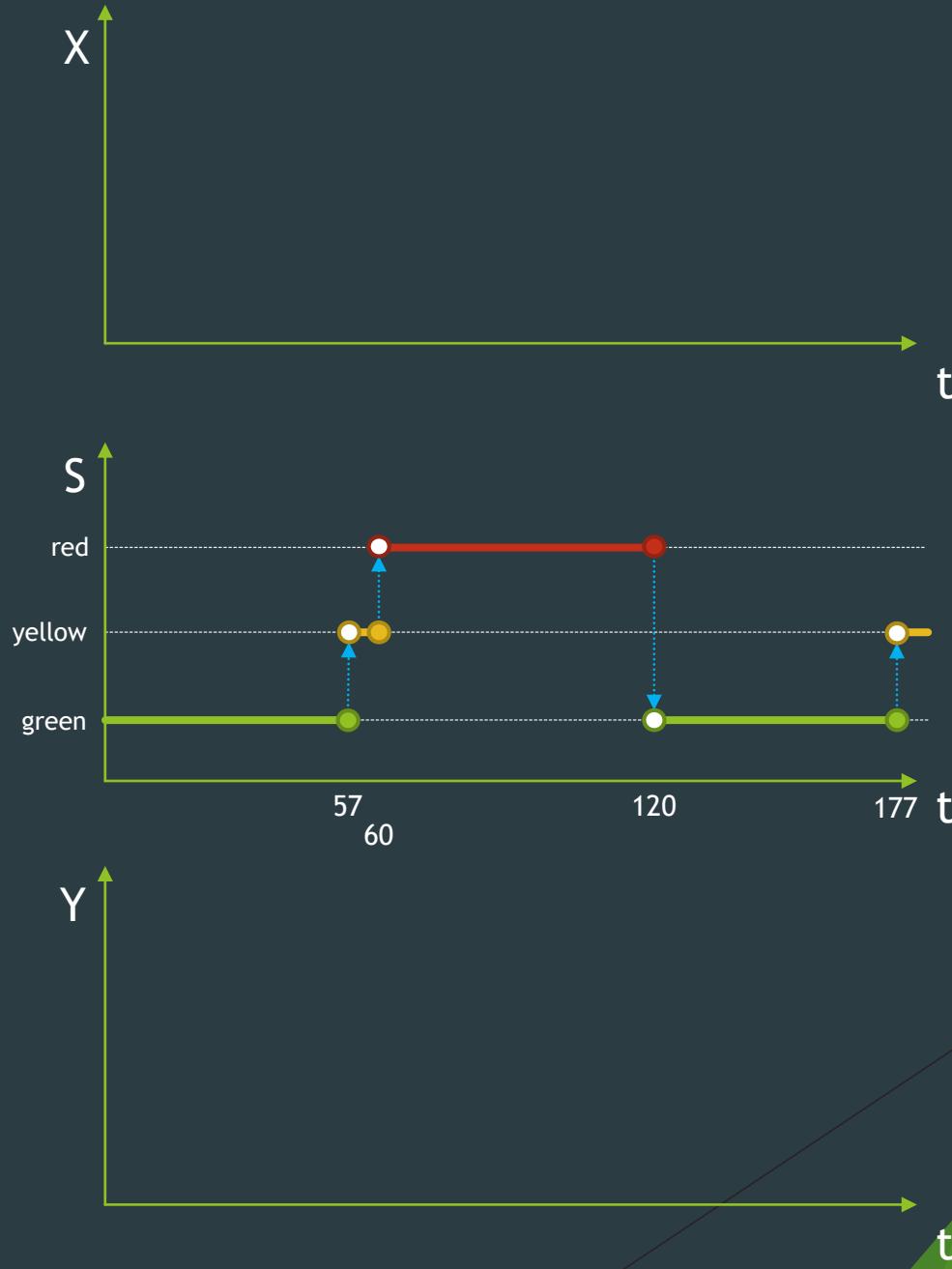
# Modelling Discrete Event Behaviour

Finite State Automaton



Timed Event Scheduling Graph







## Autonomous (no input)

$$M = \langle S, \quad , \delta_{int}, ta \rangle$$

$S$  : set of sequential states

$$S = \{\text{red, yellow, green}\}$$

$$\delta_{int} : S \rightarrow S$$

$$\delta_{int} = \{\text{red} \rightarrow \text{green}, \\ \text{green} \rightarrow \text{yellow}, \\ \text{yellow} \rightarrow \text{red}\}$$

$$ta : S \rightarrow \mathbb{R}_{0,+\infty}^+$$

$$ta = \{\text{red} \rightarrow delay_{red}, \\ \text{green} \rightarrow delay_{green}, \\ \text{yellow} \rightarrow delay_{yellow}\}$$

# Time Advance: corner cases

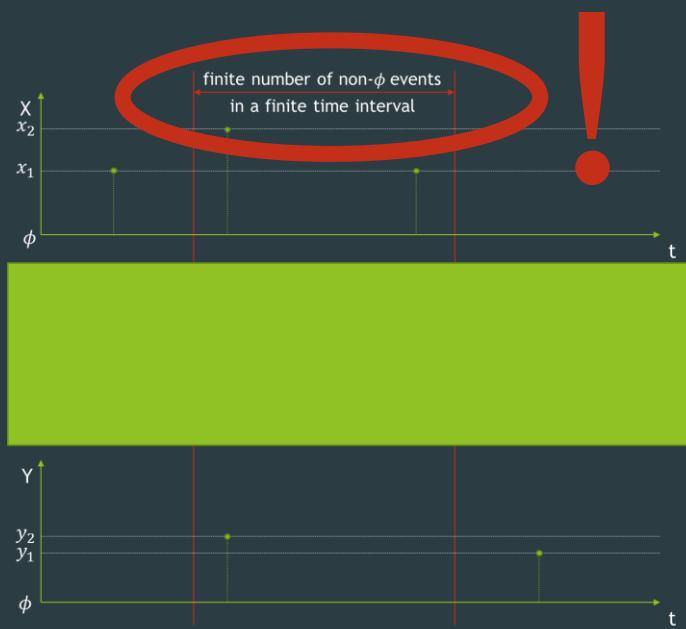
$$ta : S \rightarrow \mathbb{R}_{0,+\infty}^+$$

$$ta(s_i) = 0$$

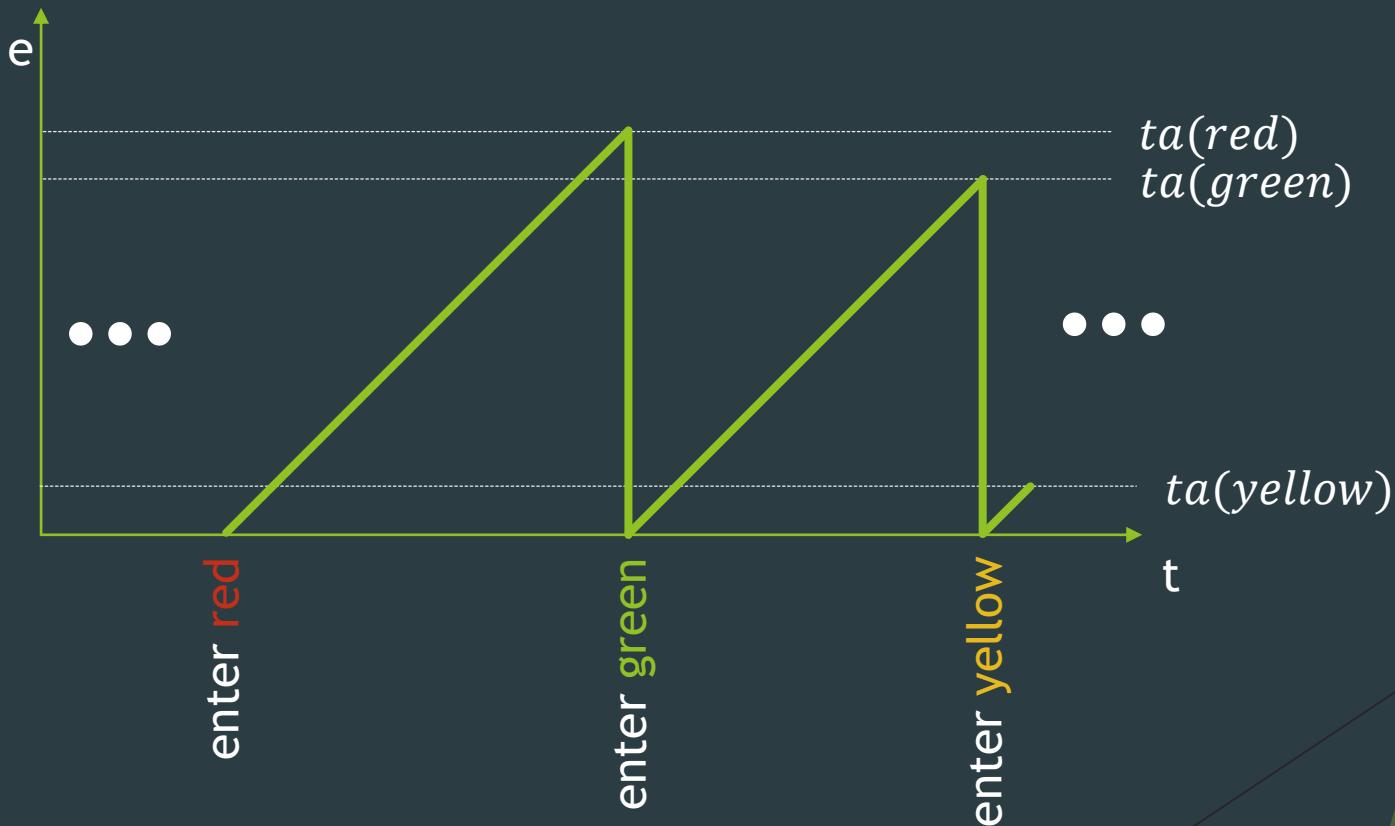
transient states

$$ta(s_i) = +\infty$$

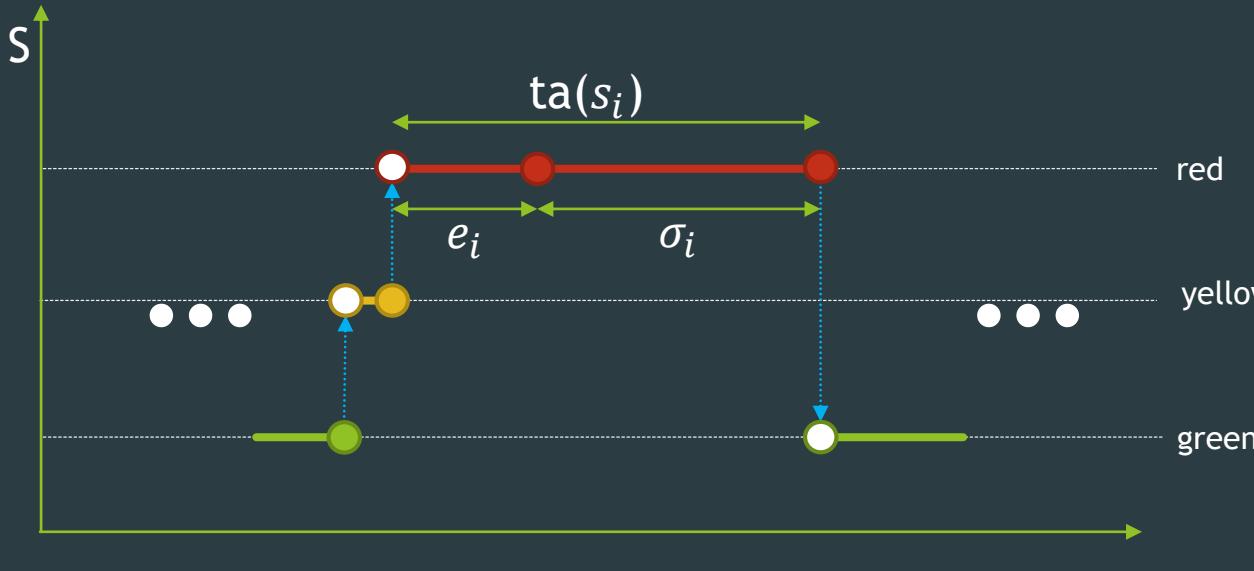
passive states



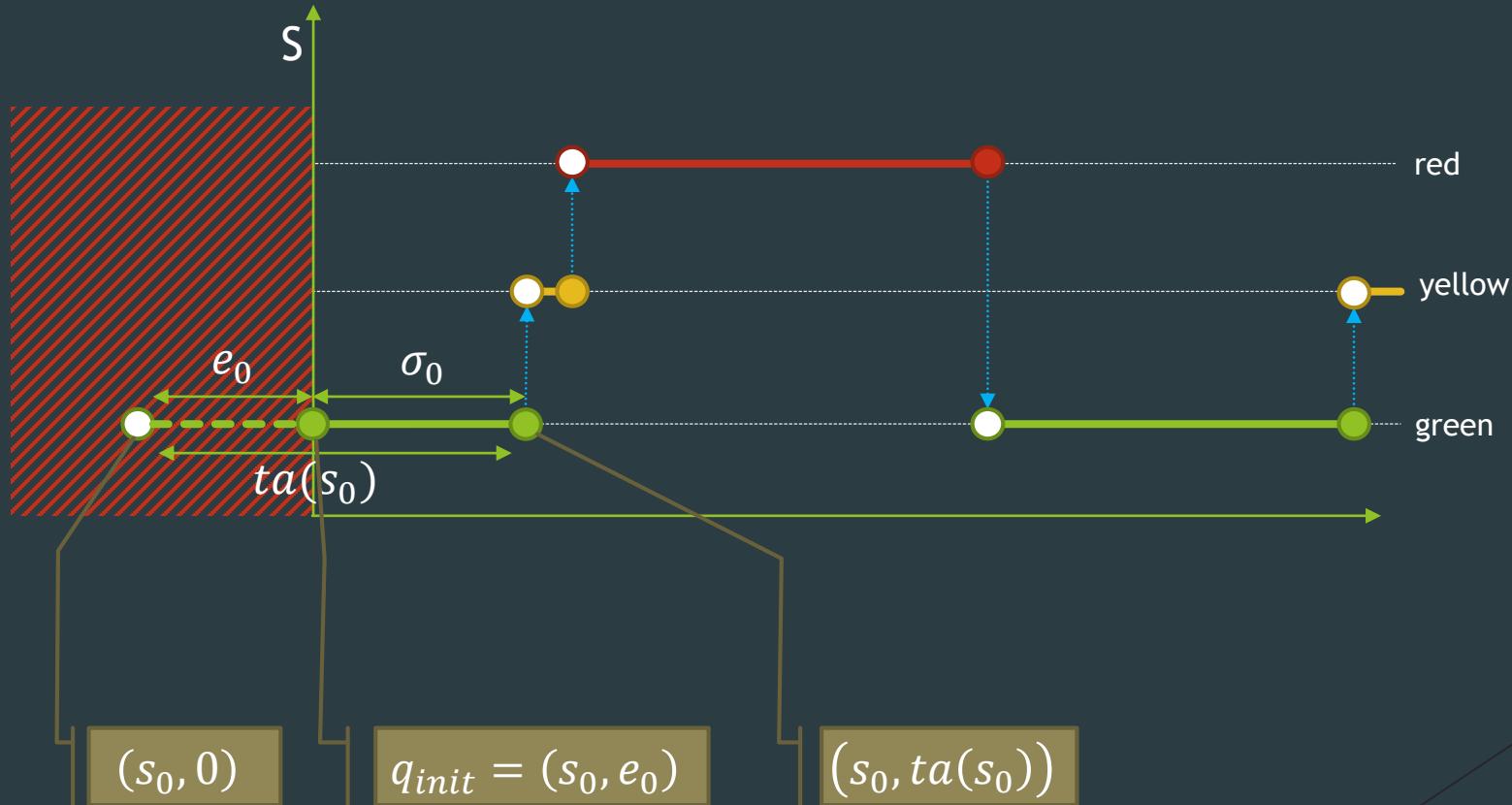
# Elapsed time



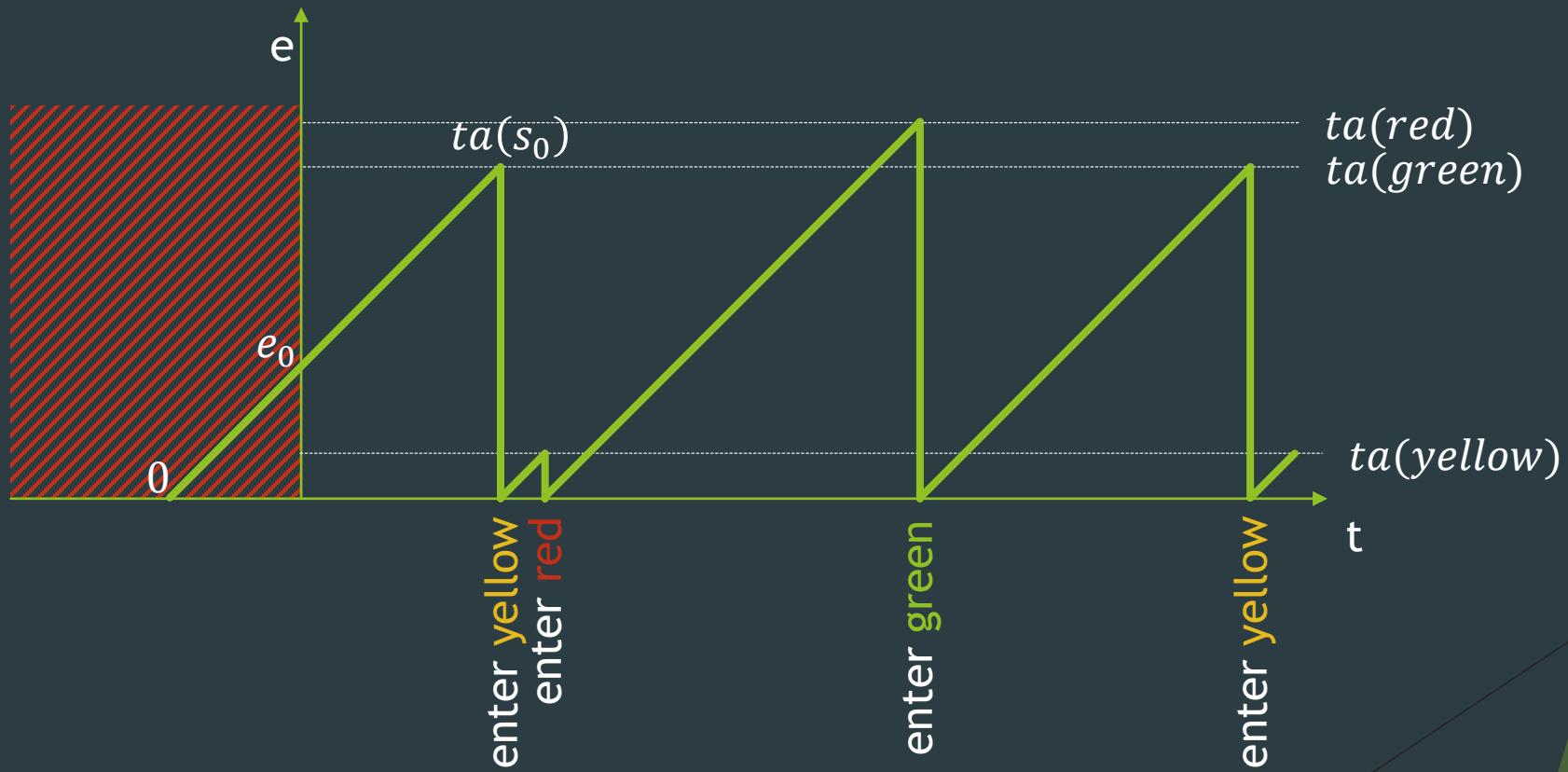
# Elapsed time

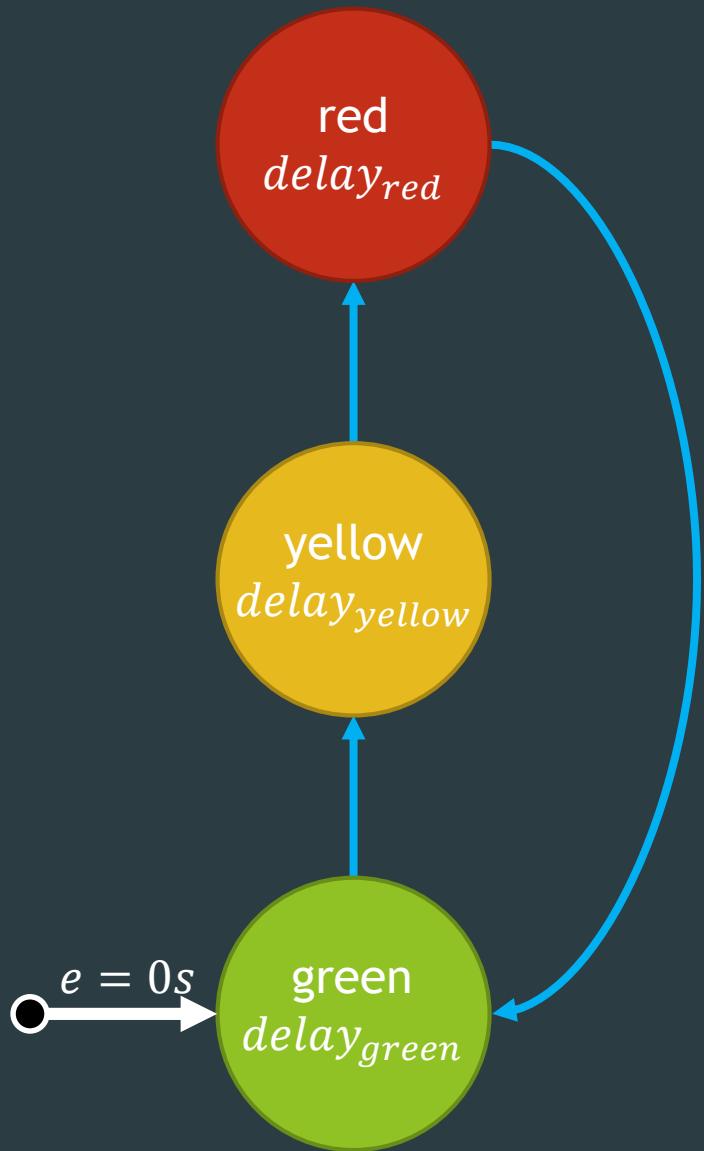


# Initialization of Initial State



# Elapsed time





## Autonomous (no output)

$$M = \langle S, q_{init}, \delta_{int}, ta \rangle$$

$S$  : set of sequential states

$$S = \{\text{red, yellow, green}\}$$

$$\delta_{int} : S \rightarrow S$$

$$\delta_{int} = \{\text{red} \rightarrow \text{green}, \\ \text{green} \rightarrow \text{yellow}, \\ \text{yellow} \rightarrow \text{red}\}$$

$$ta : S \rightarrow \mathbb{R}_{0,+\infty}^+$$

$$ta = \{\text{red} \rightarrow delay_{red}, \\ \text{green} \rightarrow delay_{green}, \\ \text{yellow} \rightarrow delay_{yellow}\}$$

$$q_{init} : Q - \text{set of total states}$$

$$Q = \{(s, e) | s \in S, 0 \leq e \leq ta(s)\}$$

$$q_{init} = (\text{green}, 0)$$

## Abstract Syntax

```
S = {red, yellow, green}  
 $\delta_{int}$  = { red → green,  
           green → yellow,  
           yellow → red}  
ta = {red → delayred,  
      green → delaygreen,  
      yellow → delayyellow}  
qinit = (green, 0)
```

## Operational Semantics

```
time = 0  
current_state = initial_state  
last_time = -initial_elapsed  
while not termination_condition():  
    time = last_time + ta(current_state)  
    current_state =  $\delta_{int}$ (current_state)  
    last_time = time
```

## Concrete Syntax



```
from pypdevs.DEVS import *  
  
class TrafficLightAutonomous(AtomicDEVS):  
    def __init__(self, q_init, delay_green,  
                 delay_yellow, delay_red):  
        AtomicDEVS.__init__(self, "light")  
        self.state, self.elapsed = q_init  
        self.delay_green = delay_green  
        self.delay_yellow = delay_yellow  
        self.delay_red = delay_red  
  
    def intTransition(self):  
        state = self.state  
        return {"red": "green",  
                "yellow": "red",  
                "green": "yellow"}[state]  
  
    def timeAdvance(self):  
        state = self.state  
        return {"red": self.delay_red,  
                "yellow": self.delay_yellow,  
                "green": self.delay_green}[state]
```

\_\_ Current Time: 0.00 \_\_\_\_\_

INITIAL CONDITIONS in model <light>

Initial State: green

Next scheduled internal transition at time 57.00

\_\_ Current Time: 57.00 \_\_\_\_\_

INTERNAL TRANSITION in model <light>

New State: yellow

Output Port Configuration:

Next scheduled internal transition at time 60.00

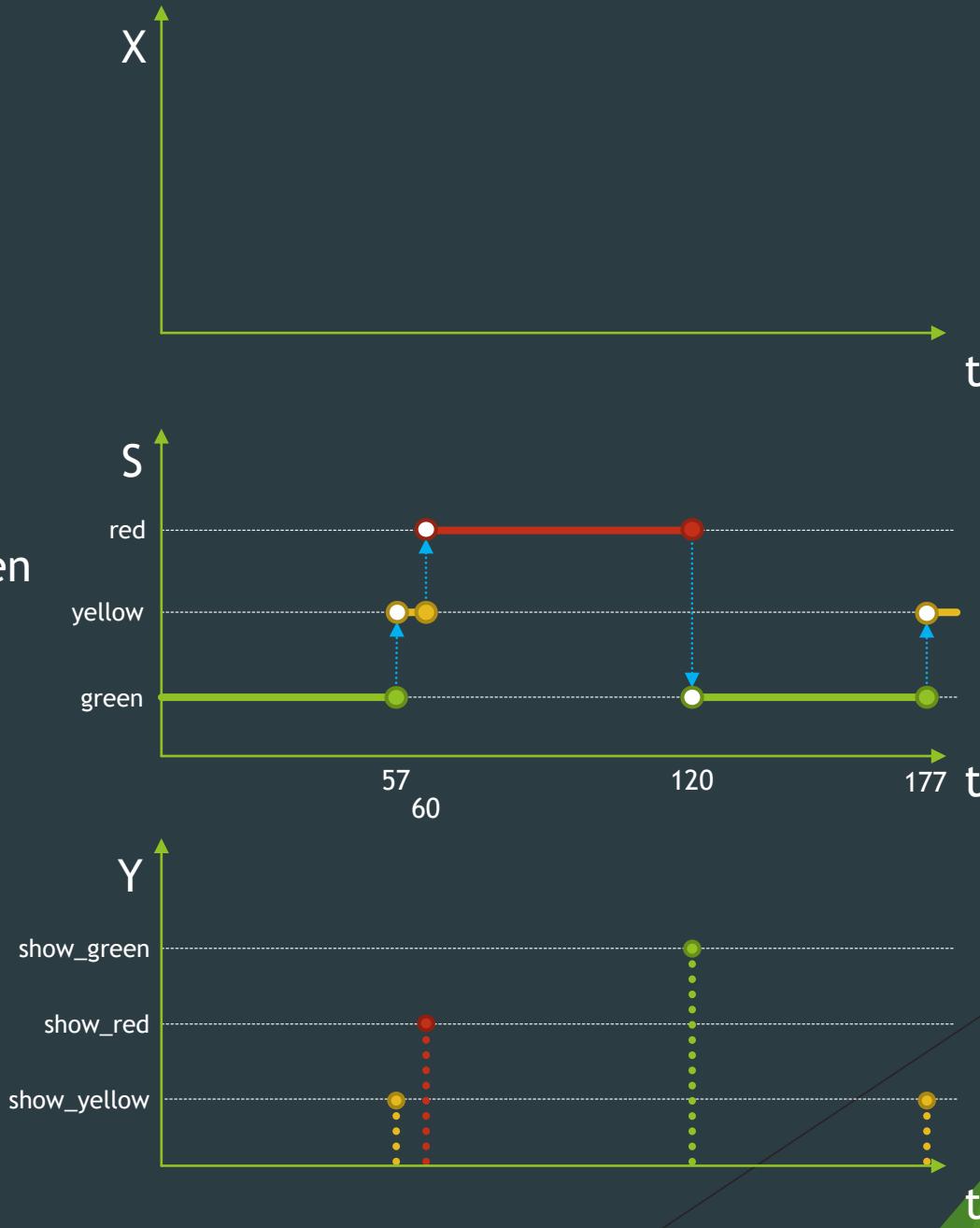
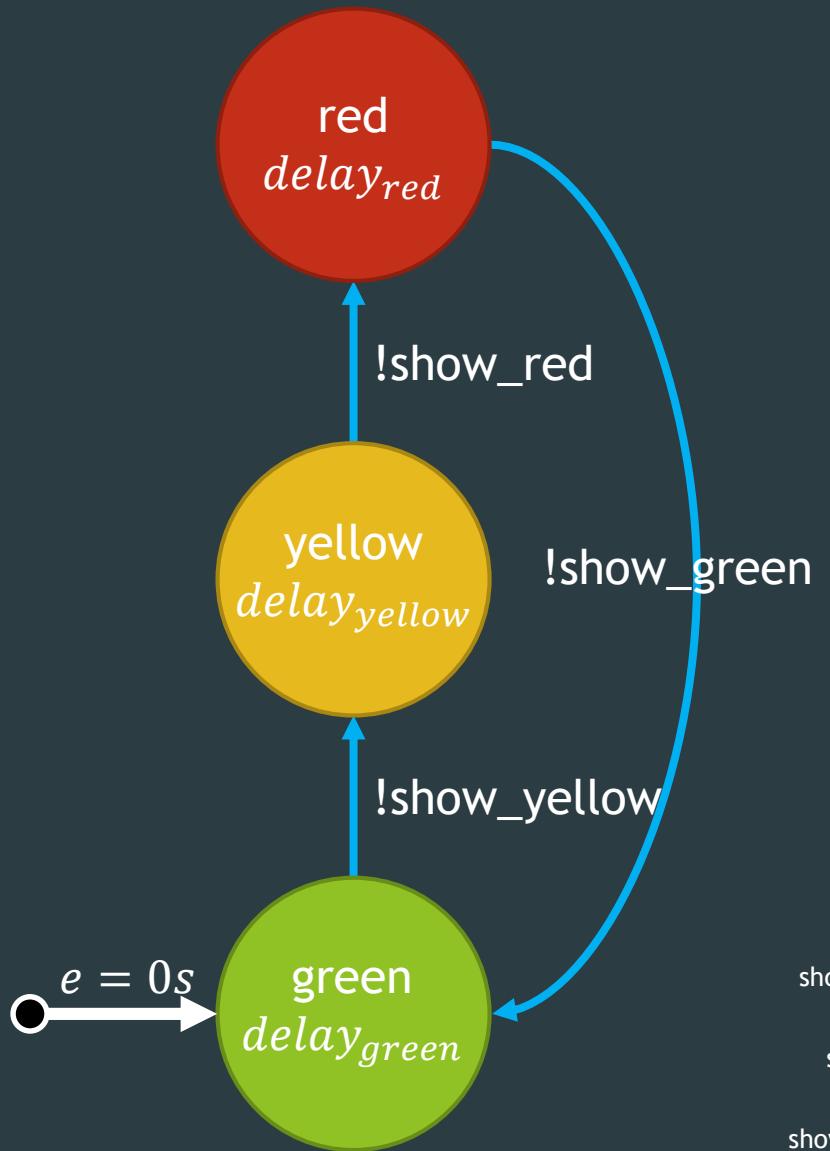
\_\_ Current Time: 60.00 \_\_\_\_\_

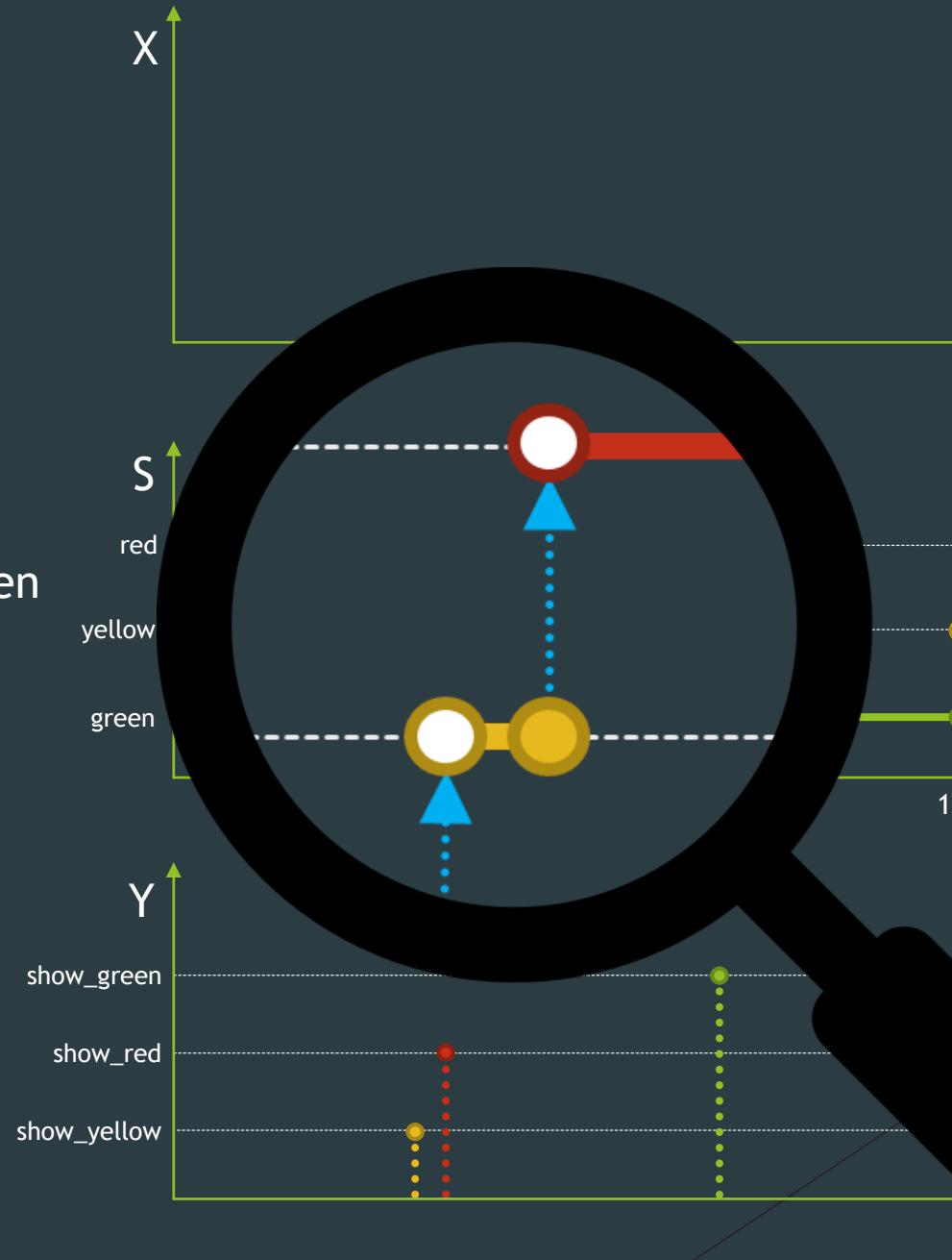
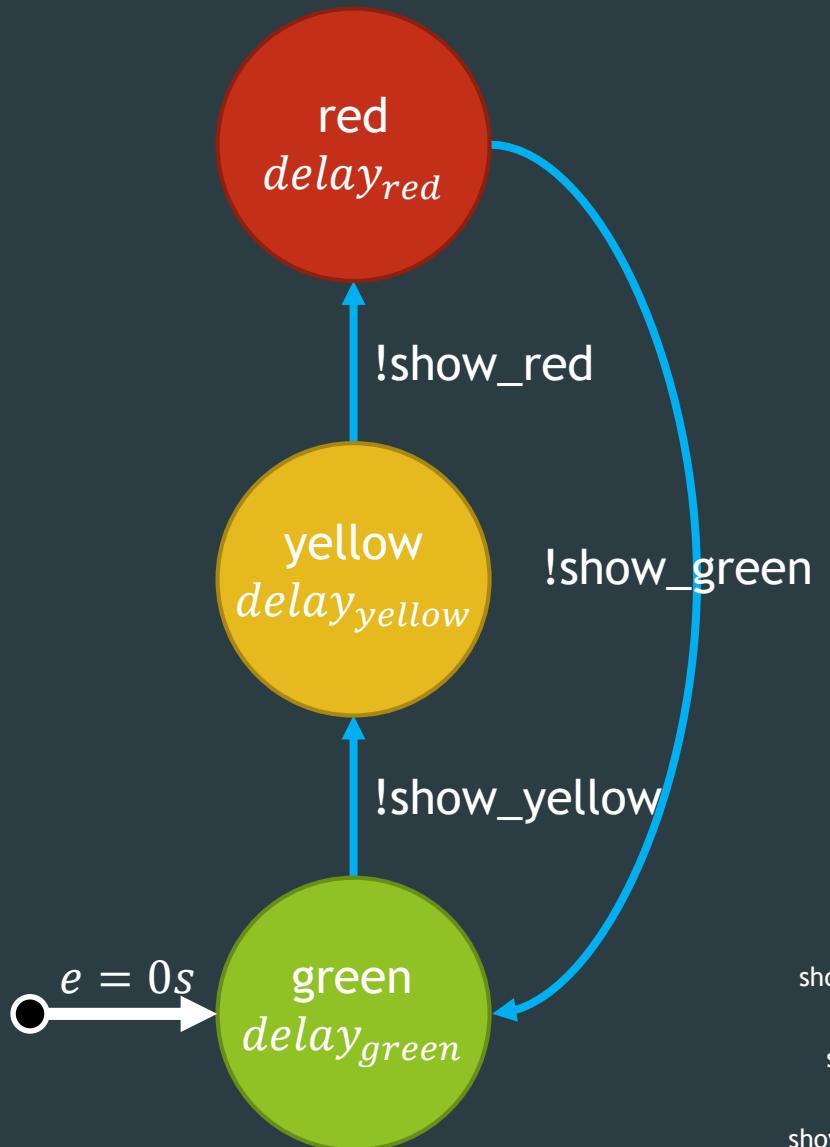
INTERNAL TRANSITION in model <light>

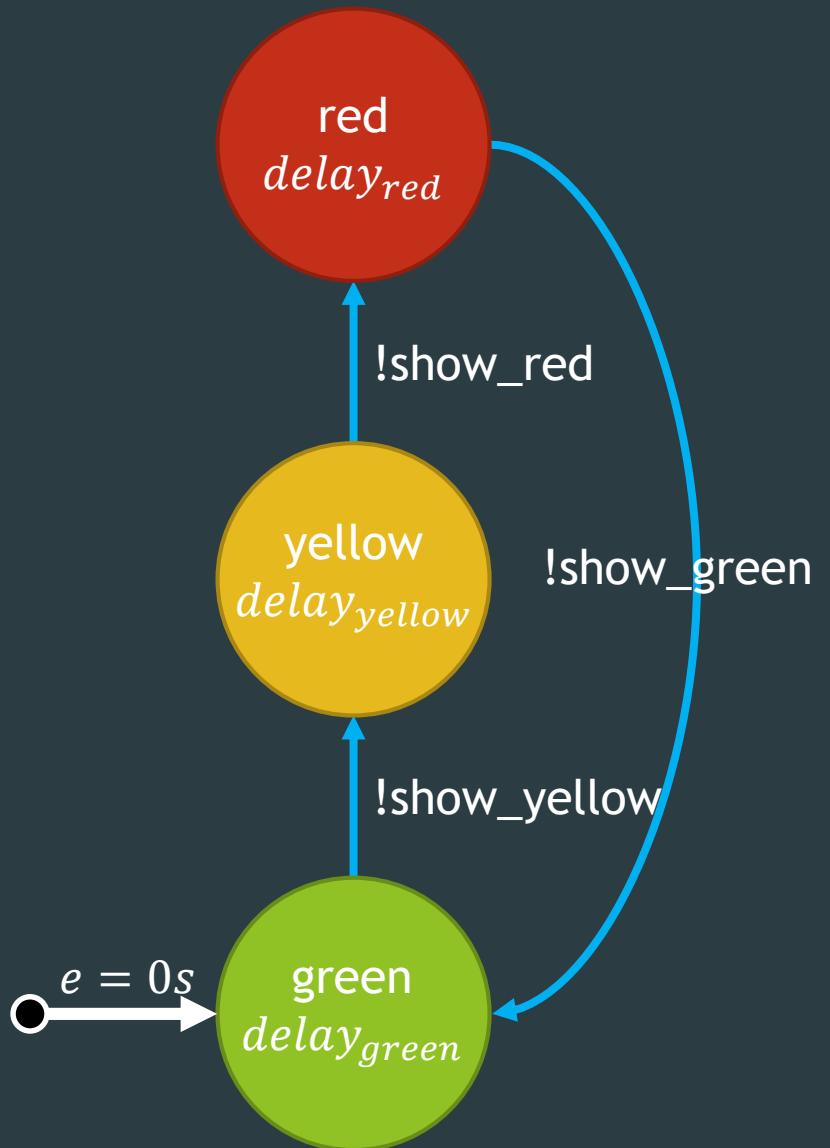
New State: red

Output Port Configuration:

Next scheduled internal transition at time 120.00







## Autonomous (with output)

$$M = \langle Y, S, q_{init}, \delta_{int}, \lambda, ta \rangle$$

$$S = \{ \text{red, yellow, green} \}$$

$$\delta_{int} = \{ \text{ red} \rightarrow \text{green}, \\ \text{green} \rightarrow \text{yellow}, \\ \text{yellow} \rightarrow \text{red} \}$$

$$q_{init} = (\text{green}, 0)$$

$$ta = \{ \text{red} \rightarrow delay_{red}, \\ \text{green} \rightarrow delay_{green}, \\ \text{yellow} \rightarrow delay_{yellow} \}$$

$Y$  : set of output events

$$Y = \{ \text{"show\_red"}, \text{"show\_green"}, \text{"show\_yellow"} \}$$

$$\lambda : S \rightarrow Y \cup \{\phi\}$$

$$\lambda = \{ \text{green} \rightarrow \text{"show\_yellow"}, \\ \text{yellow} \rightarrow \text{"show\_red"}, \\ \text{red} \rightarrow \text{"show\_green"} \}$$

## Abstract Syntax

```
S = {red, yellow, green}  
qinit = (green, 0)  
 $\delta_{int}$  = { red → green,  
           green → yellow,  
           yellow → red}  
ta = {red → delayred,  
      green → delaygreen,  
      yellow → delayyellow}  
Y = {"show_red",  
     "show_green",  
     "show_yellow"}  
 $\lambda$  = {green → "show_yellow",  
        yellow → "show_red",  
        red → "show_green"}
```

## Operational Semantics

```
time = 0  
current_state = initial_state  
last_time = -initial_elapsed  
while not termination_condition():  
    time = last_time + ta(current_state)  
    output( $\lambda$ (current_state))  
    current_state =  $\delta_{int}$ (current_state)  
    last_time = time
```

## Concrete Syntax



```
from pypdevs.DEVS import *  
  
class TrafficLightWithOutput(AtomicDEVS):  
    def __init__(self, ...):  
        AtomicDEVS.__init__(self, "light")  
        self.observe = self.addOutPort("observer")  
        ...  
        ...  
  
    def outputFnc(self):  
        state = self.state  
        if state == "red":  
            return {self.observe: "show_green"}  
        elif state == "yellow":  
            return {self.observe: "show_red"}  
        elif state == "green":  
            return {self.observe: "show_yellow"}
```

\_\_ Current Time: 0.00 \_\_\_\_\_

INITIAL CONDITIONS in model <light>

Initial State: green

Next scheduled internal transition at time 57.00

\_\_ Current Time: 57.00 \_\_\_\_\_

INTERNAL TRANSITION in model <light>

New State: yellow

Output Port Configuration:

port <observer>:

show\_yellow

Next scheduled internal transition at time 60.00

\_\_ Current Time: 60.00 \_\_\_\_\_

INTERNAL TRANSITION in model <light>

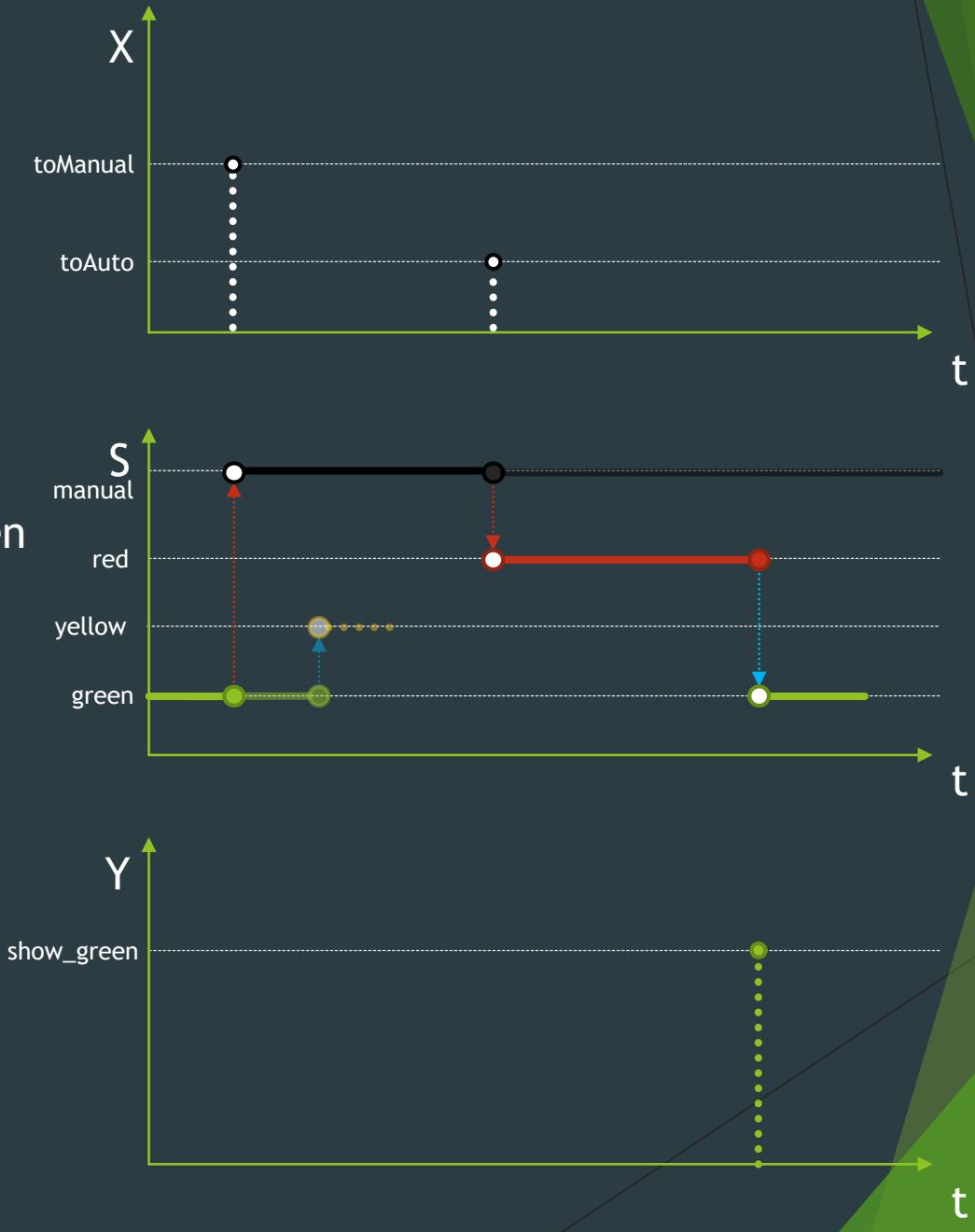
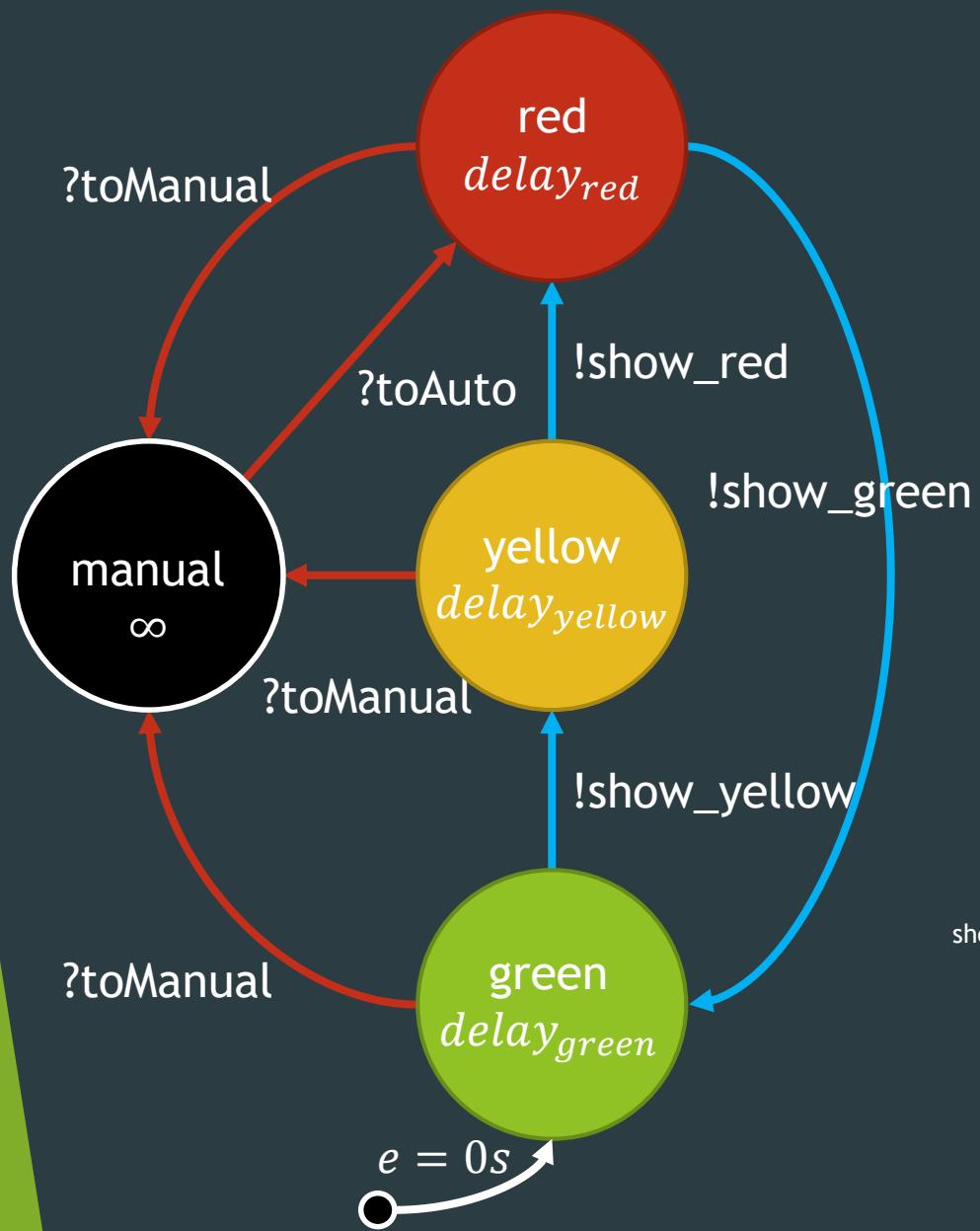
New State: red

Output Port Configuration:

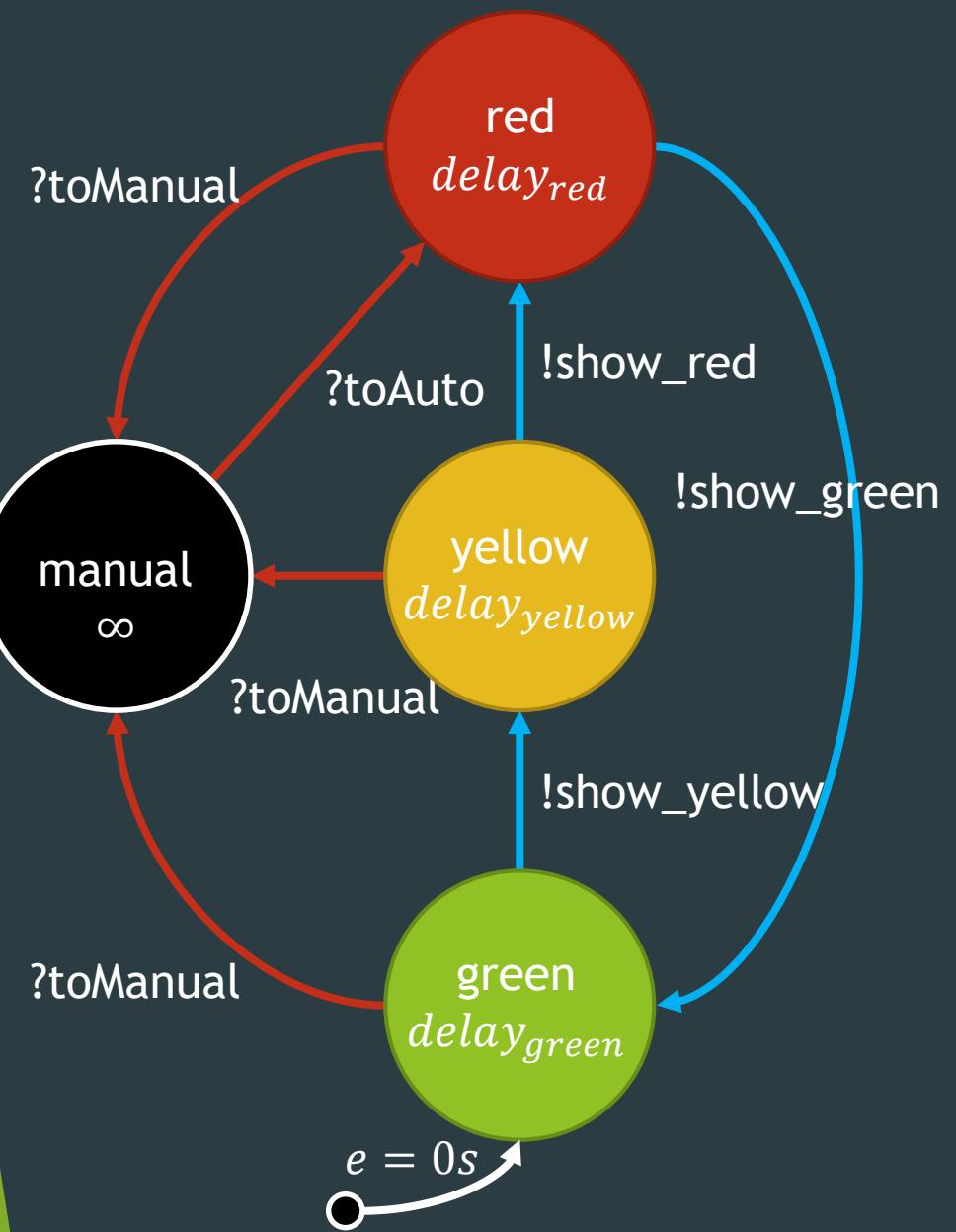
port <observer>:

show\_red

Next scheduled internal transition at time 120.00



# Reactive



$$M = \langle X, Y, S, q_{init}, \delta_{int}, \delta_{ext}, \lambda, ta \rangle$$

$Y = \{\text{"show\_red"}, \text{"show\_green"}, \text{"show\_yellow"}\}$

$S = \{\text{red}, \text{yellow}, \text{green}, \text{manual}\}$

$q_{init} = (\text{green}, 0)$

$\delta_{int} = \{\text{red} \rightarrow \text{green},$   
 $\text{green} \rightarrow \text{yellow},$   
 $\text{yellow} \rightarrow \text{red}\}$

$\lambda = \{\text{green} \rightarrow \text{"show\_yellow"},$   
 $\text{yellow} \rightarrow \text{"show\_red"},$   
 $\text{red} \rightarrow \text{"show\_green"}\}$

$ta = \{\text{red} \rightarrow \text{delay}_{red},$   
 $\text{green} \rightarrow \text{delay}_{green},$   
 $\text{yellow} \rightarrow \text{delay}_{yellow},$   
 $\text{manual} \rightarrow +\infty\}$

$X : \text{set of input events}$

$X = \{\text{"toAuto"}, \text{"toManual"}\}$

$\delta_{ext} : Q \times X \rightarrow S$

$Q = \{(s, e) | s \in S, 0 \leq e \leq ta(s)\}$

$\delta_{ext} = \{(\text{(*, *}), \text{"toManual"}) \rightarrow \text{"manual"},$   
 $(\text{("manual", *)}, \text{"toAuto"}) \rightarrow \text{"red"}\}$

## Abstract Syntax

```
Y = {"show_red", "show_green", "show_yellow"}  
S = {red, yellow, green, manual}  
 $q_{init} = (\text{green}, 0)$   
 $\delta_{int} = \{\text{red} \rightarrow \text{green},$   
           $\text{green} \rightarrow \text{yellow},$   
           $\text{yellow} \rightarrow \text{red}\}$   
 $\lambda = \{\text{green} \rightarrow \text{"show_yellow"},$   
         $\text{yellow} \rightarrow \text{"show_red"},$   
         $\text{red} \rightarrow \text{"show_green"}$   
       $\}$   
 $ta = \{\text{red} \rightarrow delay_{red},$   
       $\text{green} \rightarrow delay_{green},$   
       $\text{yellow} \rightarrow delay_{yellow},$   
       $\text{manual} \rightarrow \infty\}$   
 $X = \{\text{"toAuto"}, \text{"toManual"}\}$   
 $\delta_{ext} = \{(\text{(*, *}), \text{"toManual"}) \rightarrow \text{manual},$   
           $(\text{(manual, *)}, \text{"toAuto"}) \rightarrow \text{red}\}$ 
```

## Operational Semantics

```
time = 0  
current_state = initial_state  
last_time = -initial_elapsed  
while not termination_condition():  
    next_time = last_time + ta(current_state)  
    if time_next_ev <= next_time:  
        e = time_next_ev - last_time  
        time = time_next_ev  
        current_state =  $\delta_{ext}((\text{current\_state}, e), \text{next\_ev})$   
    else:  
        time = next_time  
        output( $\lambda(\text{current\_state})$ )  
        current_state =  $\delta_{int}(\text{current\_state})$   
    last_time = time
```

## Abstract Syntax

```
Y = {"show_red", "show_green", "show_yellow"}  
S = {red, yellow, green, manual}  
 $q_{init} = (\text{green}, 0)$   
 $\delta_{int} = \{\text{red} \rightarrow \text{green},$   
           $\text{green} \rightarrow \text{yellow},$   
           $\text{yellow} \rightarrow \text{red}\}$   
 $\lambda = \{\text{green} \rightarrow \text{"show\_yellow"},$   
         $\text{yellow} \rightarrow \text{"show\_red"},$   
         $\text{red} \rightarrow \text{"show\_green"}$   
       $\}$   
 $ta = \{\text{red} \rightarrow delay_{red},$   
       $\text{green} \rightarrow delay_{green},$   
       $\text{yellow} \rightarrow delay_{yellow},$   
       $\text{manual} \rightarrow \infty\}$   
 $X = \{\text{"toAuto"}, \text{"toManual"}\}$   
 $\delta_{ext} = \{(\text{(*, *}), \text{"toManual"}) \rightarrow \text{manual},$   
           $(\text{(manual, *)}, \text{"toAuto"}) \rightarrow \text{red}\}$ 
```

## Concrete Syntax



```
from pypdevs.DEVS import *\n\n\nclass TrafficLight(AtomicDEVS):\n    def __init__(self, ...):\n        AtomicDEVS.__init__(self, "light")\n        self.interrupt = self.addInPort("interrupt")\n\n        ...\n\n        ...\n\n    def extTransition(self, inputs):\n        inp = inputs[self.interrupt]\n        if inp == "toManual":\n            return "manual"\n        elif inp == "toAuto":\n            if self.state == "manual":\n                return "red"
```

\_\_ Current Time: 0.00 \_\_\_\_\_

INITIAL CONDITIONS in model <light>

Initial State: green

Next scheduled internal transition at time 57.00

\_\_ Current Time: 57.00 \_\_\_\_\_

INTERNAL TRANSITION in model <light>

New State: yellow

Output Port Configuration:

port <observer>:

show\_yellow

Next scheduled internal transition at time 60.00

\_\_ Current Time: 60.00 \_\_\_\_\_

INTERNAL TRANSITION in model <light>

New State: red

Output Port Configuration:

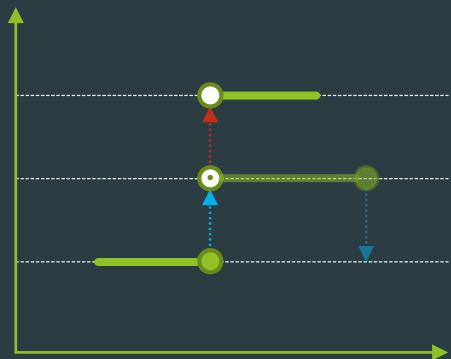
port <observer>:

show\_red

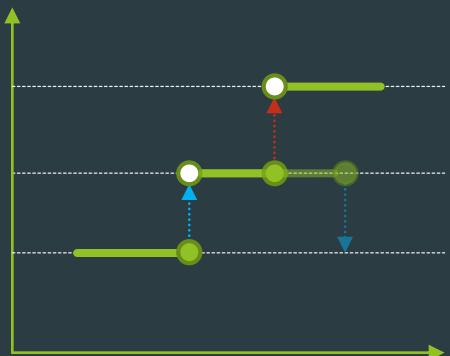
Next scheduled internal transition at time 120.00

$$Q = \{(s, e) | s \in S, 0 \leq e \leq ta(s)\}$$

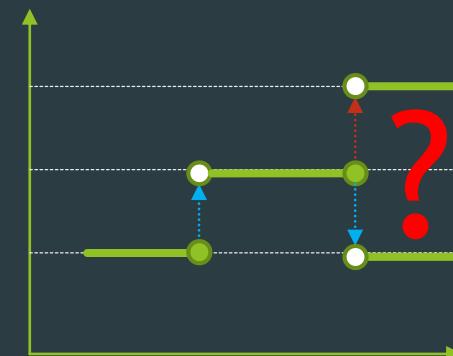
$$e = 0$$

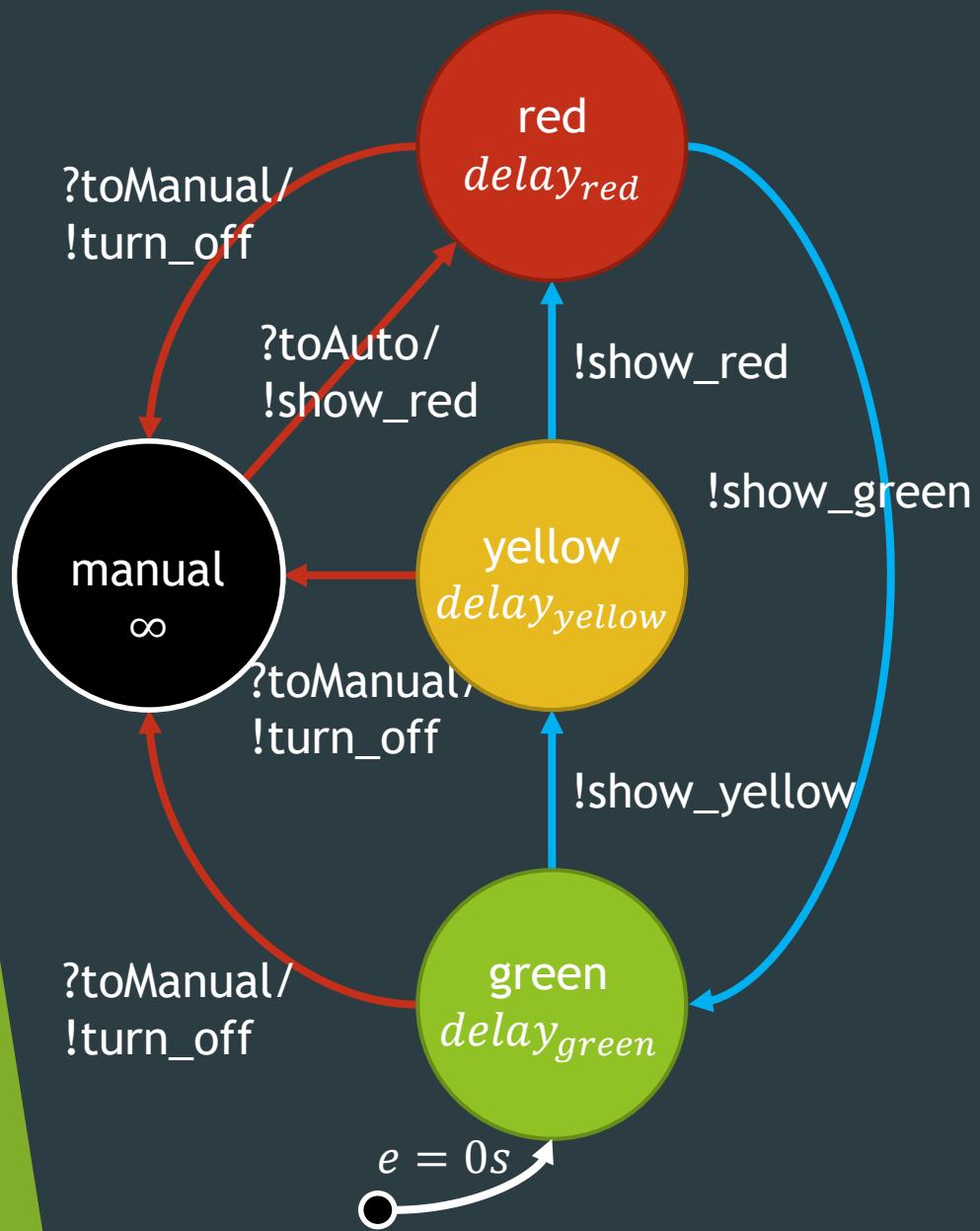


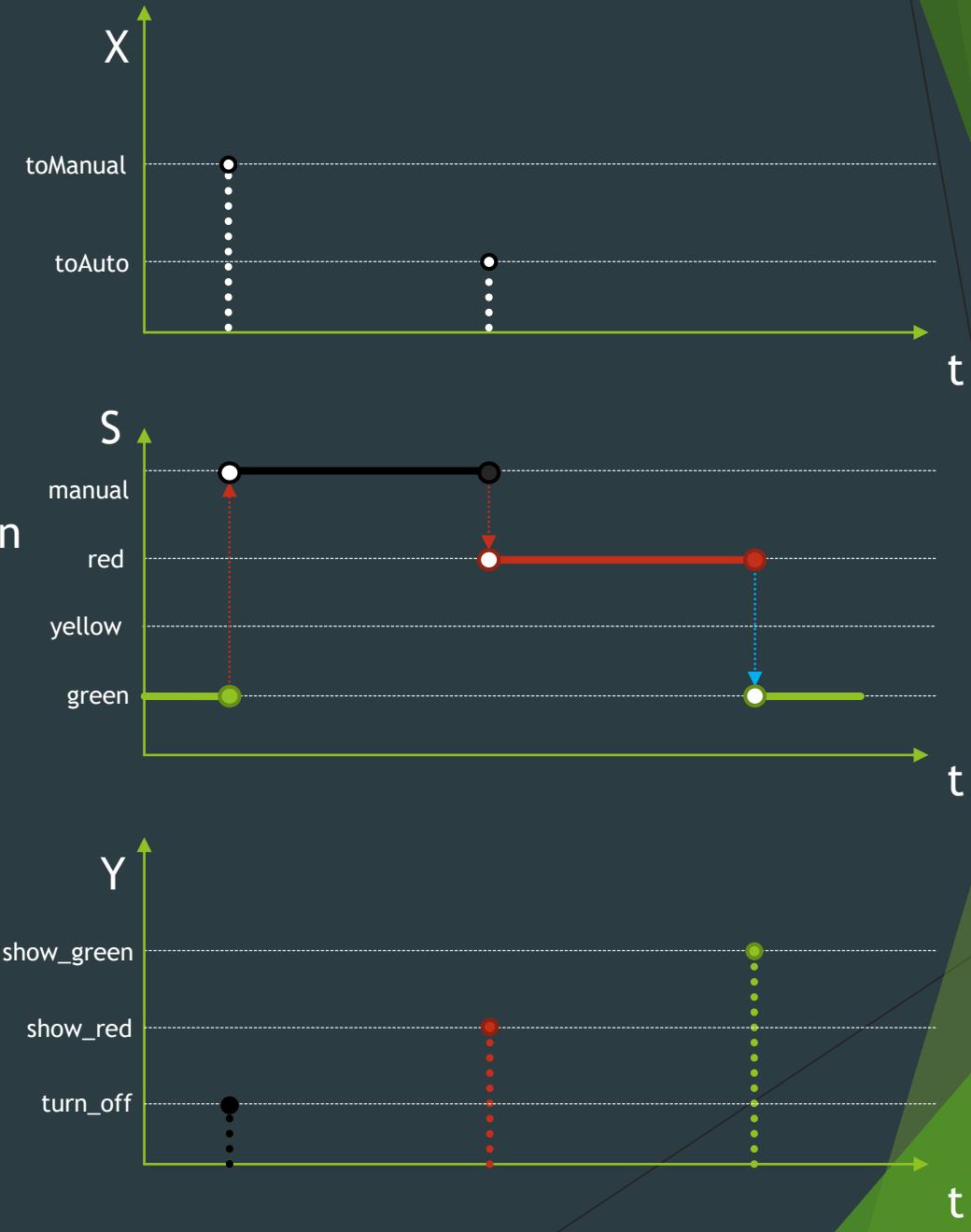
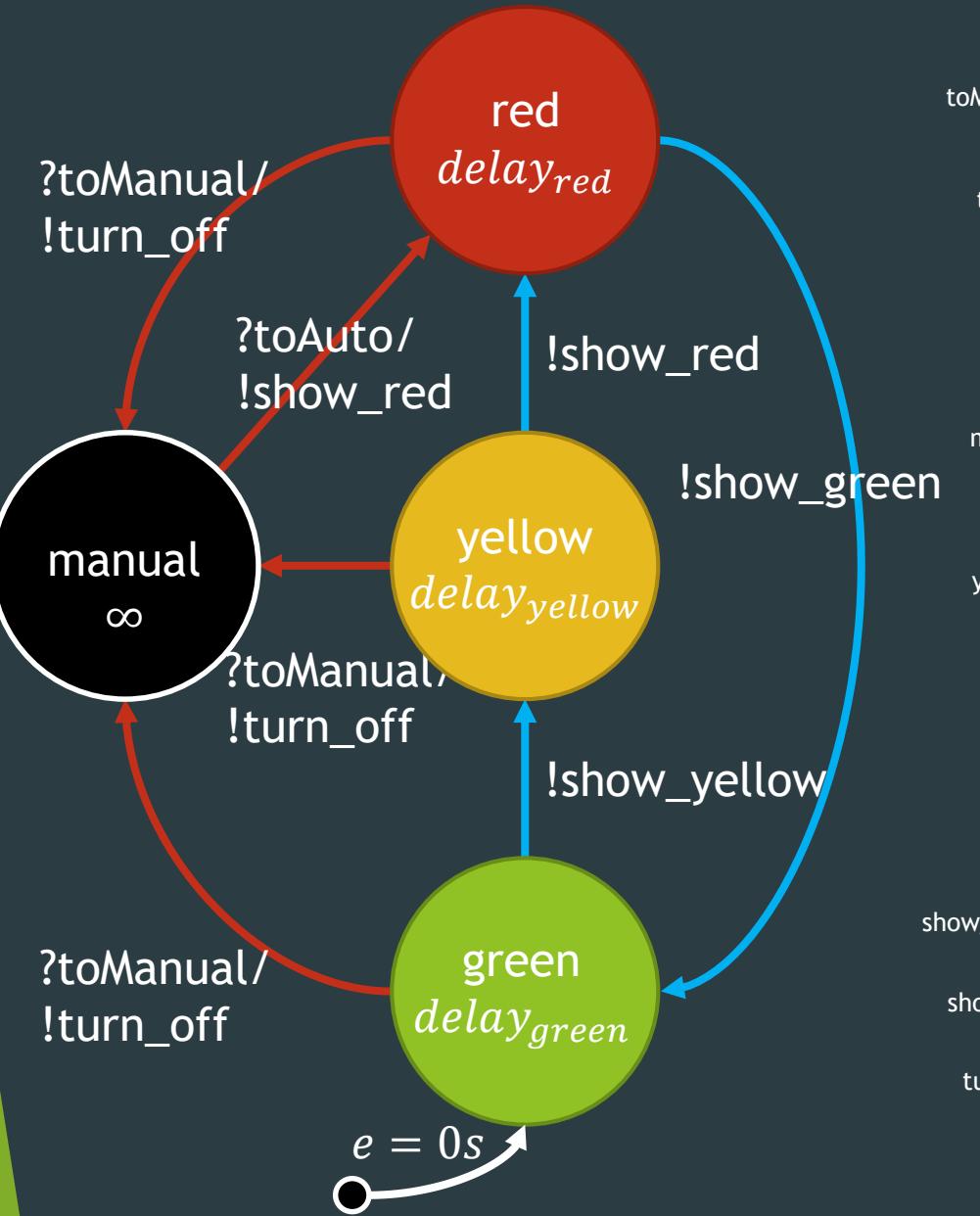
$$0 < e < ta(s)$$

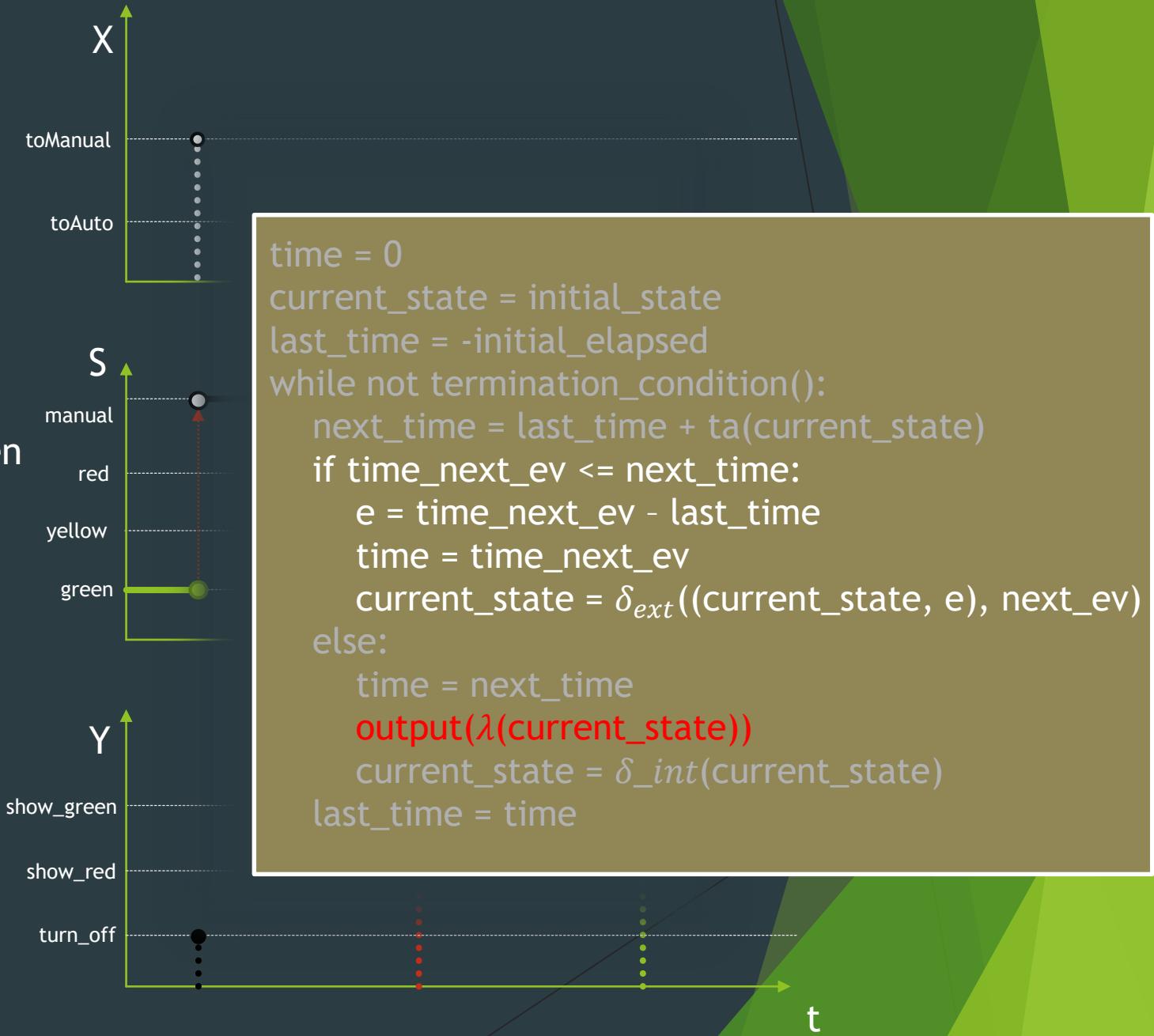
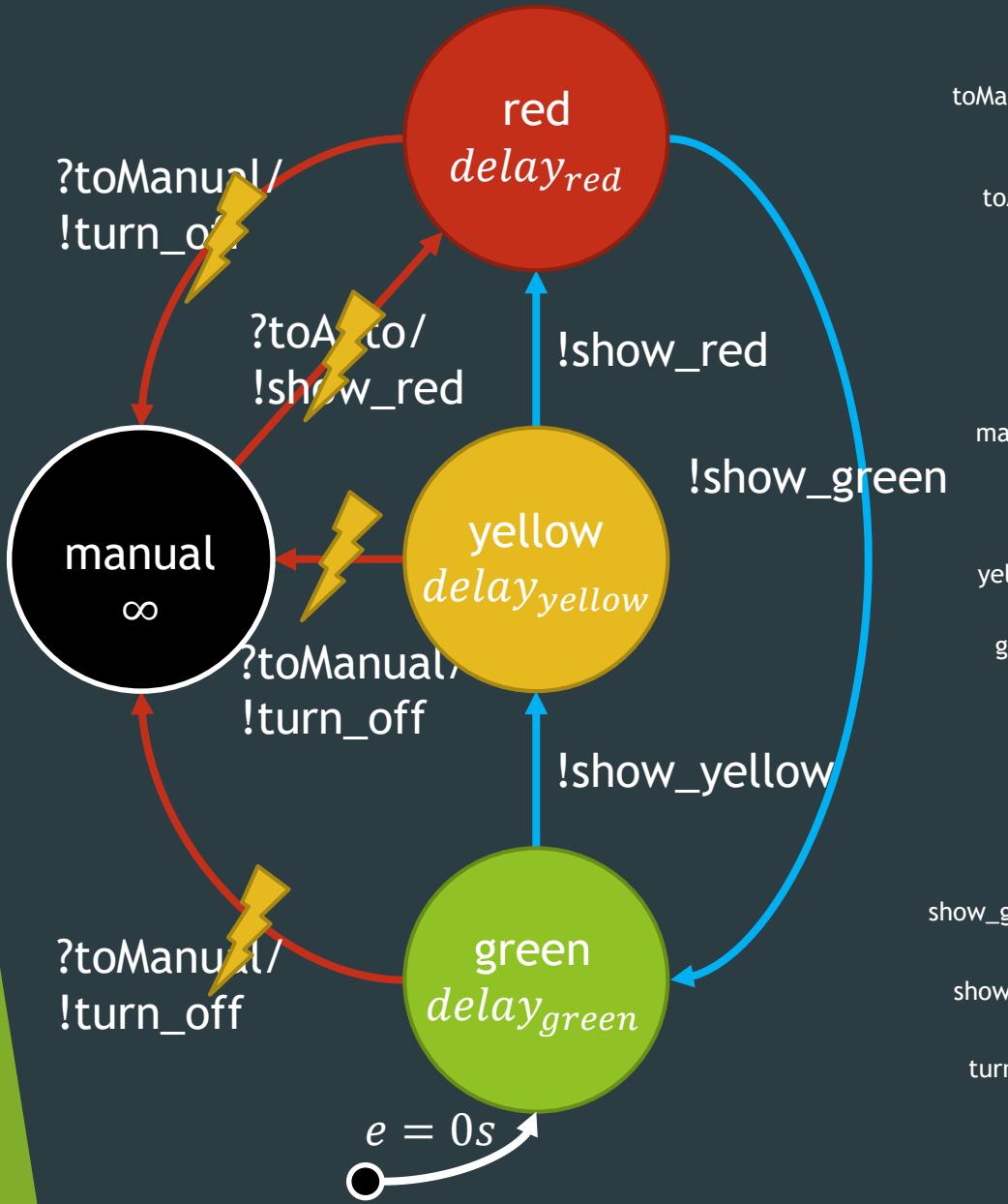


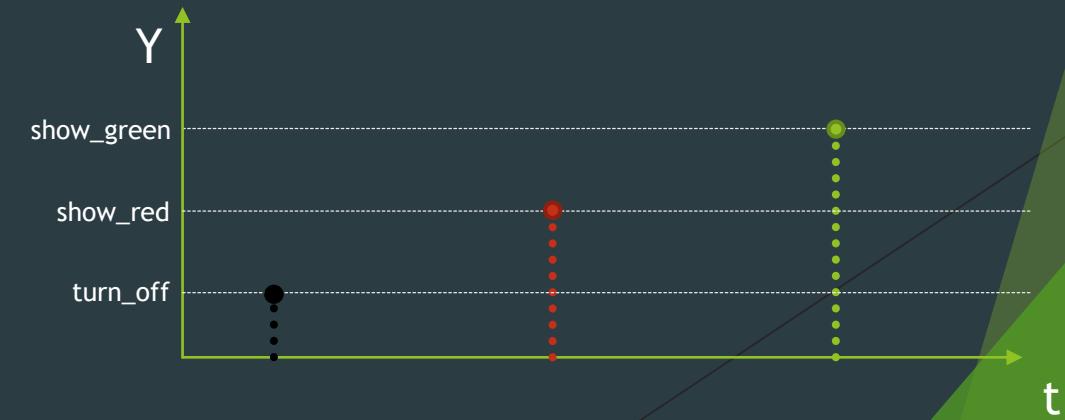
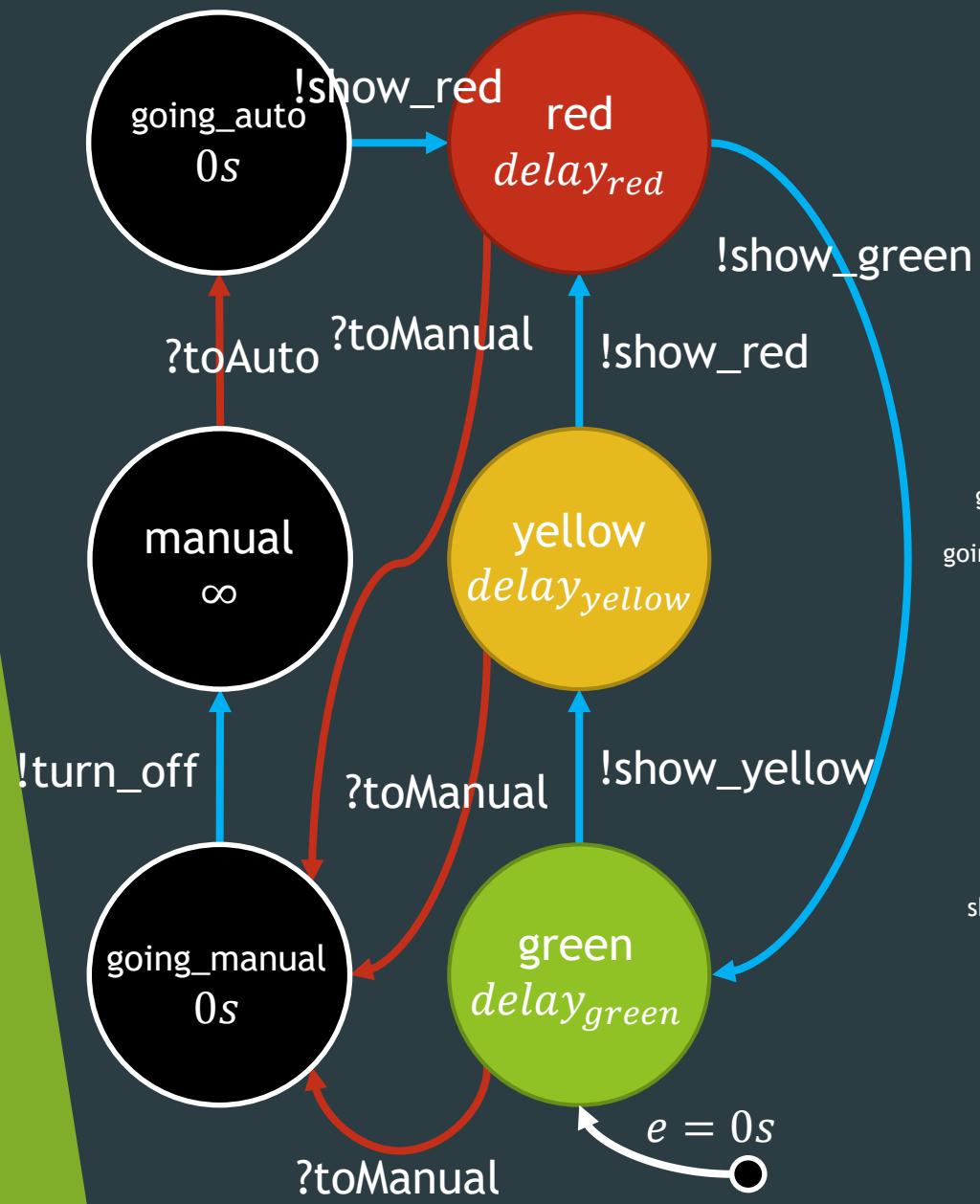
$$e = ta(s)$$











# Full Atomic DEVS Specification

$$M = \langle X, Y, S, q_{init}, \delta_{int}, \delta_{ext}, \lambda, ta \rangle$$

$X$  : set of input events

$Y$  : set of output events

$S$  : set of sequential states

$q_{init} : Q$

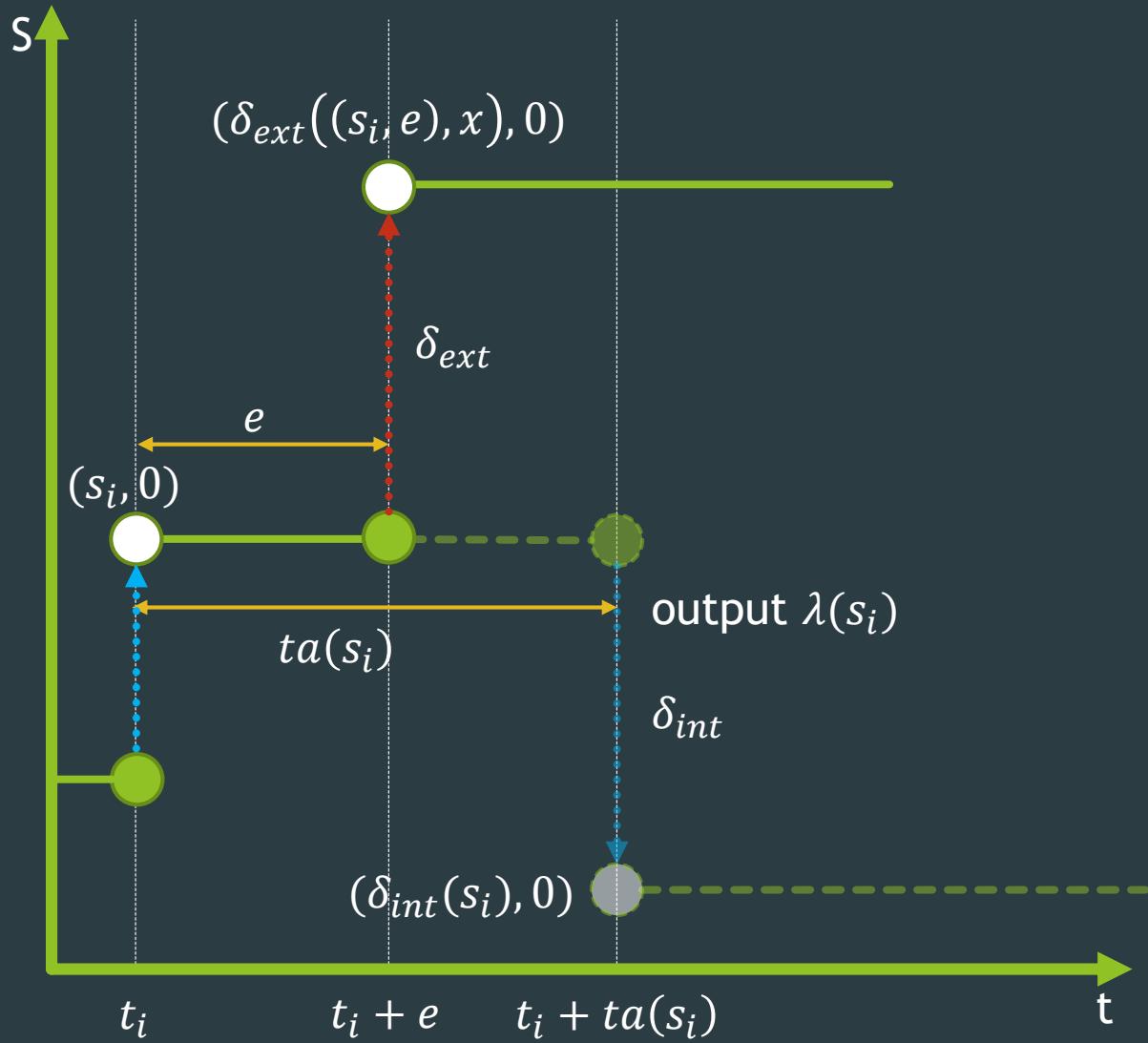
$$Q = \{(s, e) | s \in S, 0 \leq e \leq ta(s)\}$$

$\delta_{int} : S \rightarrow S$

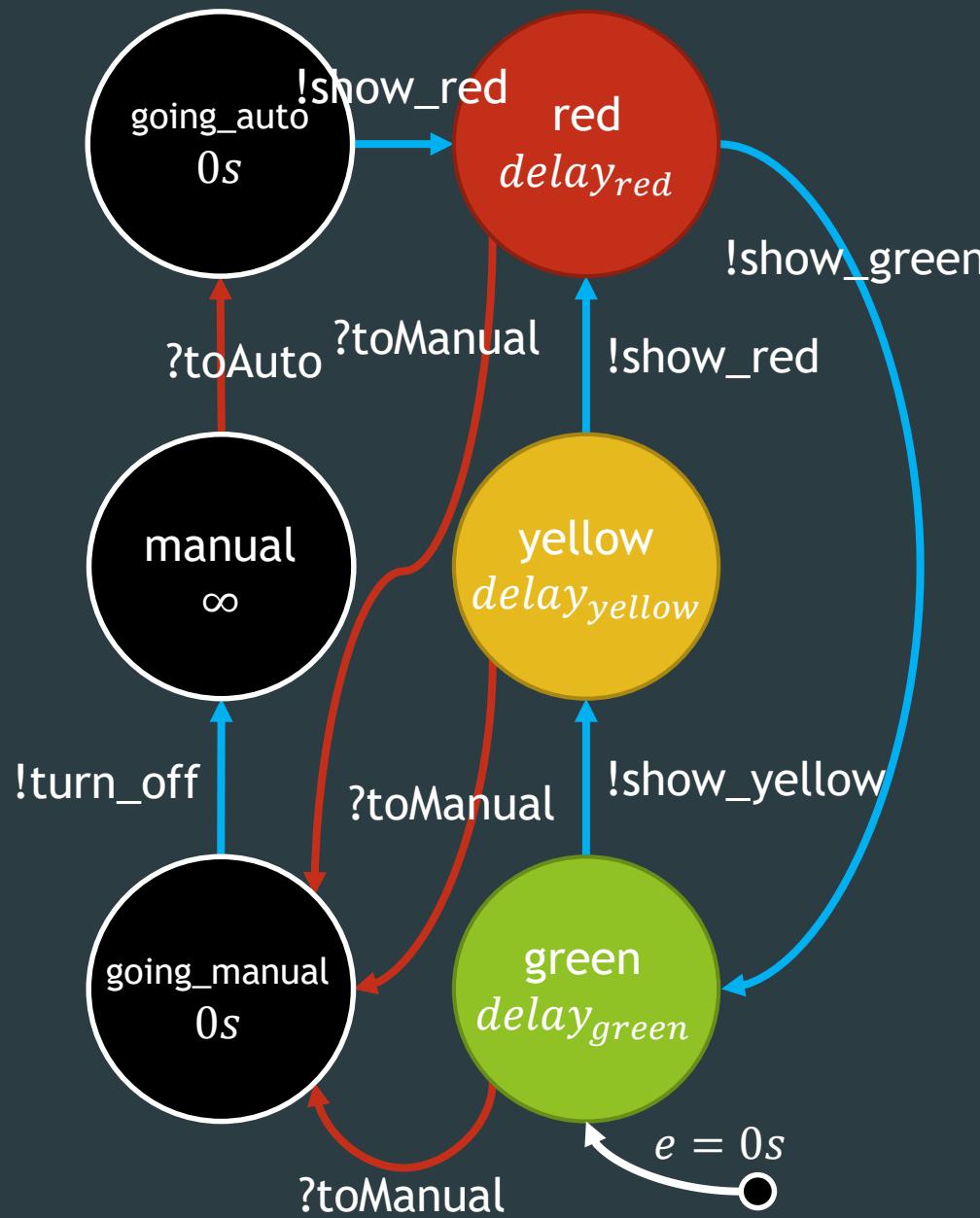
$\delta_{ext} : Q \times X \rightarrow S$

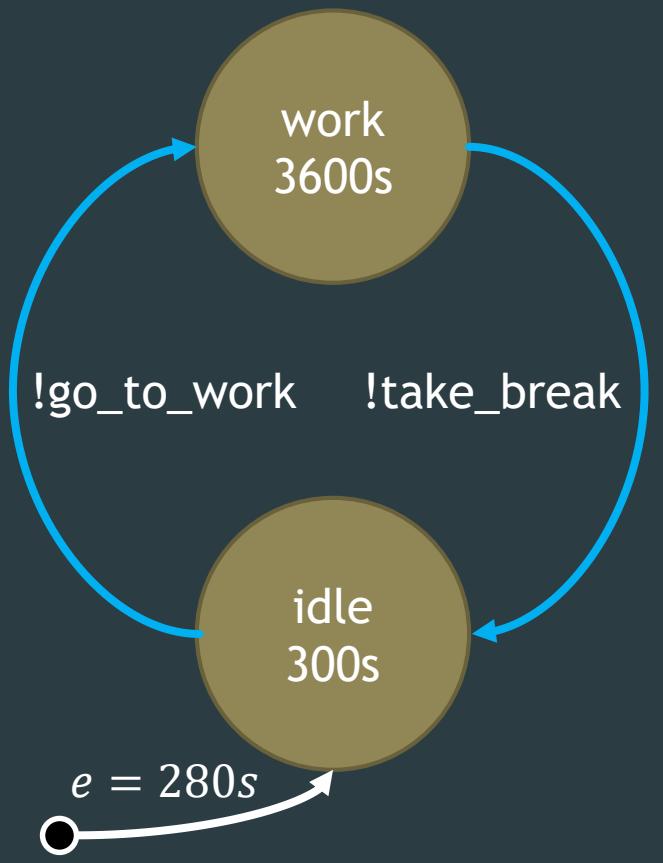
$\lambda : S \rightarrow Y \cup \{\phi\}$

$ta : S \rightarrow \mathbb{R}_{0,+\infty}^+$



# Coupled Models

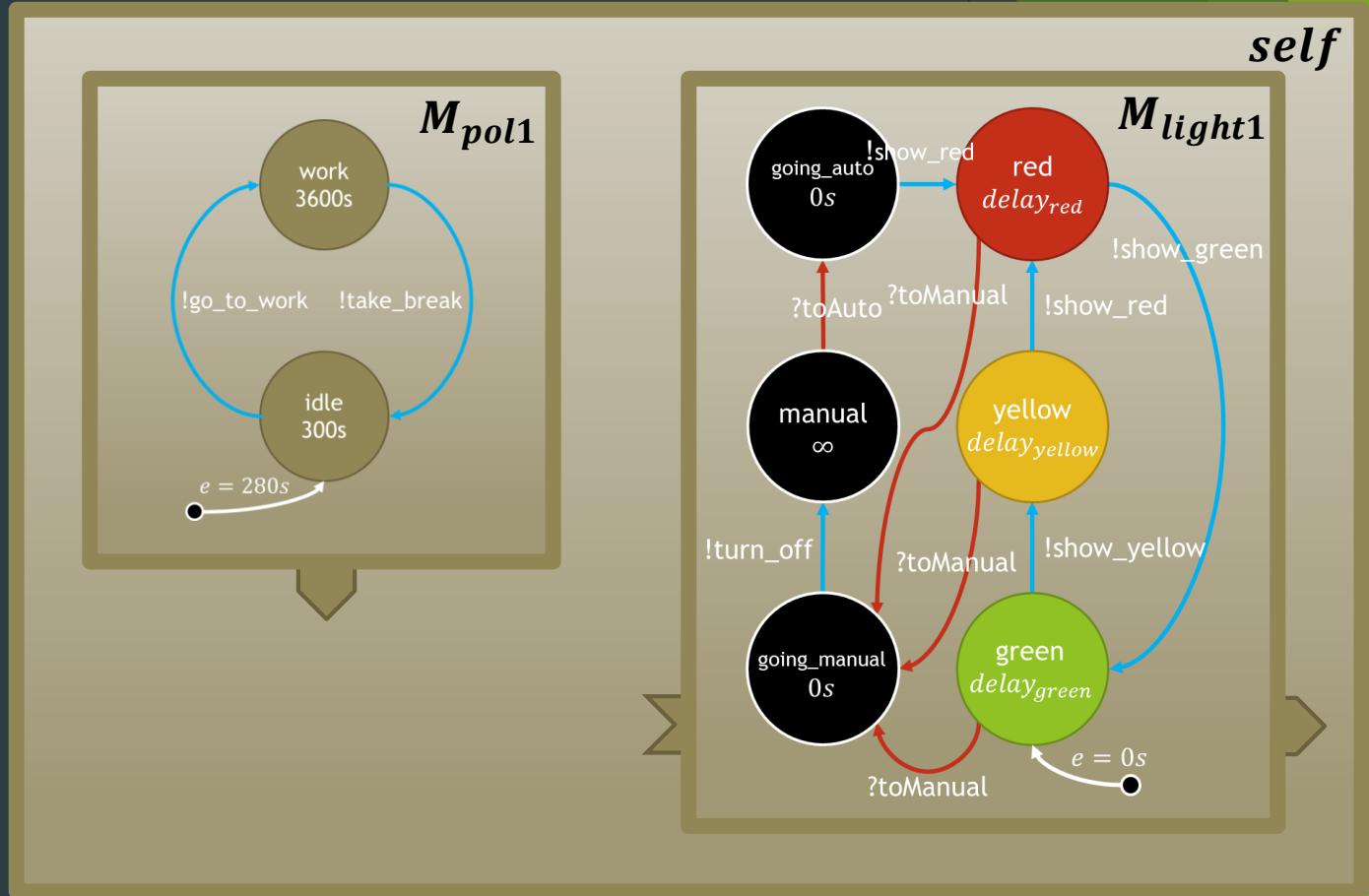




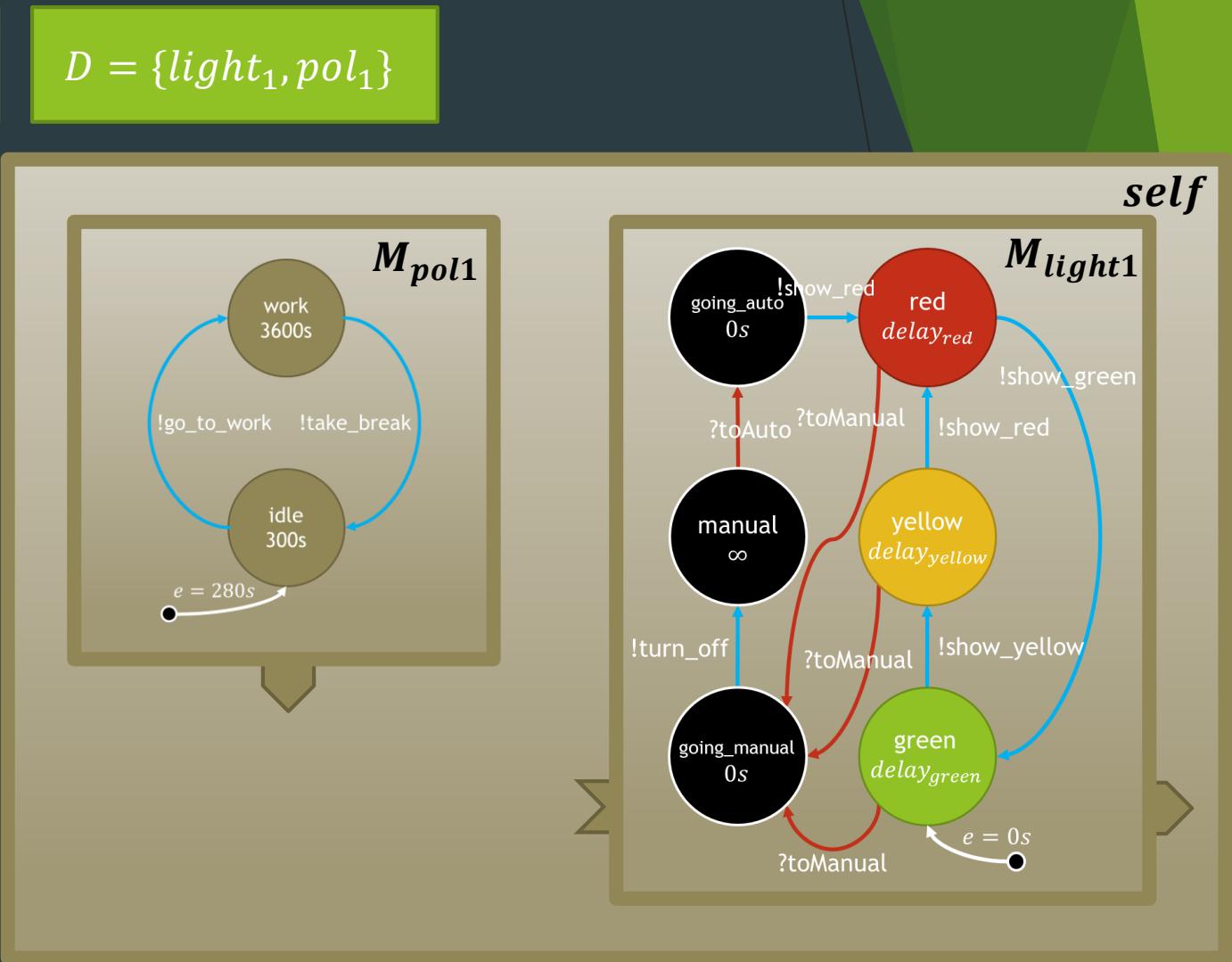
$$\mathcal{C} = \langle D, MS \rangle$$

$$MS = \{M_i | i \in D\}$$

$$M_i = \langle X_i, Y_i, S_i, q_{init,i}, \delta_{int,i}, \delta_{ext,i}, \lambda_i, ta_i \rangle, \forall i \in D$$



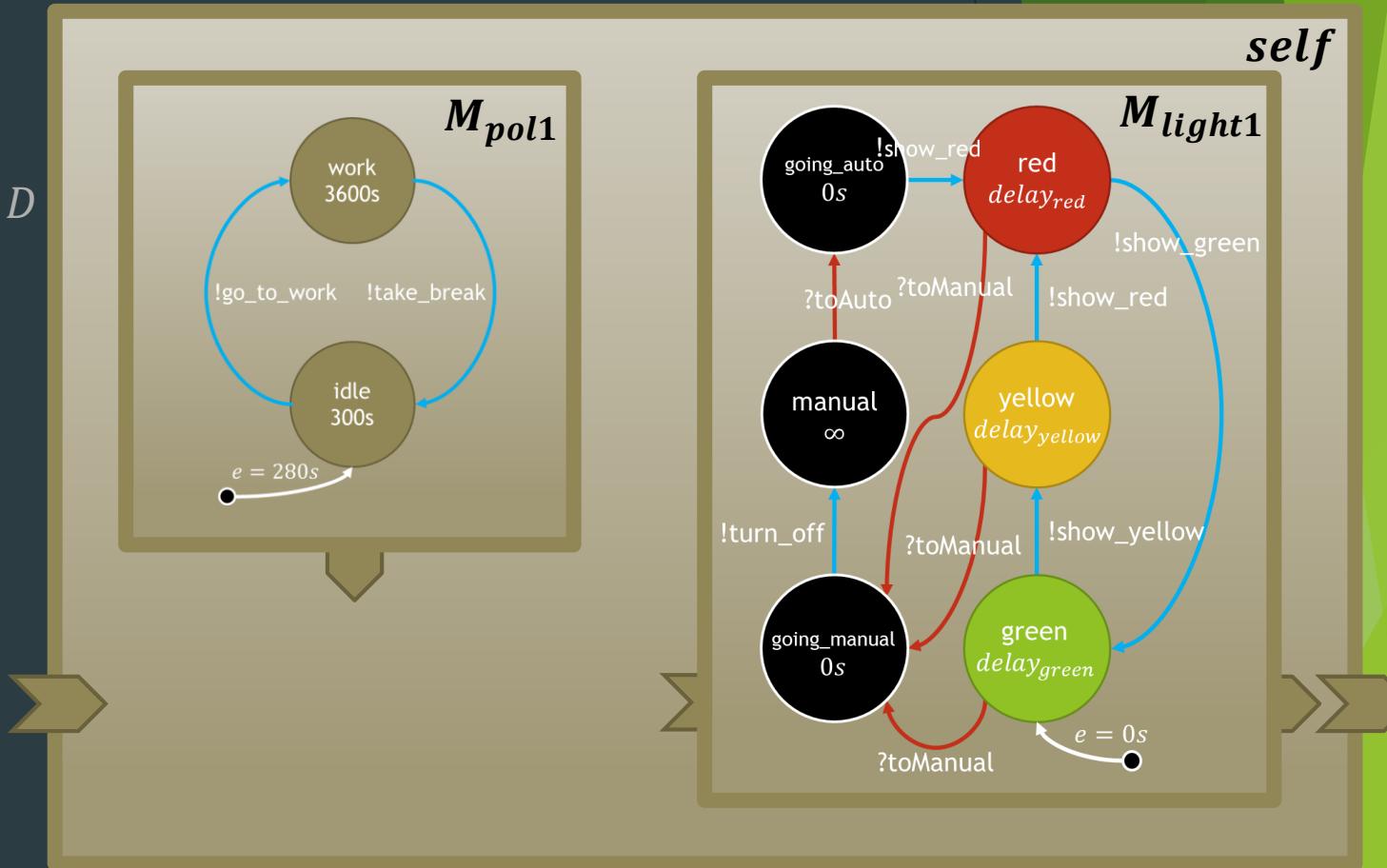
$$\begin{aligned}
 C &= \langle D, MS \rangle \\
 MS &= \{M_i | i \in D\} \\
 M_i &= \langle X_i, Y_i, S_i, q_{init,i}, \delta_{int,i}, \delta_{ext,i}, \lambda_i, ta_i \rangle, \forall i \in D
 \end{aligned}$$



$$C = \langle X_{self}, Y_{self}, D, MS \rangle$$

$$MS = \{M_i | i \in D\}$$

$$M_i = \langle X_i, Y_i, S_i, q_{init,i}, \delta_{int,i}, \delta_{ext,i}, \lambda_i, ta_i \rangle, \forall i \in D$$



$$C = \langle X_{self}, Y_{self}, D, MS, IS \rangle$$

$$MS = \{M_i | i \in D\}$$

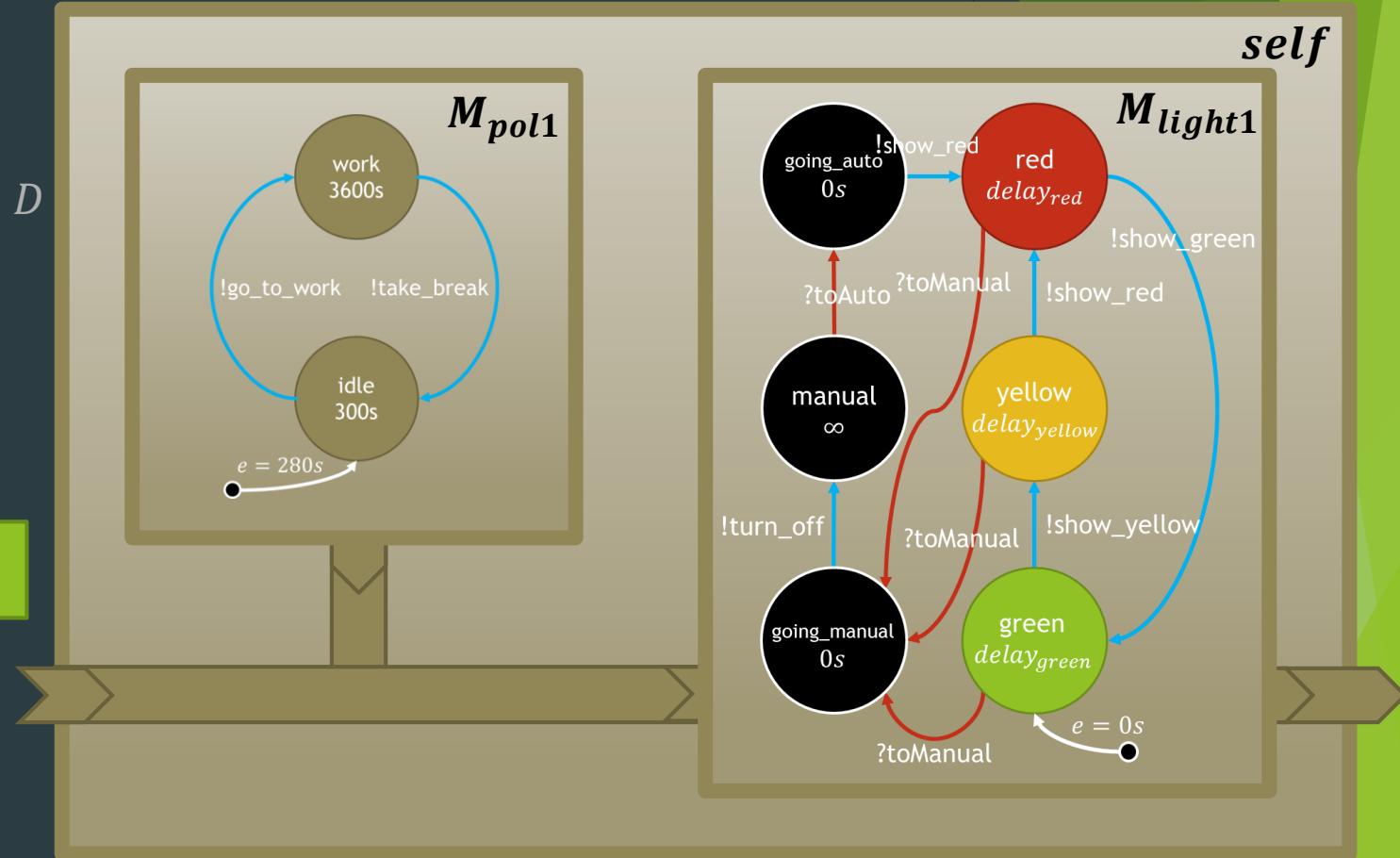
$$M_i = \langle X_i, Y_i, S_i, q_{init,i}, \delta_{int,i}, \delta_{ext,i}, \lambda_i, ta_i \rangle, \forall i \in D$$

$$IS = \{I_i | i \in D \cup \{self\}\}$$

$$\forall i \in D \cup \{self\} : I_i \subseteq D \cup \{self\}$$

$$\forall i \in D \cup \{self\} : i \notin I_i$$

$I_i$  :Influences of  $i$



$$C = \langle X_{self}, Y_{self}, D, MS, IS \rangle$$

$$MS = \{M_i | i \in D\}$$

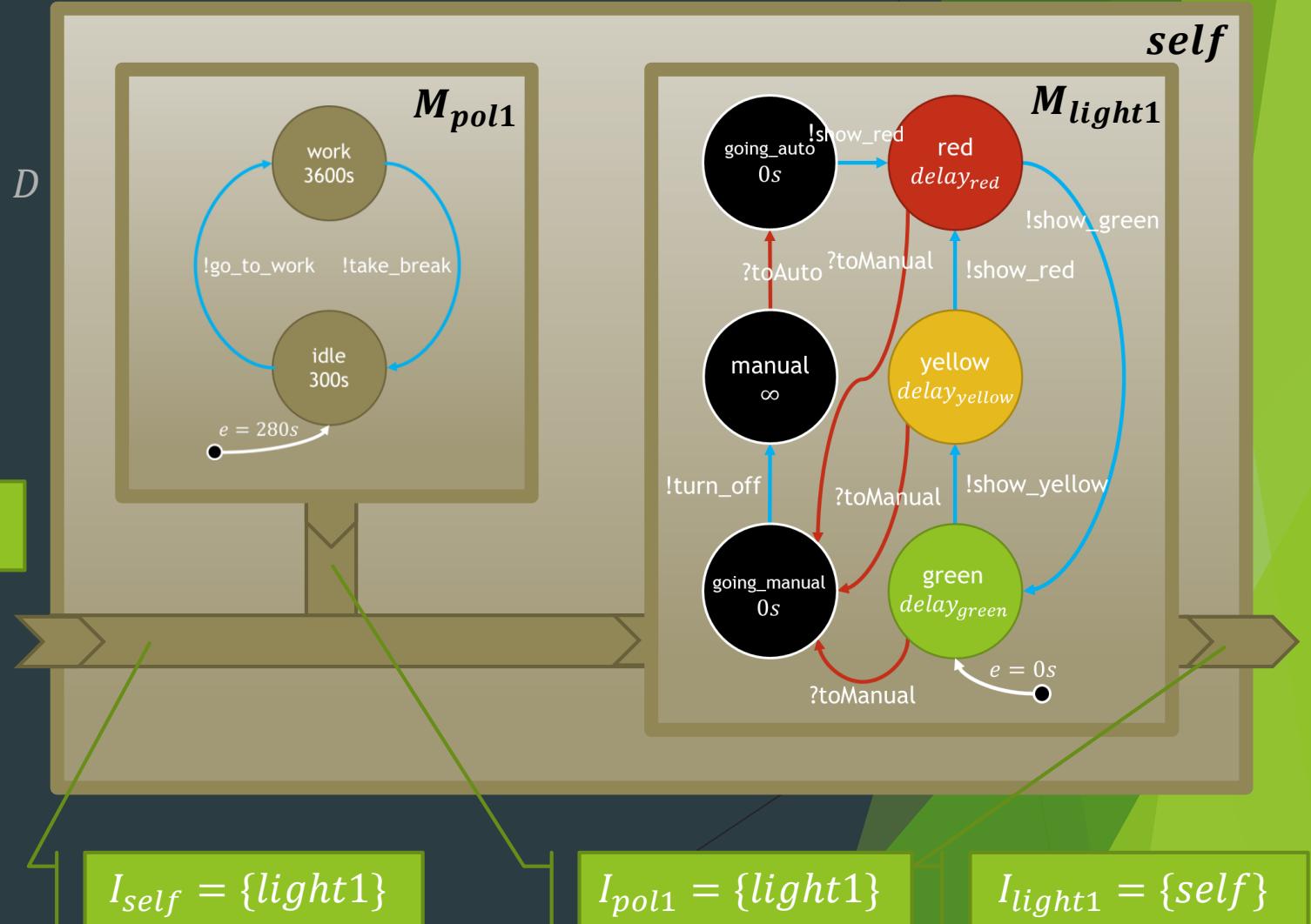
$$M_i = \langle X_i, Y_i, S_i, q_{init,i}, \delta_{int,i}, \delta_{ext,i}, \lambda_i, ta_i \rangle, \forall i \in D$$

$$IS = \{I_i | i \in D \cup \{self\}\}$$

$$\forall i \in D \cup \{self\} : I_i \subseteq D \cup \{self\}$$

$$\forall i \in D \cup \{self\} : i \notin I_i$$

$I_i$  :Influences of  $i$



$$Y_{pol1} = \{go\_to\_work, take\_break\}$$

$$C = \langle X_{self}, Y_{self}, D, MS, IS, ZS \rangle$$

$$MS = \{M_i | i \in D\}$$

$$M_i = \langle X_i, Y_i, S_i, q_{init,i}, \delta_{int,i}, \delta_{ext,i}, \lambda_i, ta_i \rangle, \forall i \in D$$

$$IS = \{I_i | i \in D \cup \{self\}\}$$

$$\forall i \in D \cup \{self\} : I_i \subseteq D \cup \{self\}$$

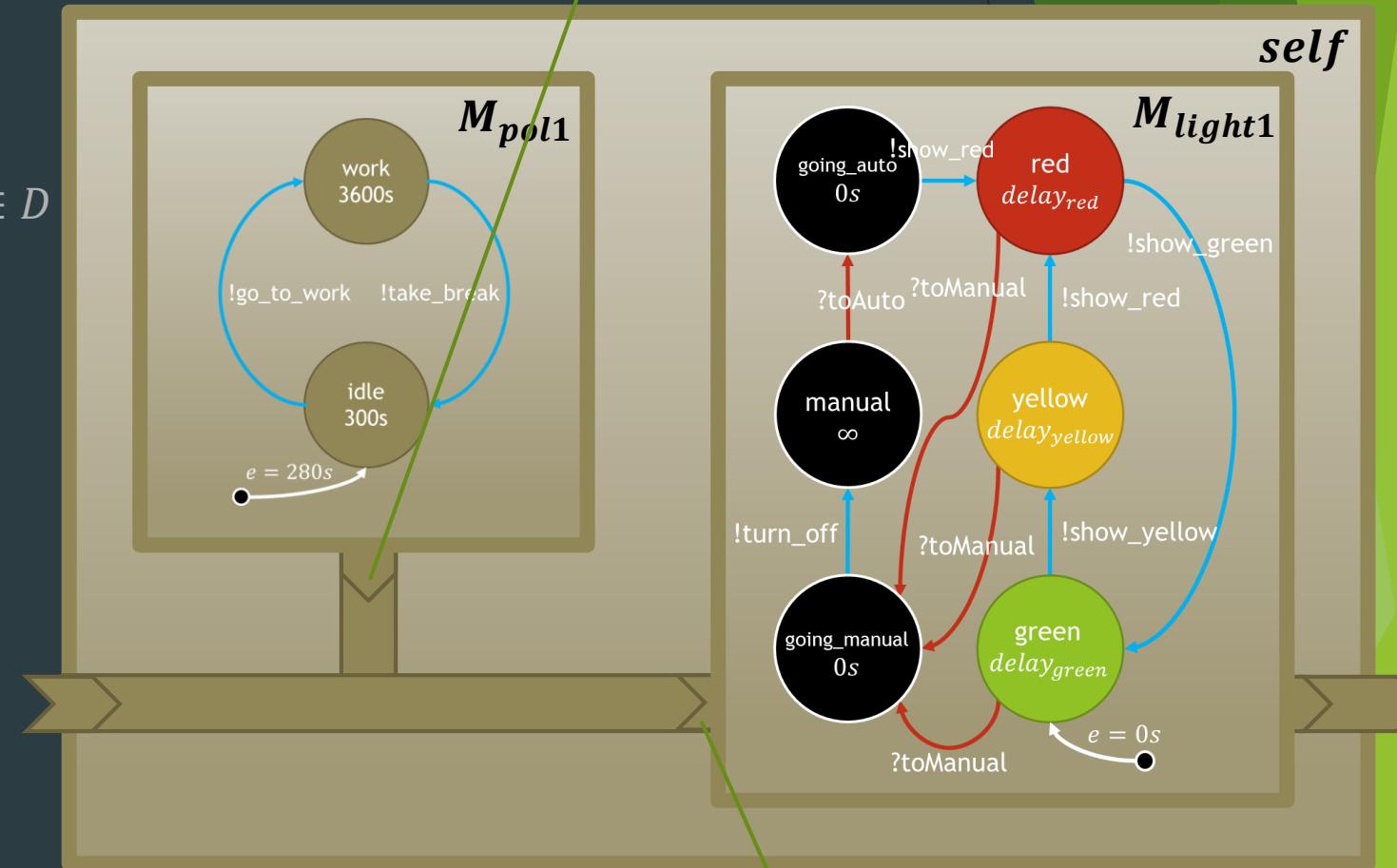
$$\forall i \in D \cup \{self\} : i \notin I_i$$

$$ZS = \{Z_{i,j} | i \in D \cup \{self\}, j \in I_i\}$$

$$Z_{self,j} : X_{self} \rightarrow X_j, \forall j \in D$$

$$Z_{i,self} : Y_i \rightarrow Y_{self}, \forall i \in D$$

$$Z_{i,j} : Y_i \rightarrow X_j, \forall i, j \in D$$



$$X_{light1} = \{toManual, toAuto\}$$

$$C = \langle X_{self}, Y_{self}, D, MS, IS, ZS \rangle$$

$$MS = \{M_i | i \in D\}$$

$$M_i = \langle X_i, Y_i, S_i, q_{init,i}, \delta_{int,i}, \delta_{ext,i}, \lambda_i, ta_i \rangle, \forall i \in D$$

$$IS = \{I_i | i \in D \cup \{self\}\}$$

$$\forall i \in D \cup \{self\} : I_i \subseteq D \cup \{self\}$$

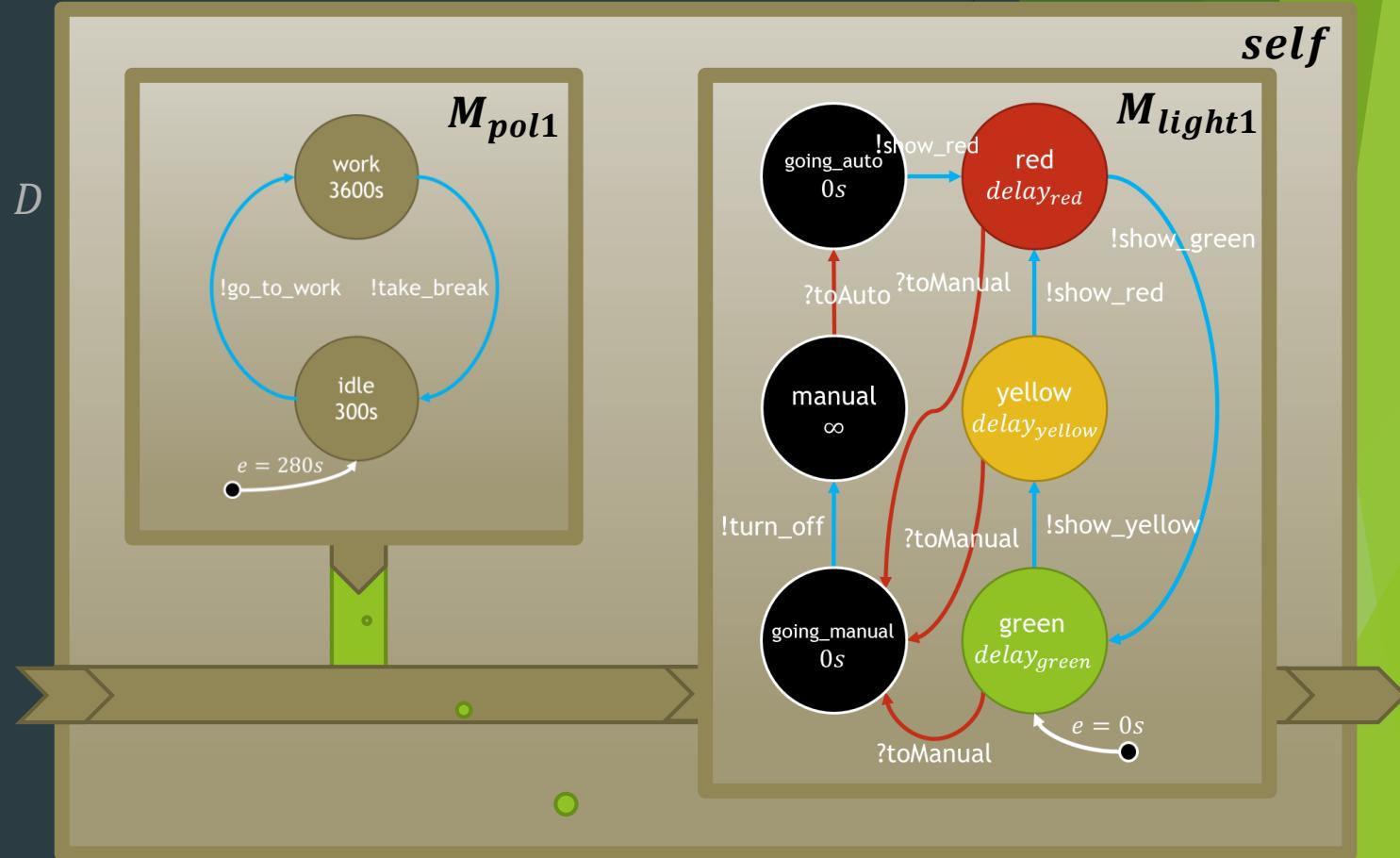
$$\forall i \in D \cup \{self\} : i \notin I_i$$

$$ZS = \{Z_{i,j} | i \in D \cup \{self\}, j \in I_i\}$$

$$Z_{self,j} : X_{self} \rightarrow X_j, \forall j \in D$$

$$Z_{i,self} : Y_i \rightarrow Y_{self}, \forall i \in D$$

$$Z_{i,j} : Y_i \rightarrow X_j, \forall i, j \in D$$



take\_break → toAuto  
go\_to\_work → toManual

$$C = \langle X_{self}, Y_{self}, D, MS, IS, ZS, select \rangle$$

$$MS = \{M_i | i \in D\}$$

$$M_i = \langle X_i, Y_i, S_i, q_{init,i}, \delta_{int,i}, \delta_{ext,i}, \lambda_i, ta_i \rangle, \forall i \in D$$

$$IS = \{I_i | i \in D \cup \{self\}\}$$

$$\forall i \in D \cup \{self\} : I_i \subseteq D \cup \{self\}$$

$$\forall i \in D \cup \{self\} : i \notin I_i$$

$$ZS = \{Z_{i,j} | i \in D \cup \{self\}, j \in I_i\}$$

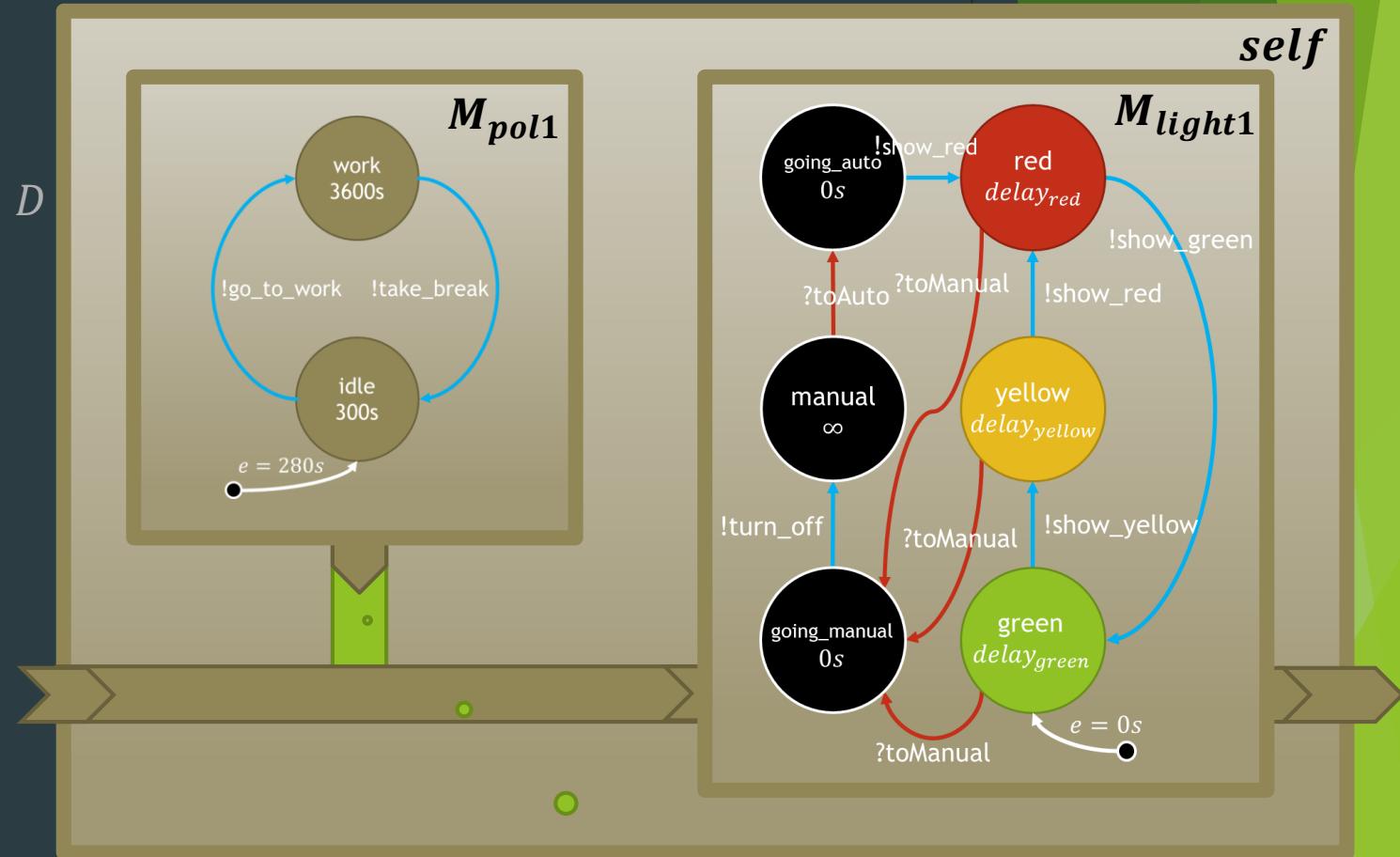
$$Z_{self,j} : X_{self} \rightarrow X_j, \forall j \in D$$

$$Z_{i,self} : Y_i \rightarrow Y_{self}, \forall i \in D$$

$$Z_{i,j} : Y_i \rightarrow X_j, \forall i, j \in D$$

$$select : 2^D \rightarrow D$$

$$\forall E \subseteq D, E \neq \emptyset : select(E) \in E$$



take\_break → toAuto  
go\_to\_work → toManual

## Concrete Syntax



trafficlight\_system.py

```
from pypdevs.DEVS import *

from trafficlight import TrafficLight
from policeman import Policeman

def translate(in_evt):
    mapping = {"take_break": "toAuto",
               "go_to_work": "toManual"}
    return mapping[in_evt]

class TrafficLightSystem(CoupledDEVS):
    def __init__(self):
        CoupledDEVS.__init__(self, "system")
        self.light = self.addSubModel(TrafficLight())
        self.police = self.addSubModel(Policeman())
        self.connectPorts(self.police.out, self.light.interrupt, translate)

    def select(self, immlist):
        if self.police in immlist:
            return self.police
        else:
            return self.light
```

— Current Time: 0.00 —

INITIAL CONDITIONS in model <system.light>

Initial State: green

Next scheduled internal transition at time 57.00

INITIAL CONDITIONS in model <system.policeman>

Initial State: idle

Next scheduled internal transition at time 20.00

\_ Current Time: 20.00 \_\_\_\_\_

EXTERNAL TRANSITION in model <system.light>

Input Port Configuration:

port <interrupt>:  
toManual

New State: going\_manual

Next scheduled internal transition at time 20.0

INTERNAL TRANSITION in model <system.policeman>

New State: working

Output Port Configuration:

port <output>:  
go\_to\_work

Next scheduled internal transition at time 3620.00

\_ Current Time: 20.00 \_\_\_\_\_

INTERNAL TRANSITION in model <system.light>

Output Port Configuration:

port <observer>:

turn\_off

New State: manual

Next scheduled internal transition at time inf

— Current Time: 3620.00 —

---

EXTERNAL TRANSITION in model <system.light>

Input Port Configuration:

port <interrupt>:

toAuto

New State: going\_auto

Next scheduled internal transition at time 3620.00

INTERNAL TRANSITION in model <system.policeman>

New State: idle

Output Port Configuration:

port <output>:

take\_break

Next scheduled internal transition at time 3920.00

\_ Current Time: 3620.00 \_\_\_\_\_

INTERNAL TRANSITION in model <system.light>

Output Port Configuration:

port <observer>:

show\_red

New State: red

Next scheduled internal transition at time 3680.00

— Current Time: 3620.00 —

---

EXTERNAL TRANSITION in model <system.light>

Input Port Configuration:

port <interrupt>:

toAuto

New State: going\_auto

Next scheduled internal transition at time 3620.00

INTERNAL TRANSITION in model <system.policeman>

New State: idle

Output Port Configuration:

port <output>:

take\_break

Next scheduled internal transition at time 3920.00

— Current Time: 3920.00 —

---

CONFLICT between models:

<system.light>

\* <system.policeman>

EXTERNAL TRANSITION in model <system.light>

Input Port Configuration:

port <interrupt>:

toManual

New State: going\_manual

Next scheduled internal transition at time 3920.00

INTERNAL TRANSITION in model <system.policeman>

New State: work

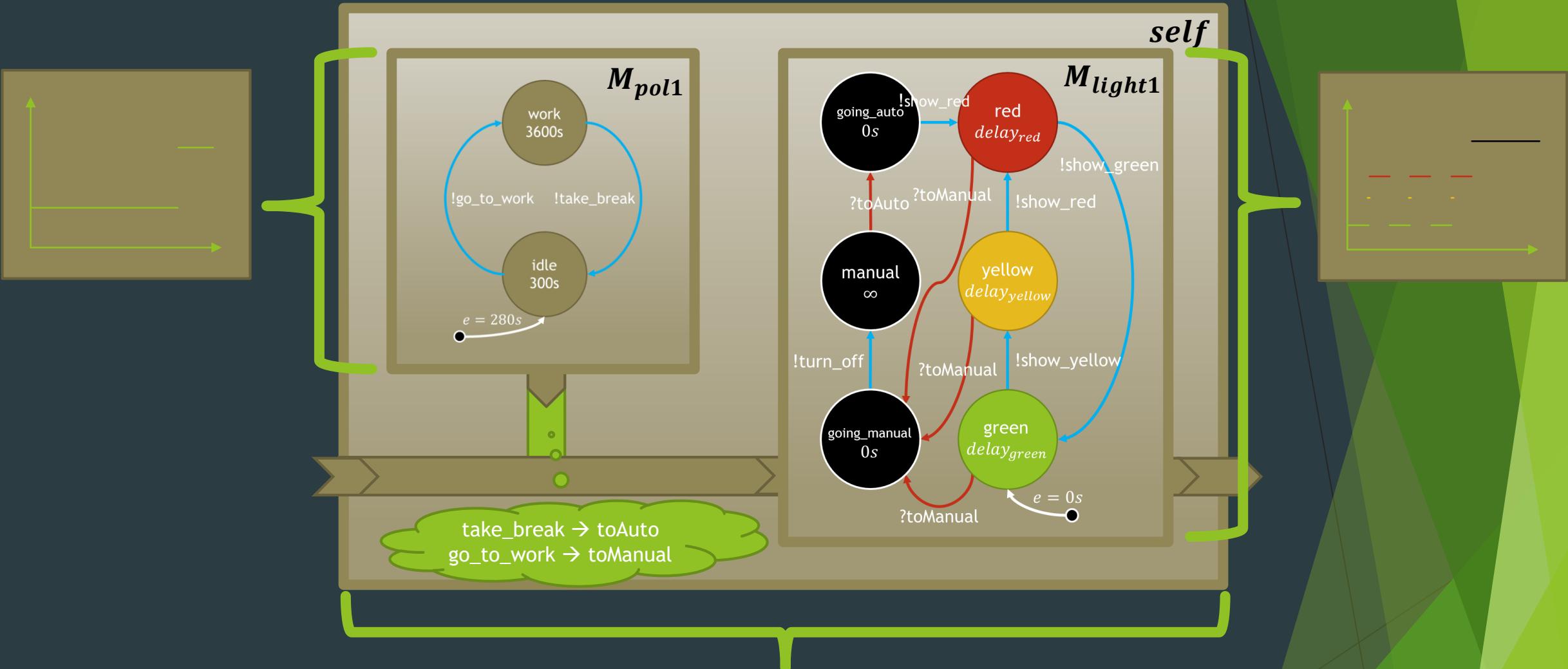
Output Port Configuration:

port <output>:

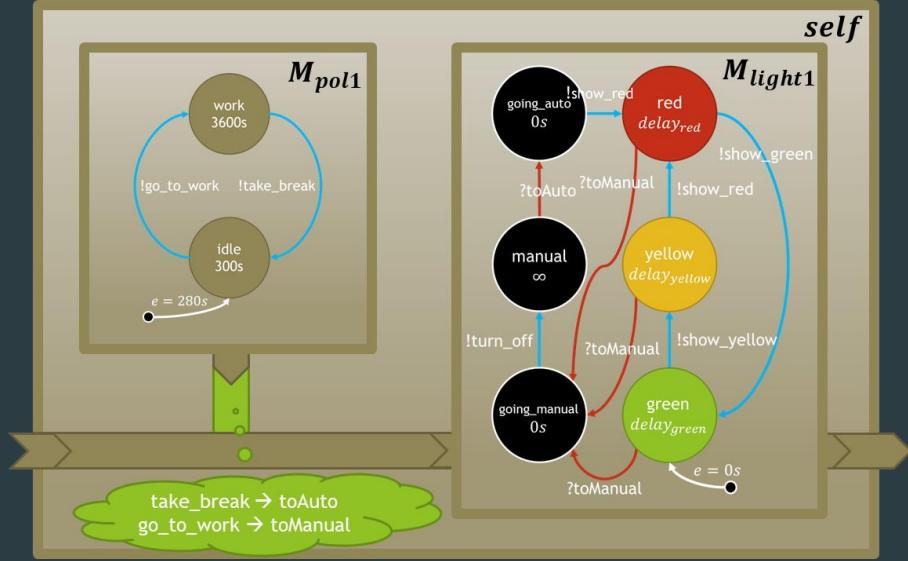
go\_to\_work

Next scheduled internal transition at time 7520.00

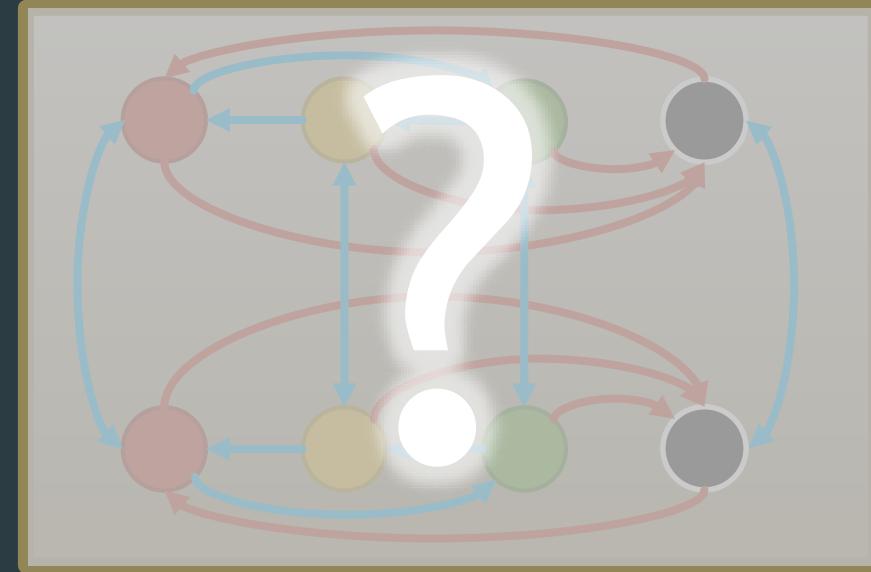
# Closure under Coupling



?



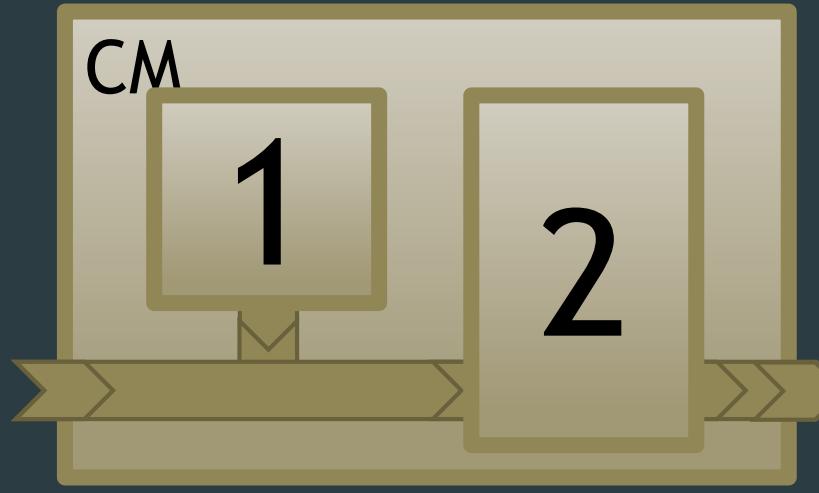
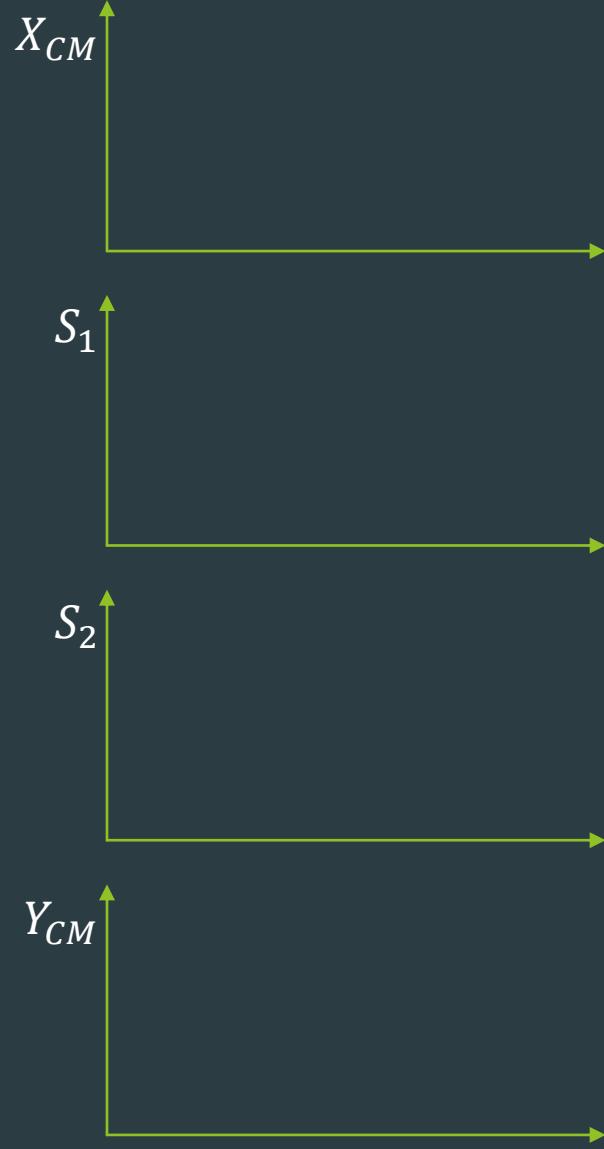
flatten

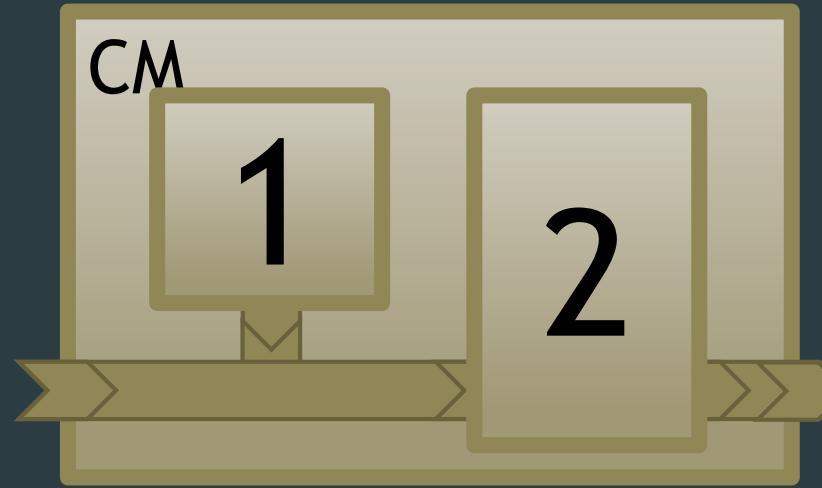
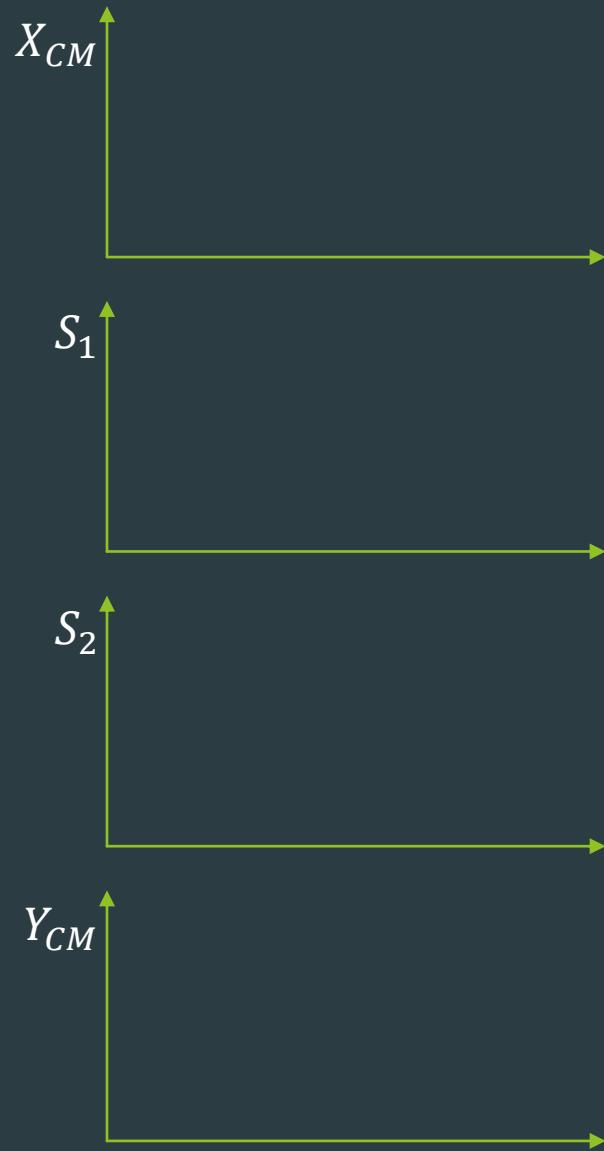


$$CM = \langle X_{self}, Y_{self}, D, MS, IS, ZS \rangle$$

$$\text{flatten}(CM) = \langle X, Y, S, q_{init}, \delta_{int}, \delta_{ext}, \lambda, ta \rangle$$



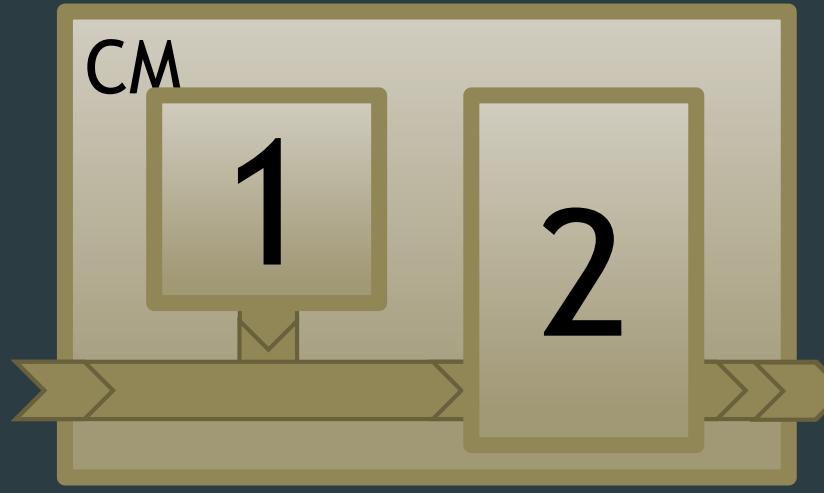
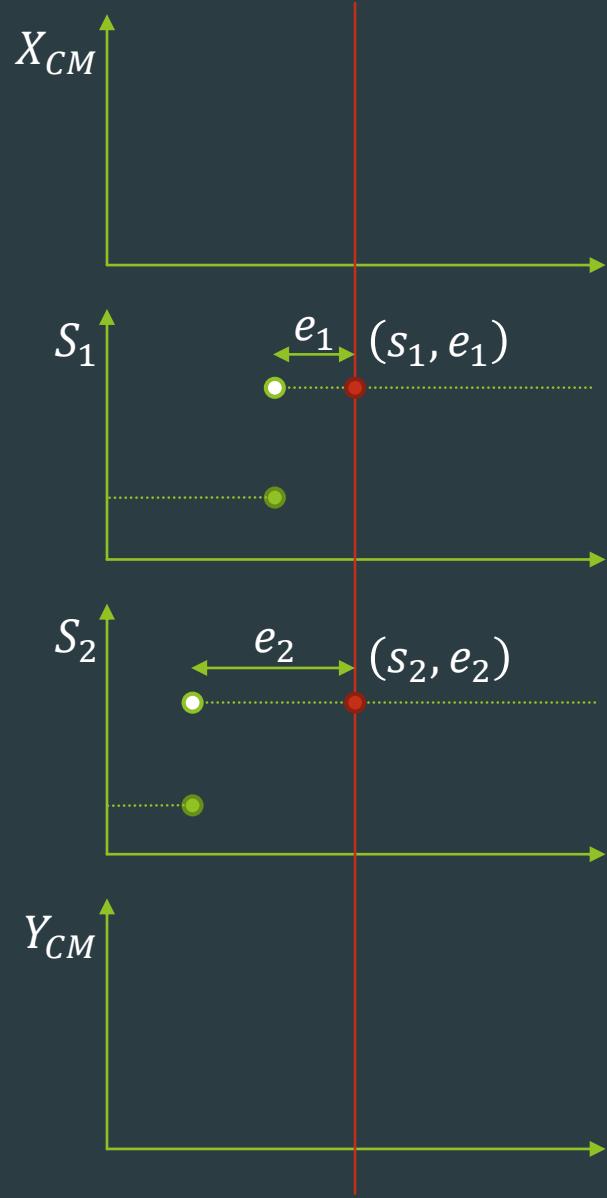

$$flatten(CM) = \langle X, Y, S, q_{init}, \delta_{int}, \delta_{ext}, \lambda, ta \rangle$$



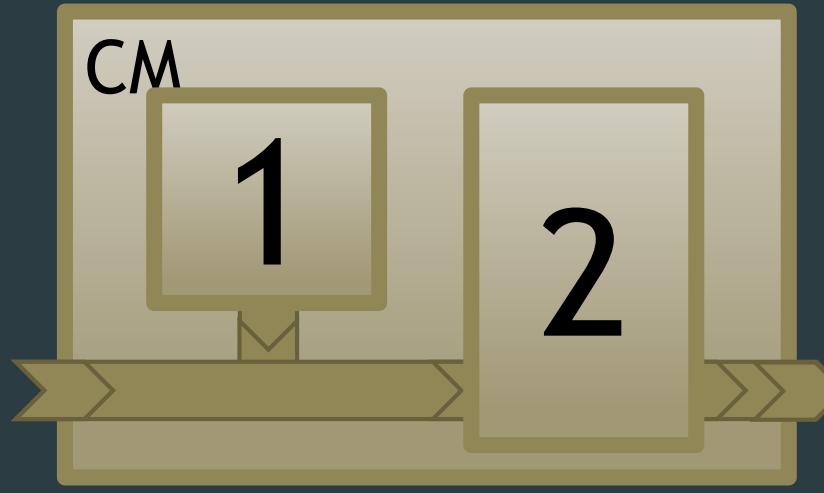
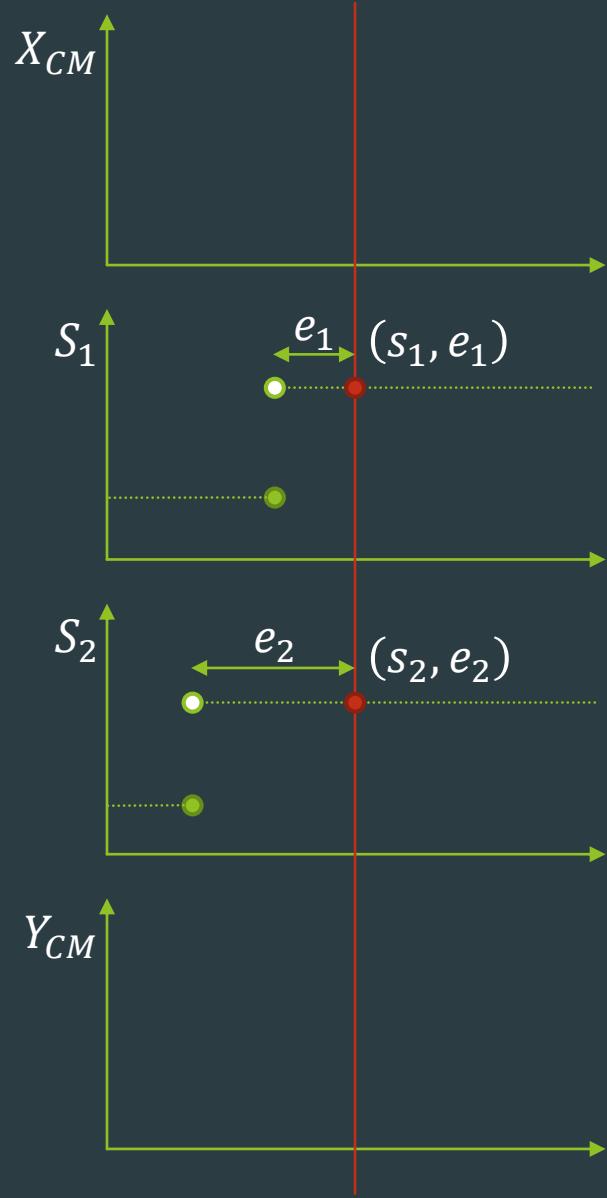
$flatten(CM) = \langle X, Y, S, q_{init}, \delta_{int}, \delta_{ext}, \lambda, ta \rangle$

$$X = X_{CM}$$

$$Y = Y_{CM}$$

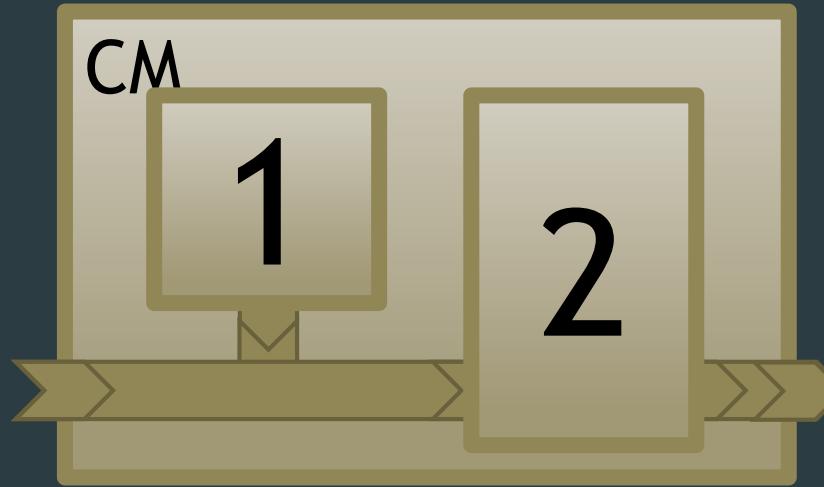
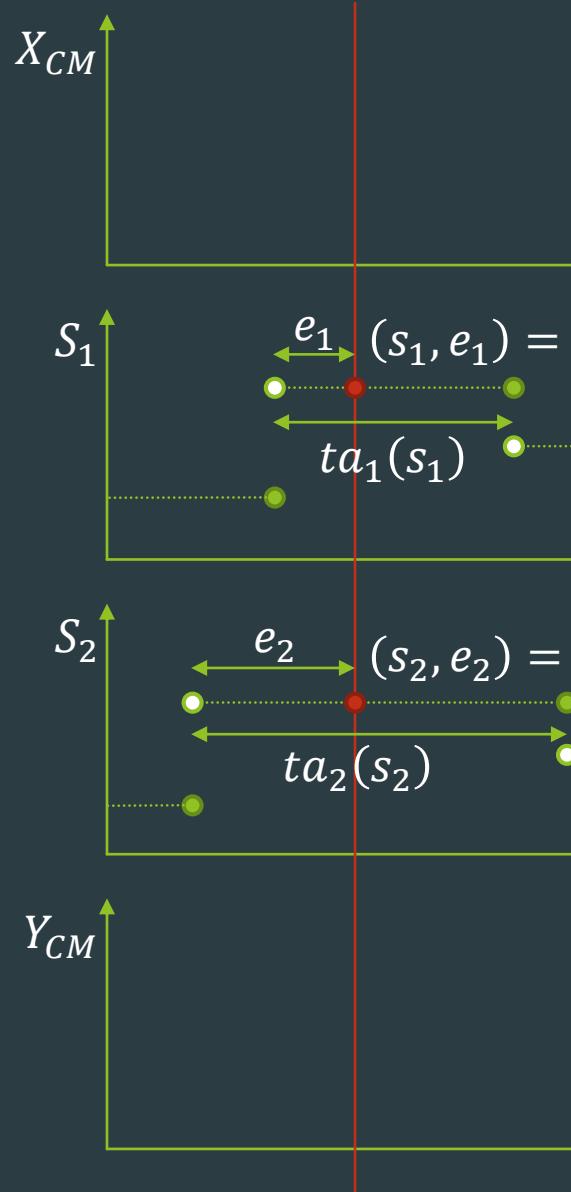


$$flatten(CM) = \langle X, Y, S, q_{init}, \delta_{int}, \delta_{ext}, \lambda, ta \rangle$$

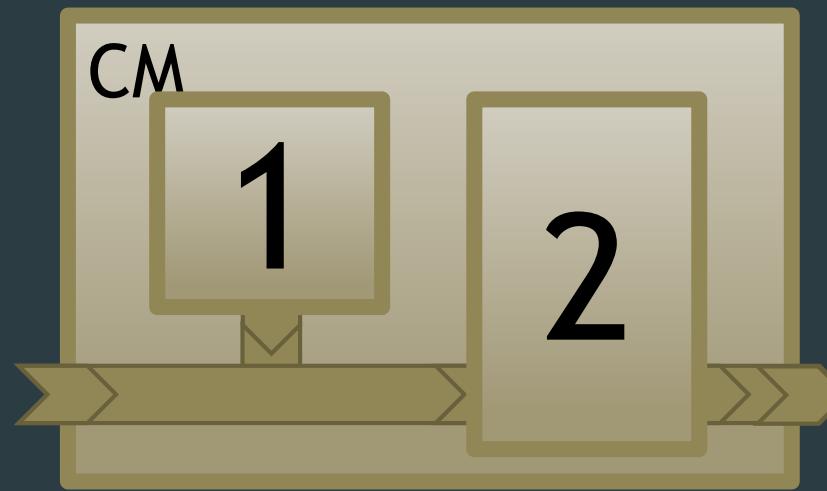
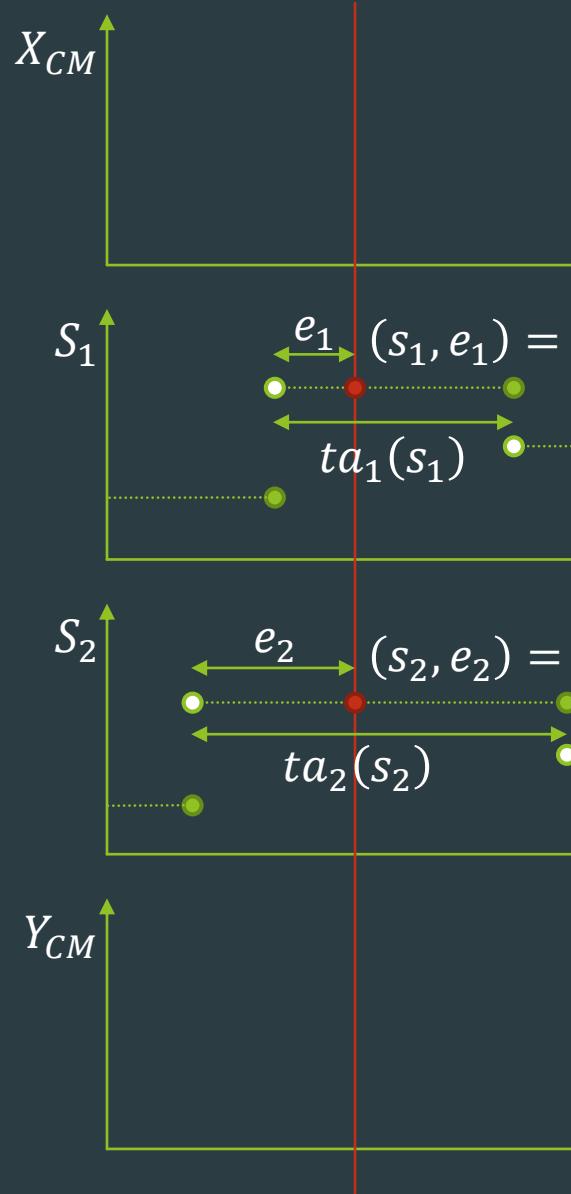


$$flatten(CM) = \langle X, Y, S, q_{init}, \delta_{int}, \delta_{ext}, \lambda, ta \rangle$$

$$S = \times_{i \in D} Q_i$$

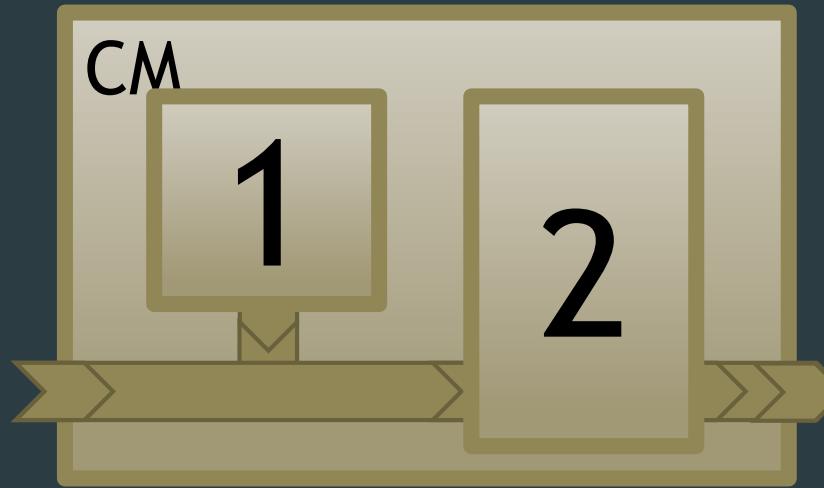
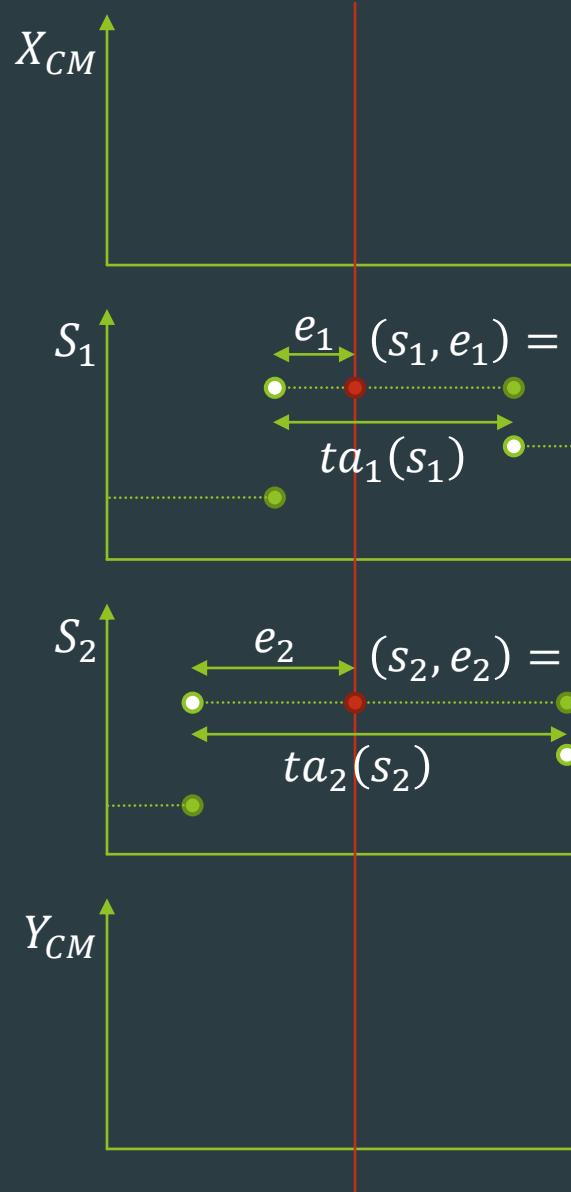


$$flatten(CM) = \langle X, Y, S, q_{init}, \delta_{int}, \delta_{ext}, \lambda, ta \rangle$$



$$flatten(CM) = \langle X, Y, S, q_{init}, \delta_{int}, \delta_{ext}, \lambda, ta \rangle$$

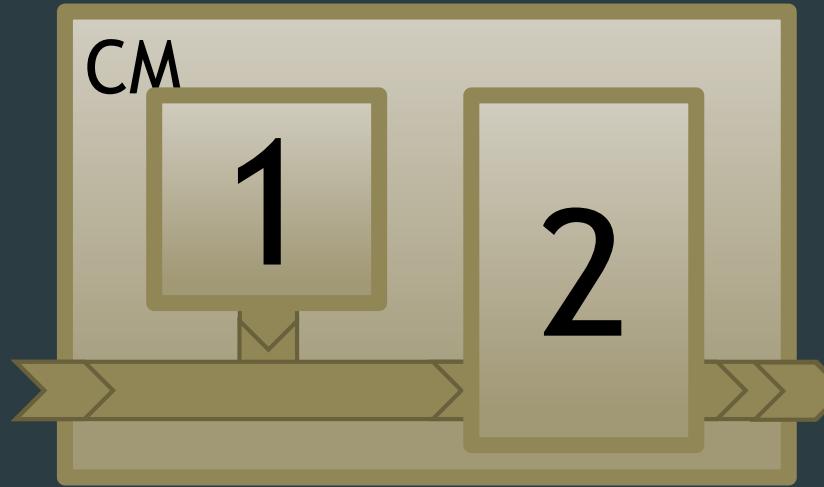
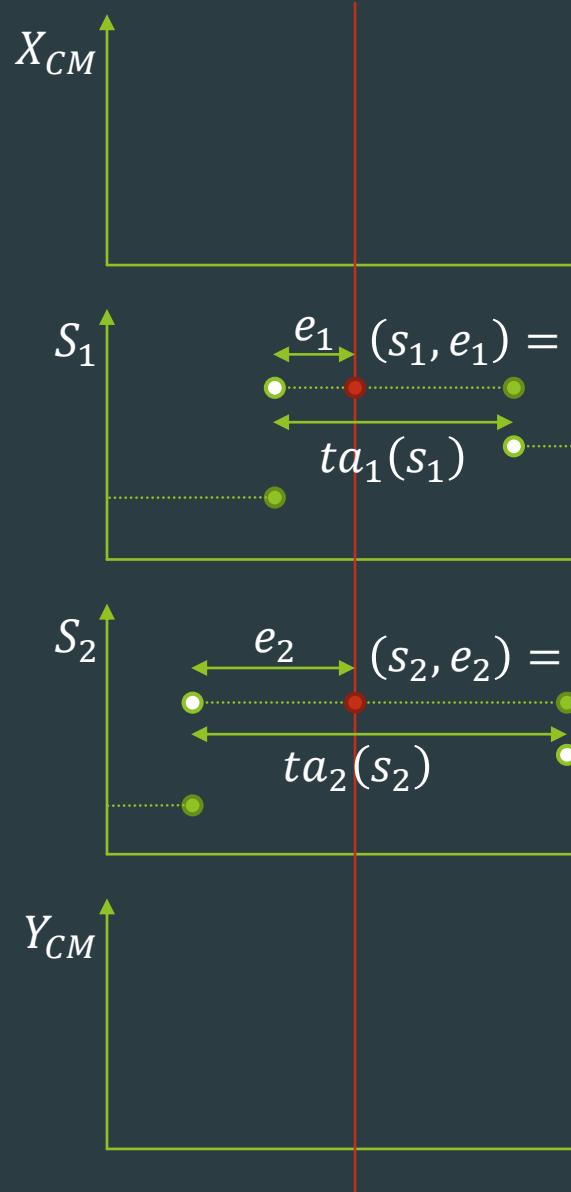
$$q_{init} = (s_{init}, e_{init})$$



$flatten(CM) = \langle X, Y, S, q_{init}, \delta_{int}, \delta_{ext}, \lambda, ta \rangle$

$$q_{init} = (s_{init}, e_{init})$$

$$s_{init} = (\dots, (s_{init,i}, e_{init,i} - e_{init}), \dots)$$

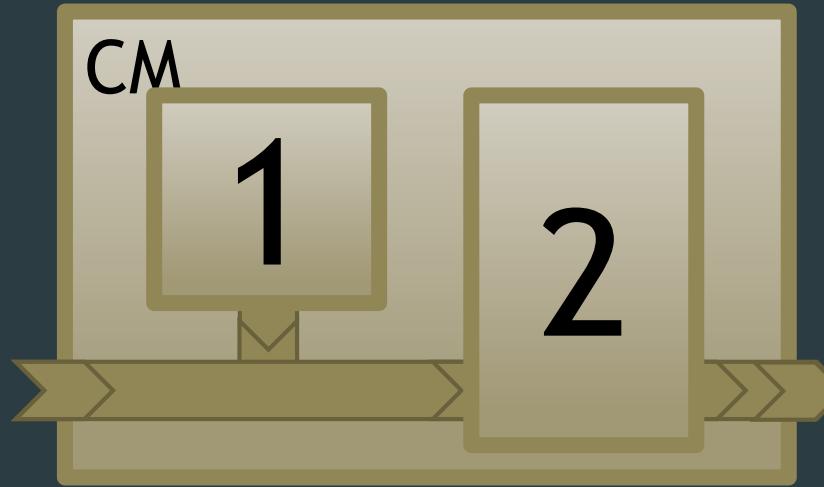
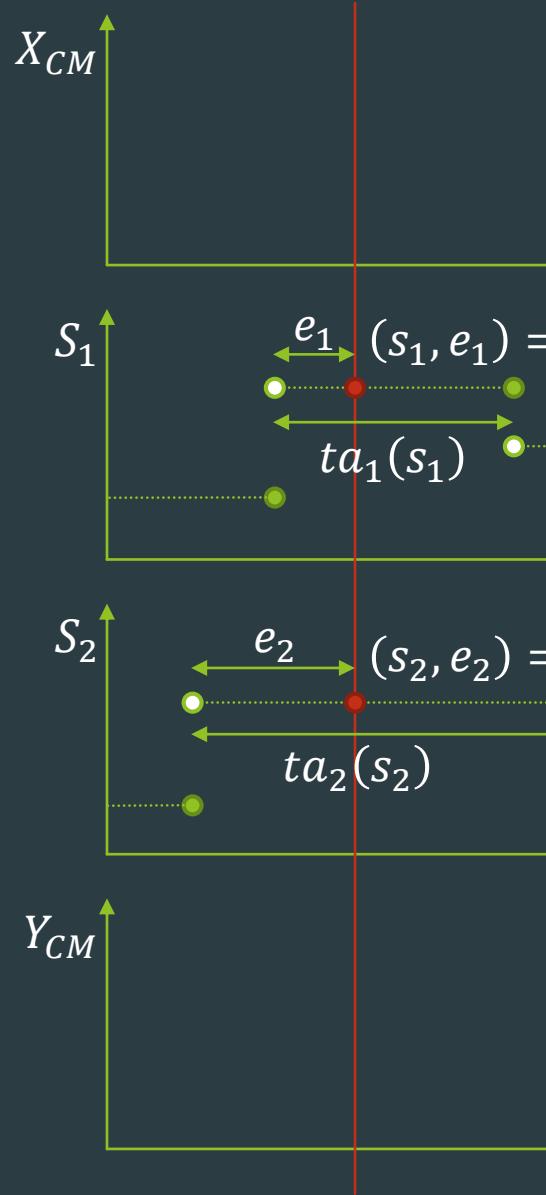


$flatten(CM) = \langle X, Y, S, q_{init}, \delta_{int}, \delta_{ext}, \lambda, ta \rangle$

$$q_{init} = (s_{init}, e_{init})$$

$$s_{init} = (\dots, (s_{init,i}, e_{init,i} - e_{init}), \dots)$$

$$e_{init} = \min_{i \in D} \{e_{init,i}\}$$



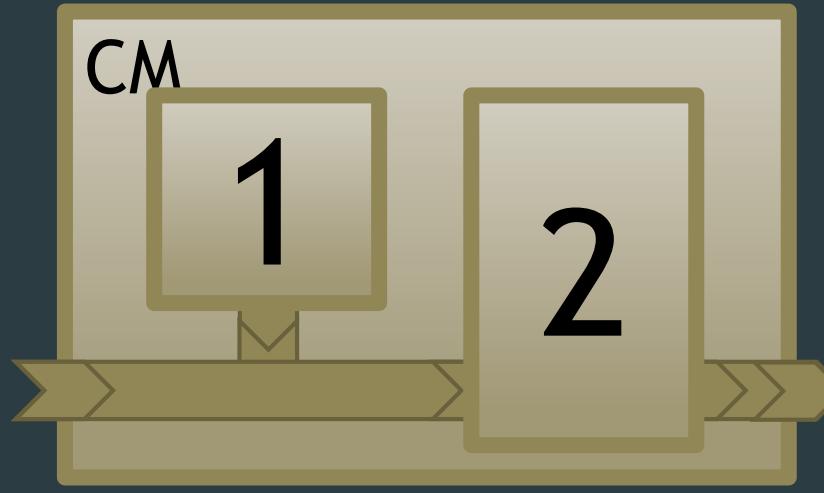
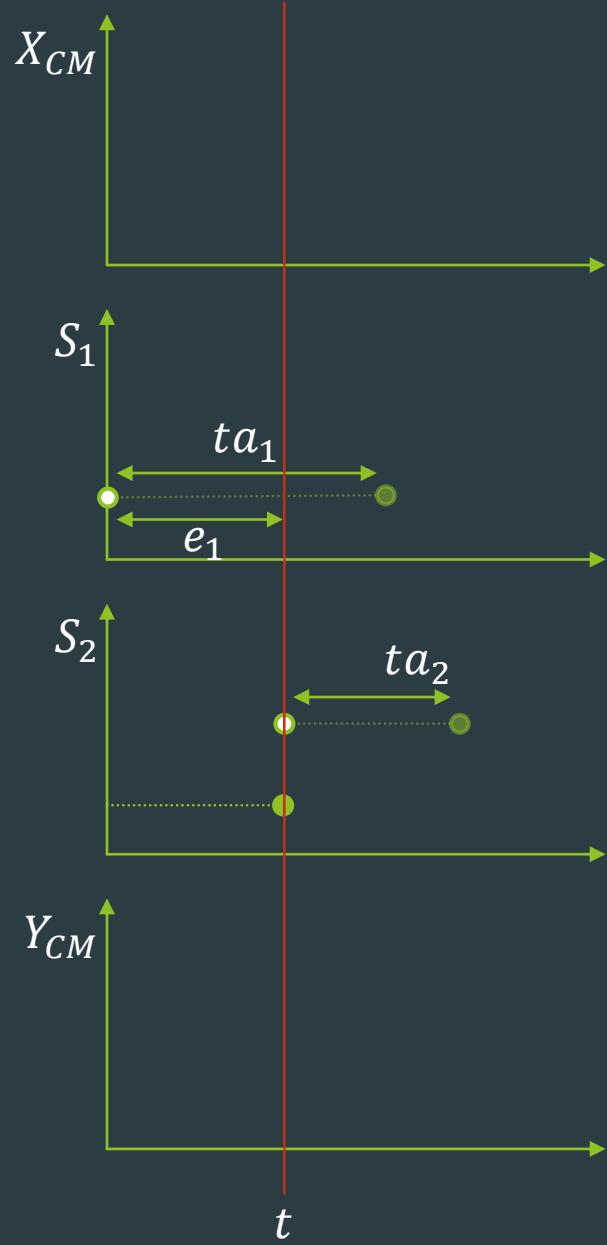
$$flatten(CM) = \langle X, Y, S, q_{init}, \delta_{int}, \delta_{ext}, \lambda, ta \rangle$$

$$q_{init} = (s_{init}, e_{init})$$

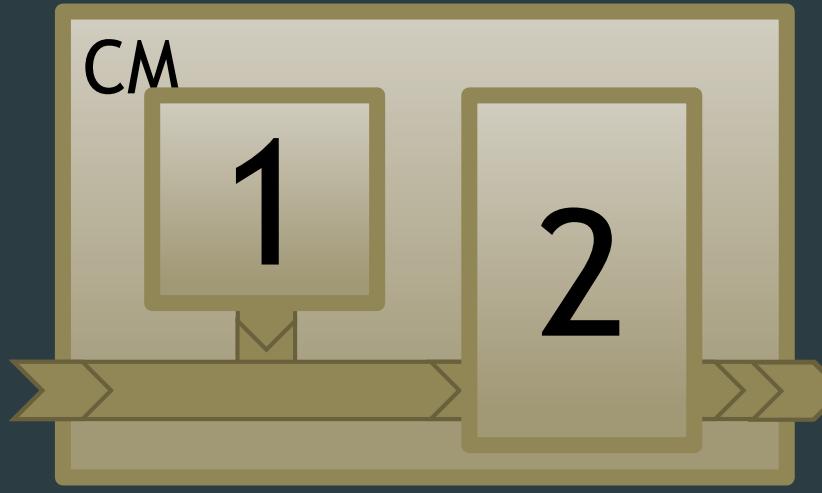
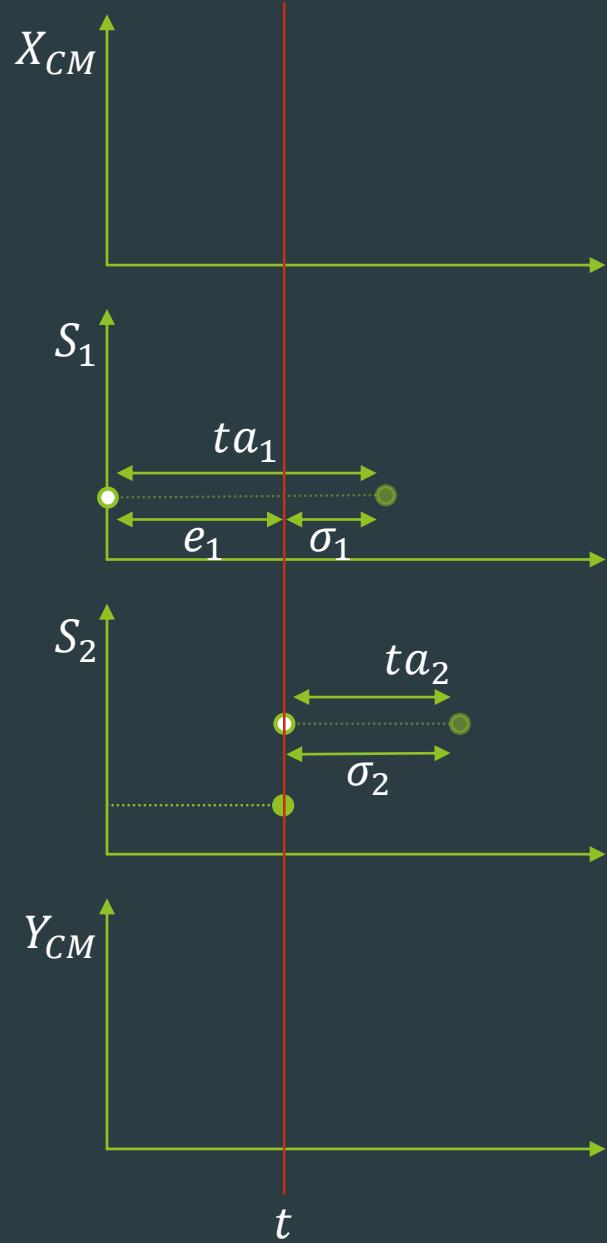
$$s_{init} = (\dots, (s_{init,i}, e_{init,i} - e_{init}), \dots)$$

$$e_{init} = \min_{i \in D} \{e_{init,i}\}$$

$$(s_{init,i}, e_{init,i}) = q_{init,i}$$

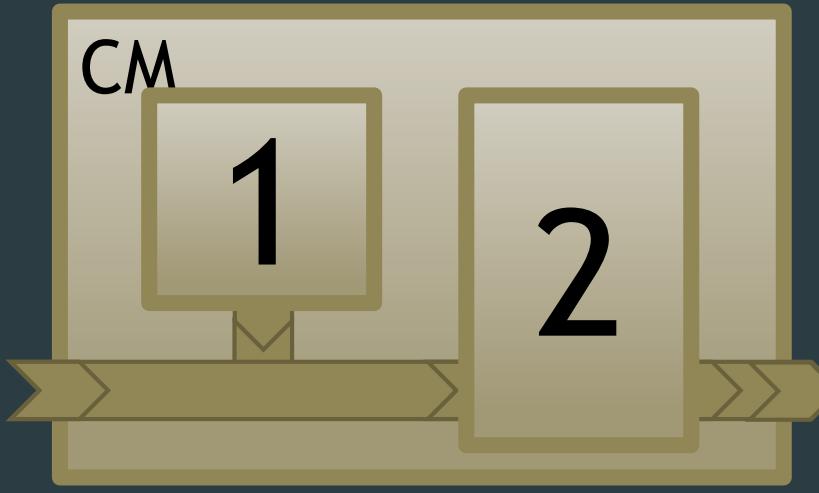
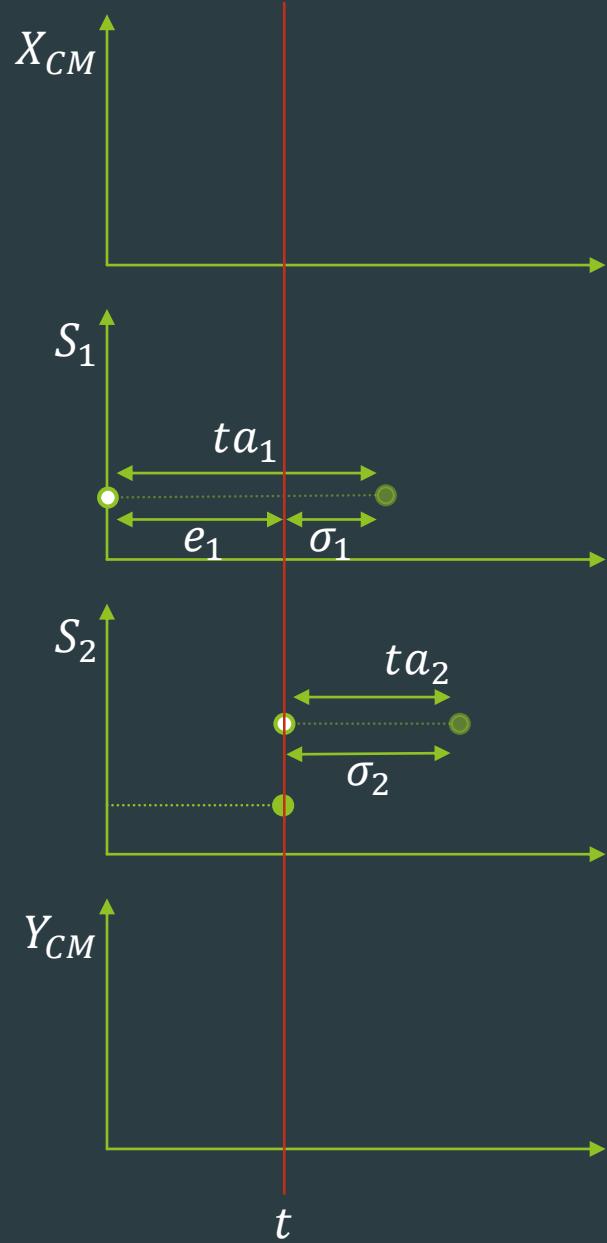


$flatten(CM) = \langle X, Y, S, q_{init}, \delta_{int}, \delta_{ext}, \lambda, ta \rangle$



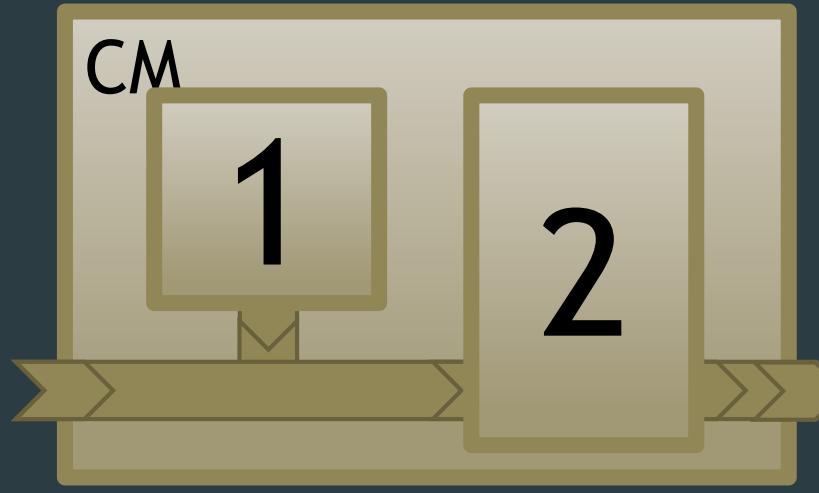
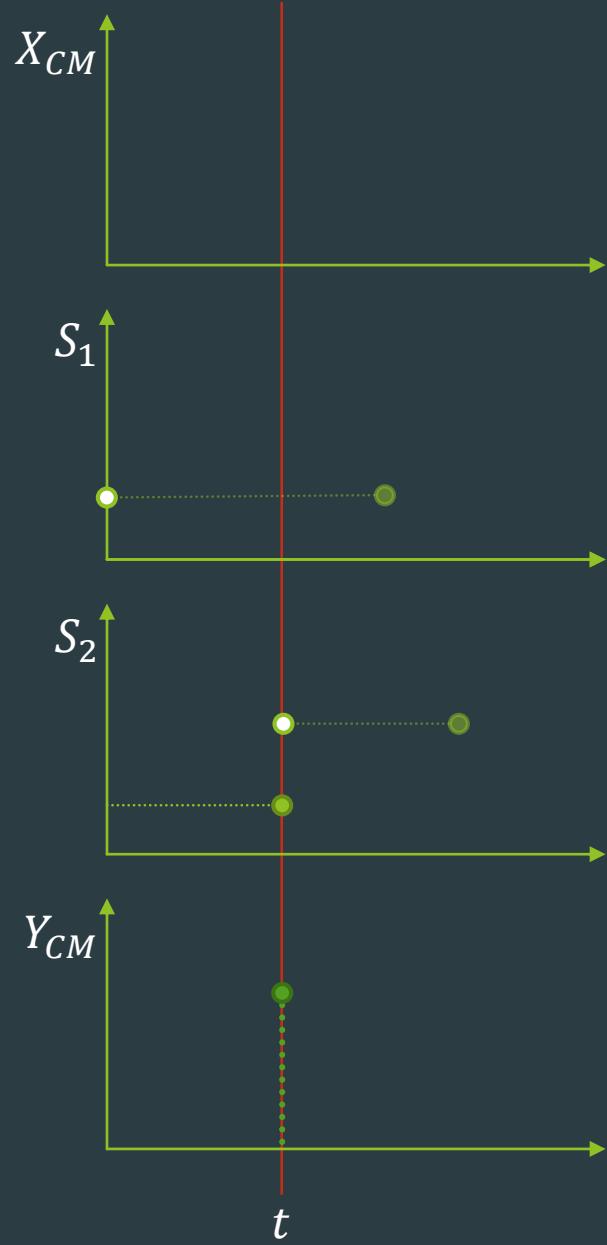
$$flatten(CM) = \langle X, Y, S, q_{init}, \delta_{int}, \delta_{ext}, \lambda, ta \rangle$$

$$\begin{aligned} ta : S &\rightarrow \mathbb{R}_{0,+\infty}^+ \\ ta(s) &= \min_{i \in D} \{\sigma_i = ta_i(s_i) - e_i\} \end{aligned}$$

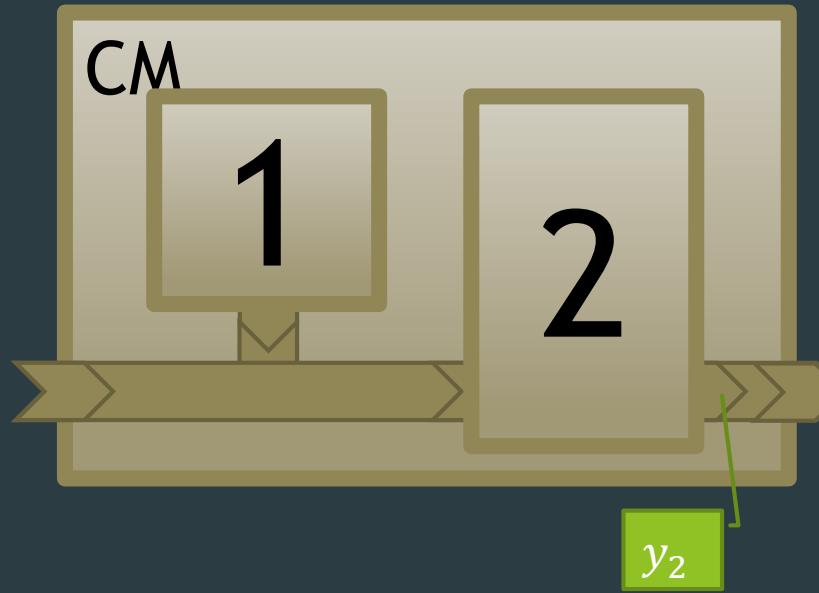
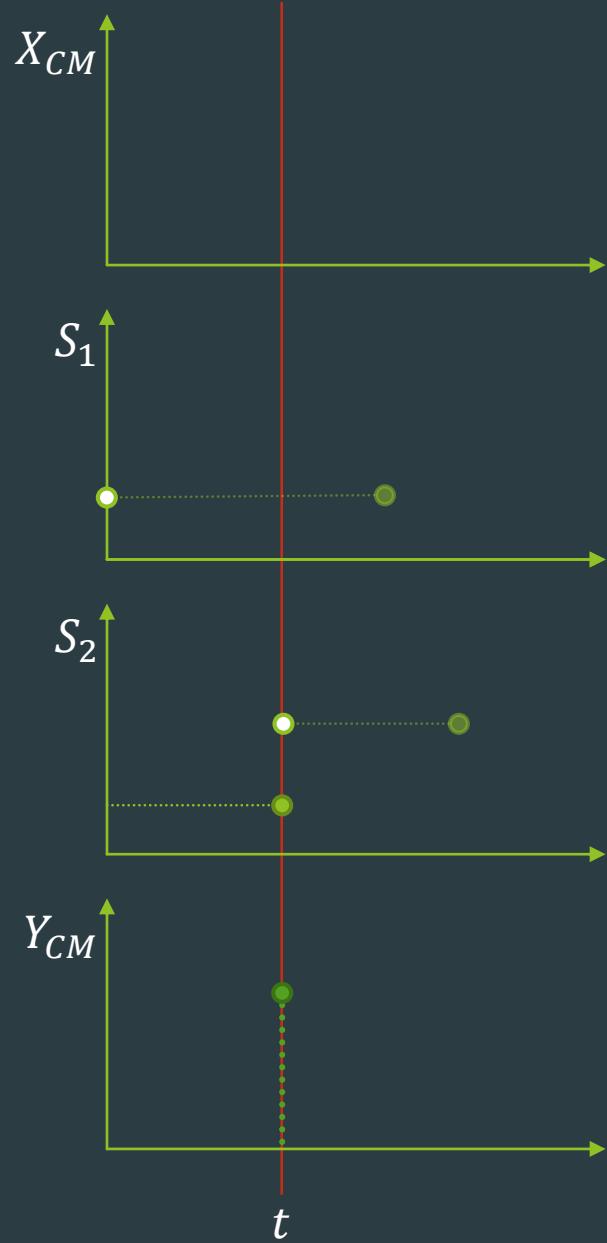


$$flatten(CM) = \langle X, Y, S, q_{init}, \delta_{int}, \delta_{ext}, \lambda, ta \rangle$$

$$\begin{aligned} ta : S &\rightarrow \mathbb{R}_{0,+\infty}^+ \\ ta(s) &= \min_{i \in D} \{\sigma_i = ta_i(s_i) - e_i\} \\ IMM(s) &= \{i \in D \mid \sigma_i = ta(s)\} \\ select(IMM(s)) &= i^* \end{aligned}$$

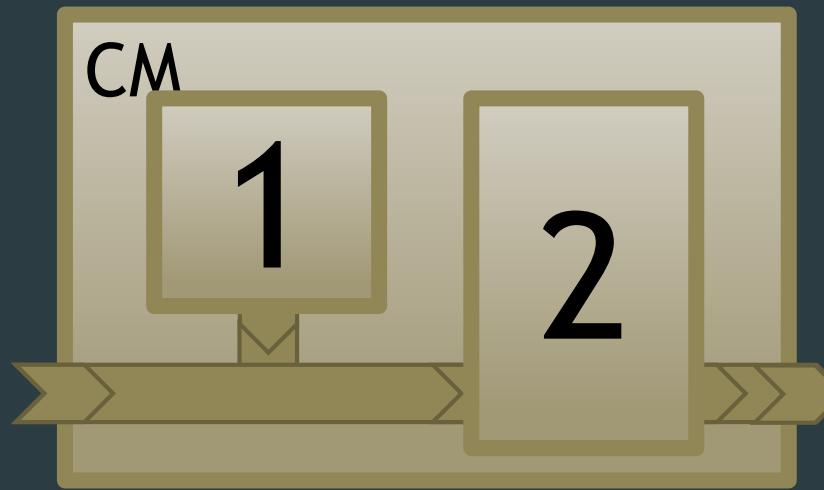
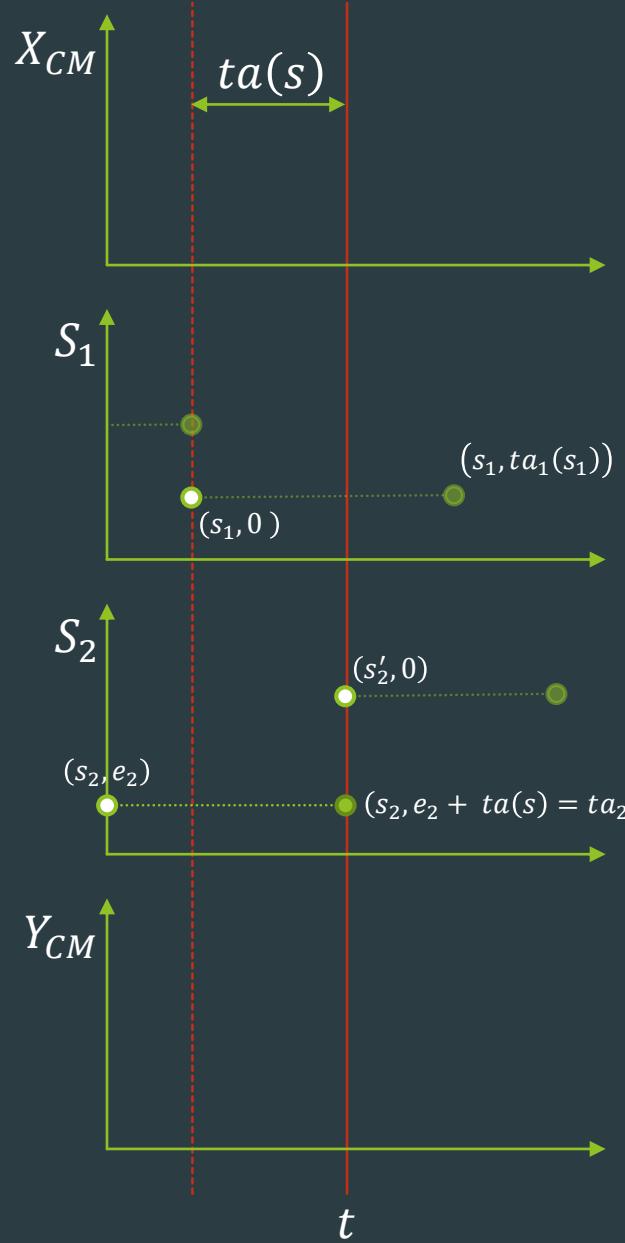


$flatten(CM) = \langle X, Y, S, q_{init}, \delta_{int}, \delta_{ext}, \lambda, ta \rangle$

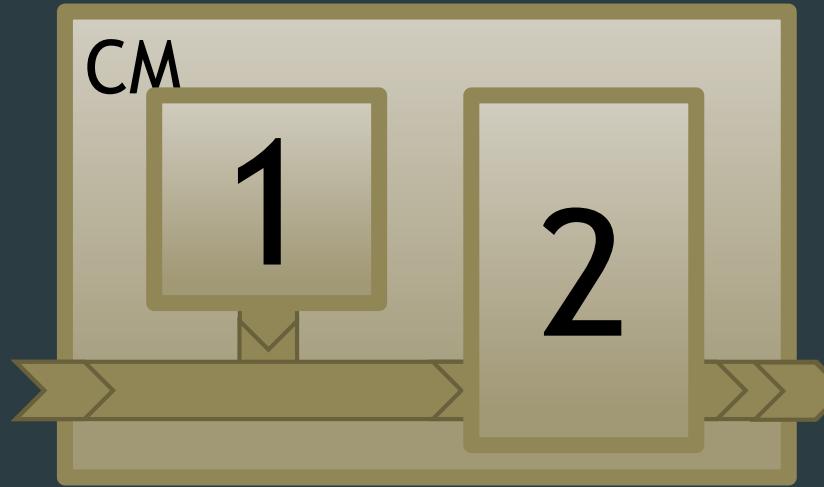
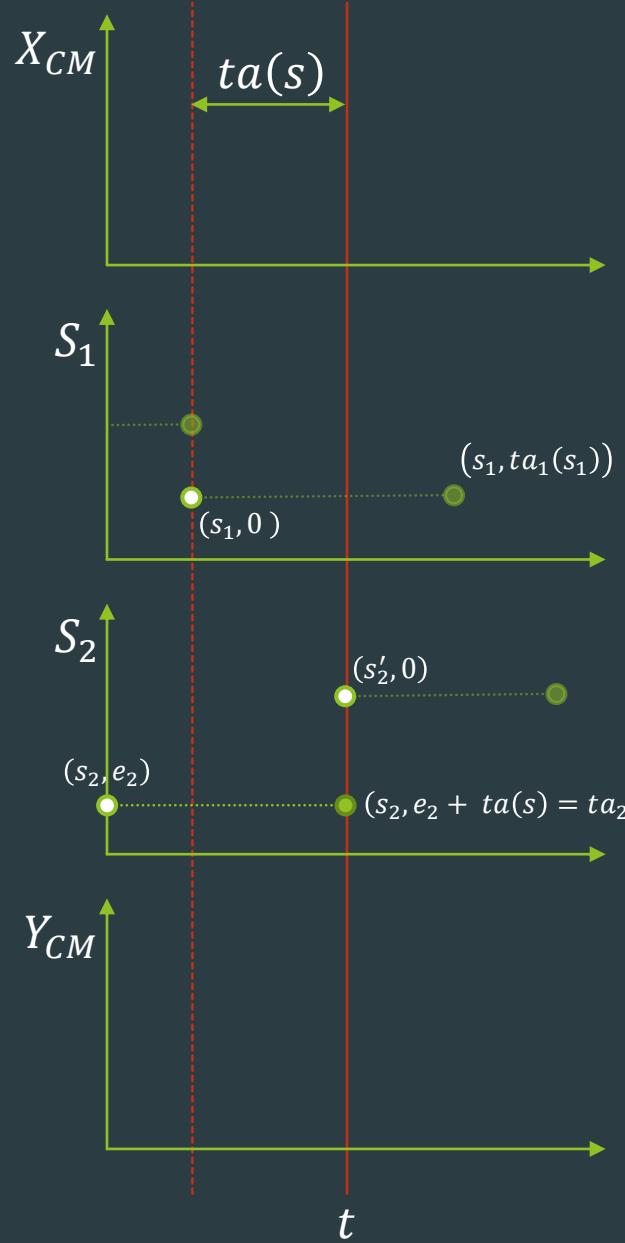


$$flatten(CM) = \langle X, Y, S, q_{init}, \delta_{int}, \delta_{ext}, \lambda, ta \rangle$$

$$\lambda(s) = \begin{cases} Z_{i^*, self}(\lambda_{i^*}(s_{i^*})) & \text{if } self \in I_{i^*} \\ \emptyset & \text{if } self \notin I_{i^*} \end{cases}$$



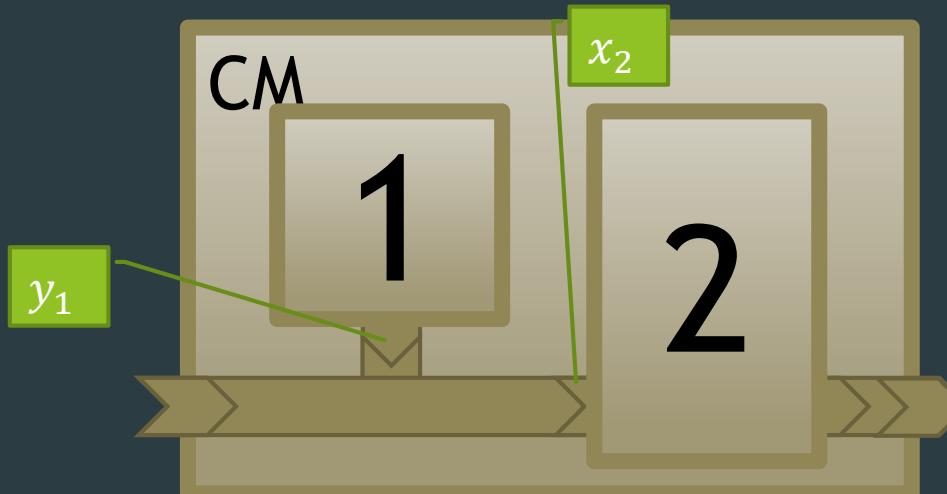
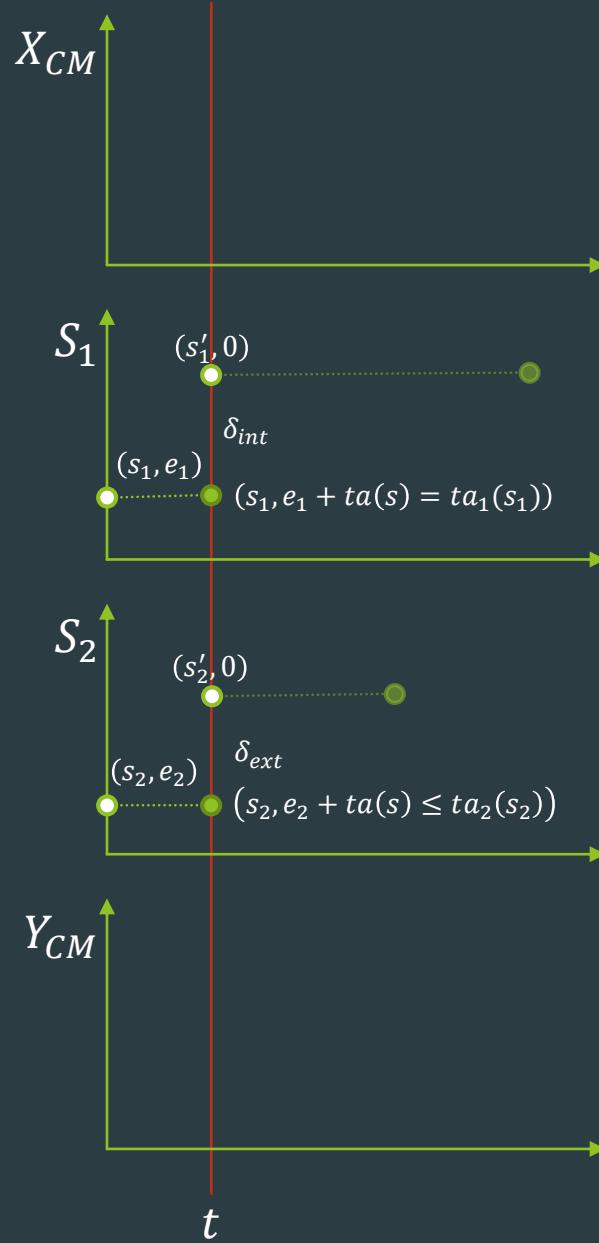
$flatten(CM) = \langle X, Y, S, q_{init}, \delta_{int}, \delta_{ext}, \lambda, ta \rangle$



$$flatten(CM) = \langle X, Y, S, q_{init}, \delta_{int}, \delta_{ext}, \lambda, ta \rangle$$

$$\delta_{int}(s) = (\dots, (s'_j, e'_j), \dots)$$

$$(s'_j, e'_j) = \begin{cases} (\delta_{int,j}(s_j), 0) & \text{for } j = i^* \\ ? & \text{for } j \in I_{i^*} \setminus \{\text{self}\} \\ (s_j, e_j + ta(s)) & \text{else} \end{cases}$$



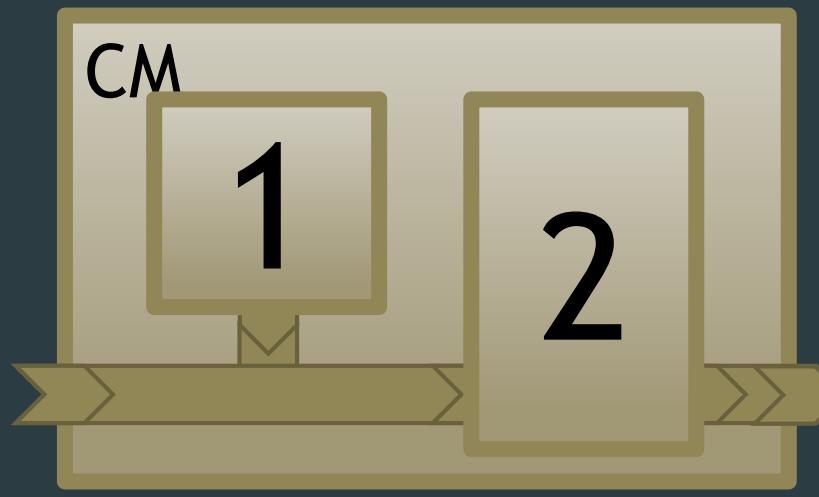
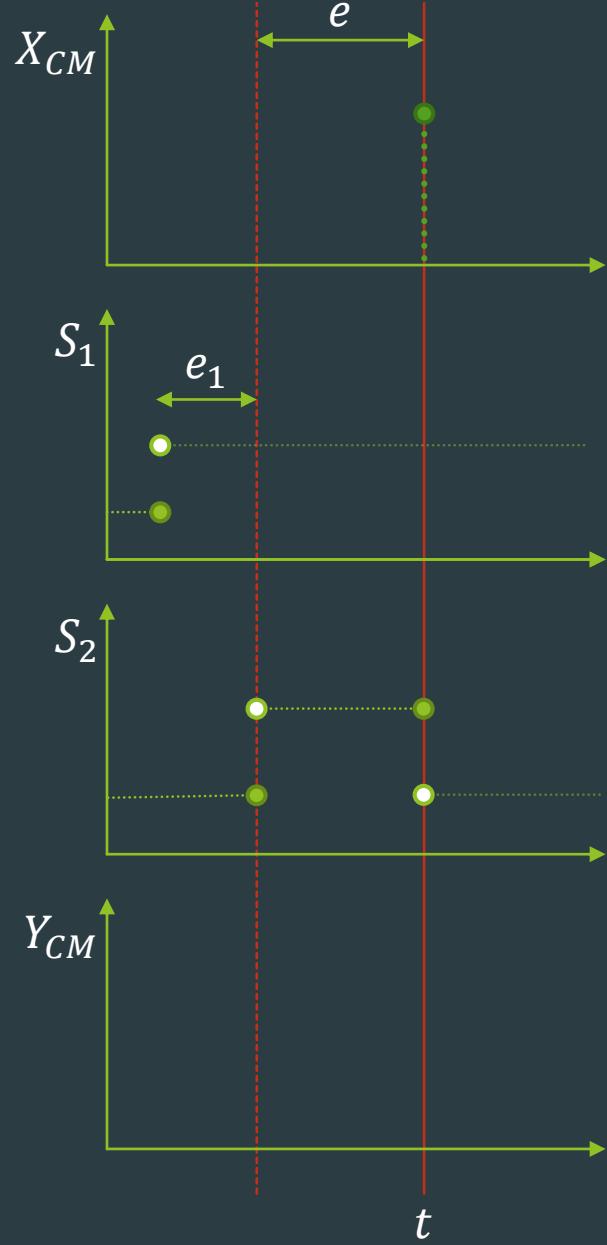
$$flatten(CM) = \langle X, Y, S, q_{init}, \delta_{int}, \delta_{ext}, \lambda, ta \rangle$$

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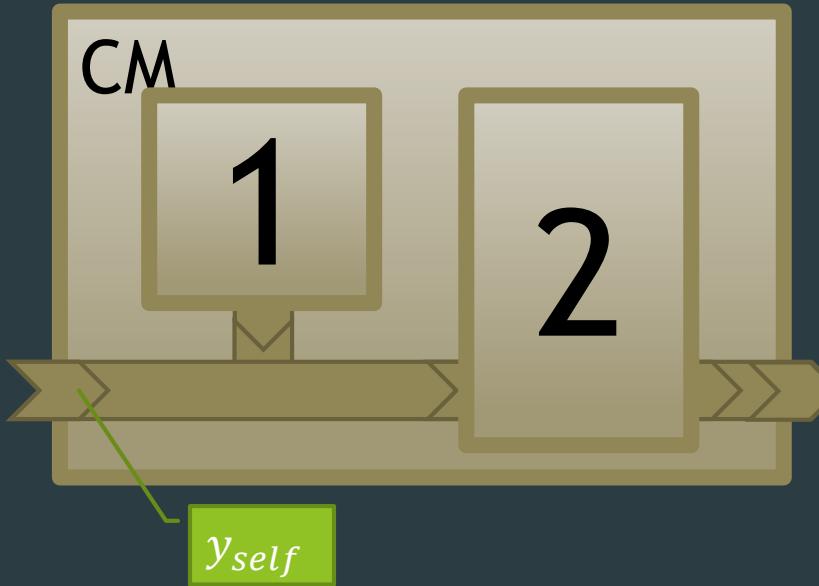
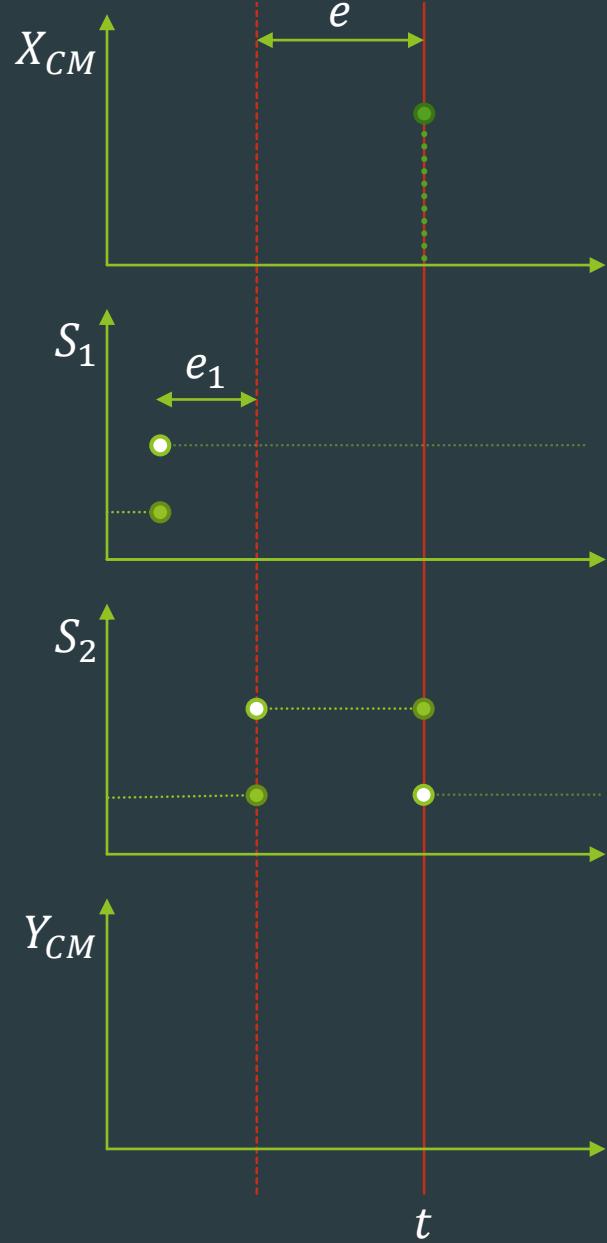
$$(\delta_{int,j}(s_j), 0)$$

for  $j = i^*$

$$(s'_j, e'_j) = \begin{cases} \left( \delta_{ext,j} \left( (s_j, e_j + ta(s)), Z_{i^*,j}(\lambda_{i^*}(s_{i^*})) \right), 0 \right) & \text{for } j \in I_{i^*} \setminus \{\text{self}\} \\ (s_j, e_j + ta(s)) & \text{else} \end{cases}$$



$$flatten(CM) = \langle X, Y, S, q_{init}, \delta_{int}, \delta_{ext}, \lambda, ta \rangle$$



$$flatten(CM) = \langle X, Y, S, q_{init}, \delta_{int}, \delta_{ext}, \lambda, ta \rangle$$

$$\delta_{ext}((s, e), x) = (\dots, (s'_i, e'_i), \dots)$$

$$(s'_i, e'_i) = \begin{cases} \left( \delta_{ext,i} \left( (s_i, e_i + e), Z_{self,i}(x) \right), 0 \right) & \text{for } i \in I_{self} \\ (s_i, e_i + e) & \text{else} \end{cases}$$

$$flatten(CM) = \langle X, Y, S, q_{init}, \delta_{int}, \delta_{ext}, \lambda, ta \rangle$$

$$X = X_{CM}$$

$$Y = Y_{CM}$$

$$S = \times_{i \in D} Q_i$$

$$Q = \{(s, e) | s \in S, 0 \leq e \leq ta(s)\}$$

$$q_{init} = (s_{init}, e_{init}) \in Q$$

$$s_{init} = (\dots, (s_{init,i}, e_{init,i} - e_{init}), \dots)$$

$$e_{init} = \min_{i \in D} \{e_{init,i}\}$$

$$(s_{init,i}, e_{init,i}) = q_{init,i}$$

$$\delta_{int}(s) = (\dots, (s'_j, e'_j), \dots)$$

$$(s'_j, e'_j) = \begin{cases} (\delta_{int,j}(s_j), 0) & \text{for } j = i^* \\ \left( \delta_{ext,j} \left( (s_j, e_j + ta(s)), Z_{i^*,j}(\lambda_{i^*}(s_{i^*})) \right), 0 \right) & \text{for } j \in I_{i^*} \\ (s_j, e_j + ta(s)) & \text{else} \end{cases}$$

$$\delta_{ext}((s, e), x) = (\dots, (s'_i, e'_i), \dots)$$

$$(s'_i, e'_i) = \begin{cases} \left( \delta_{ext,i} \left( (s_i, e_i + e), Z_{self,i}(x) \right), 0 \right) & \text{for } i \in I_{self} \\ (s_i, e_i + e) & \text{else} \end{cases}$$

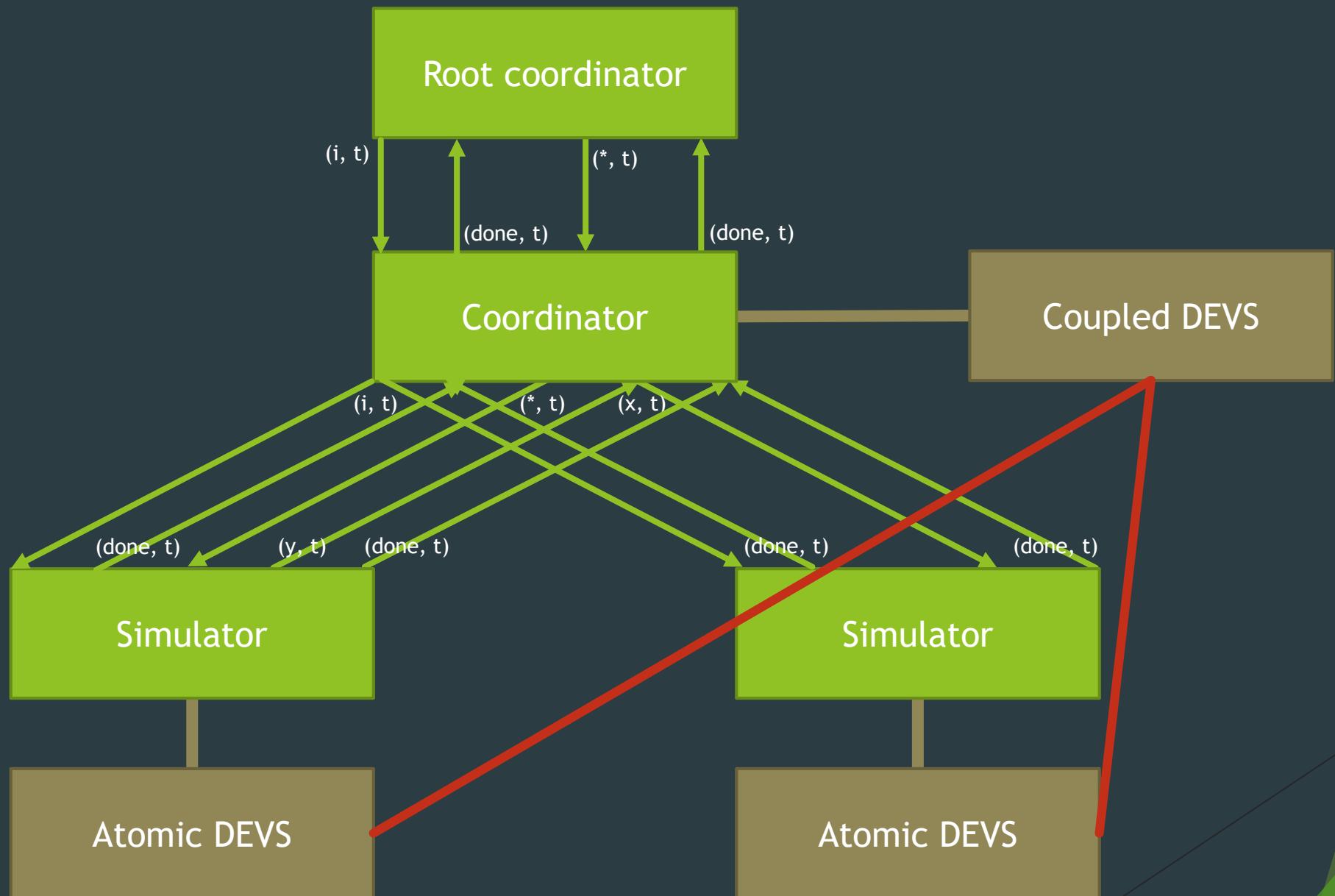
$$\lambda(s) = \begin{cases} Z_{i^*,self}(\lambda_{i^*}(s_{i^*})) & \text{if } self \in I_{i^*} \\ \phi & \text{if } self \notin I_{i^*} \end{cases}$$

$$i^* = select(IMM(s))$$

$$IMM(s) = \{i \in D | \sigma_i = ta(s)\}$$

$$ta(s) = \min_{i \in D} \{\sigma_i = ta_i(s_i) - e_i\}$$

# Hierarchical Simulator



message $m$	simulator	coordinator
$(*, from, t)$	simulator correct only if $t = t_N$	
$y \leftarrow \lambda(s)$		<b>send</b> $(*, self, t)$ to $i^*$ , where
<b>if</b> $y \neq \phi$ :		$i^* = select(imm\_children)$
	<b>send</b> $(\lambda(s), self, t)$ to parent	$imm\_children = \{i \in D \mid M_i.t_N = t\}$
$s \leftarrow \delta_{int}(s)$		$active\_children \leftarrow active\_children \cup \{i^*\}$
$t_L \leftarrow t$		
$t_N \leftarrow t_L + ta(s)$		
<b>send</b> $(done, self, t_N)$ to parent		

---

<b>message</b> $m$	<b>simulator</b>	<b>coordinator</b>
$(x, from, t)$	simulator correct only if $t_L \leq t \leq t_N$ (ignore $\delta_{int}$ to resolve a $t = t_N$ conflict)	
$e \leftarrow t - t_L$		$\forall i \in I_{self} :$
$s \leftarrow \delta_{ext}(s, e, x)$		<b>send</b> $(Z_{self,i}(x), self, t)$ to $i$
$t_L \leftarrow t$		$active\_children \leftarrow active\_children \cup \{i\}$
$t_N \leftarrow t_L + ta(s)$		
<b>send</b> $(done, self, t_N)$ to parent		

---

---

message $m$	simulator	coordinator
$(y, from, t)$		$\forall i \in I_{from} \setminus \{self\} :$ <b>send</b> $(Z_{from,i}(y), from, t)$ to $i$ $active\_children \leftarrow active\_children \cup \{i\}$ <b>if</b> $self \in I_{from} :$ <b>send</b> $(Z_{from,self}(y), self, t)$ to $parent$
$(done, from, t)$		$active\_children \leftarrow active\_children \setminus \{from\}$ <b>if</b> $active\_children = \emptyset :$ $t_L \leftarrow t$ $t_N \leftarrow \min\{M_i.t_N   i \in D\}$ <b>send</b> $(done, self, t_N)$ to $parent$

---

---

$t \leftarrow t_N$  of topmost coordinator

**repeat until**  $t \geq t_{end}$  (or some other termination condition)

**send**  $(*, \text{main}, t)$  to topmost coupled model *top*

**wait** for  $(done, \text{top}, t_N)$

$t \leftarrow t_N$

---

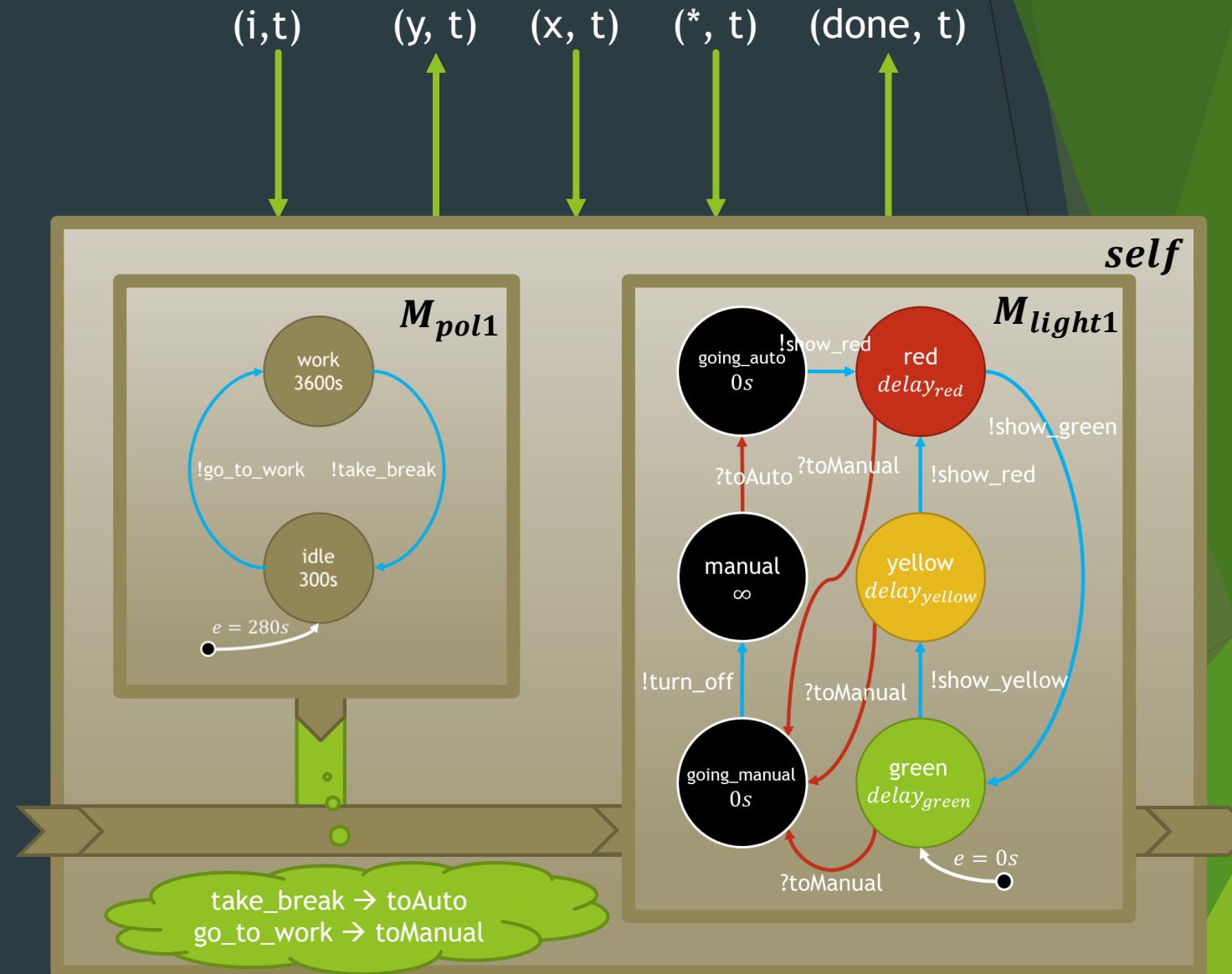
# DEVS Semantics

	Operational Semantics	Denotational Semantics
Atomic DEVS	Abstract Simulator	[1]
Coupled DEVS	Hierarchical Simulator	Closure under Coupling

[1] Ashvin Radiya and Robert G. Sargent. A logic-based foundation of discrete event modeling and simulation. ACM Transactions on Modeling and Computer Simulation, 1(1):3-51, 1994.

# Conclusions

- ▶ Atomic DEVS
- ▶ Coupled DEVS
- ▶ Closure under coupling
- ▶ Abstract Simulator



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# Examples

A small *trafficModel* and corresponding *trafficExperiment* file is included in the *examples* folder of the PyPDEVS distribution. This (completely working) example is slightly too big to use as a first introduction to PyPDEVS and therefore this page will start with a very simple example.

For this, we will first introduce a simplified queue model, which will be used as the basis of all our examples. The complete model can be downloaded: [`queue\_example\_classic.py`](#).

This section should provide you with all necessary information to get you started with creating your very own PyPDEVS simulation. More advanced features are presented in the next section.

## Generator

Somewhat simpler than a queue even, is a generator. It will simply create a message to send after a certain delay and then it will stop doing anything.

Informally, this would result in a DEVS specification as:

- Time advance function returns the waiting time to generate the message, infinity after

# Limitations of Classic DEVS

- ▶ Parallel implementation
  - ▶ Parallel DEVS [1]
- ▶ Select function is artificial
  - ▶ Parallel DEVS [1]
- ▶ Dynamic Structure systems
  - ▶ Dynamic Structure DEVS [2]

[1] A.C.-H. Chow. Parallel DEVS: A parallel, hierarchical, modular modeling formalism and its distributed simulator. *Transactions of the Society for Computer Simulation International*, 13(2):55-68, 1996.

[2] F. Barros. The dynamic structure discrete event system specification formalism. *Transactions of the Society for Computer Simulation International*, 13(1):35-46, 1996.

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Real-time

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Verification

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<http://msdl.cs.mcgill.ca/projects/PythonPDEVS>