



# Agent-Based Modelling and Simulation

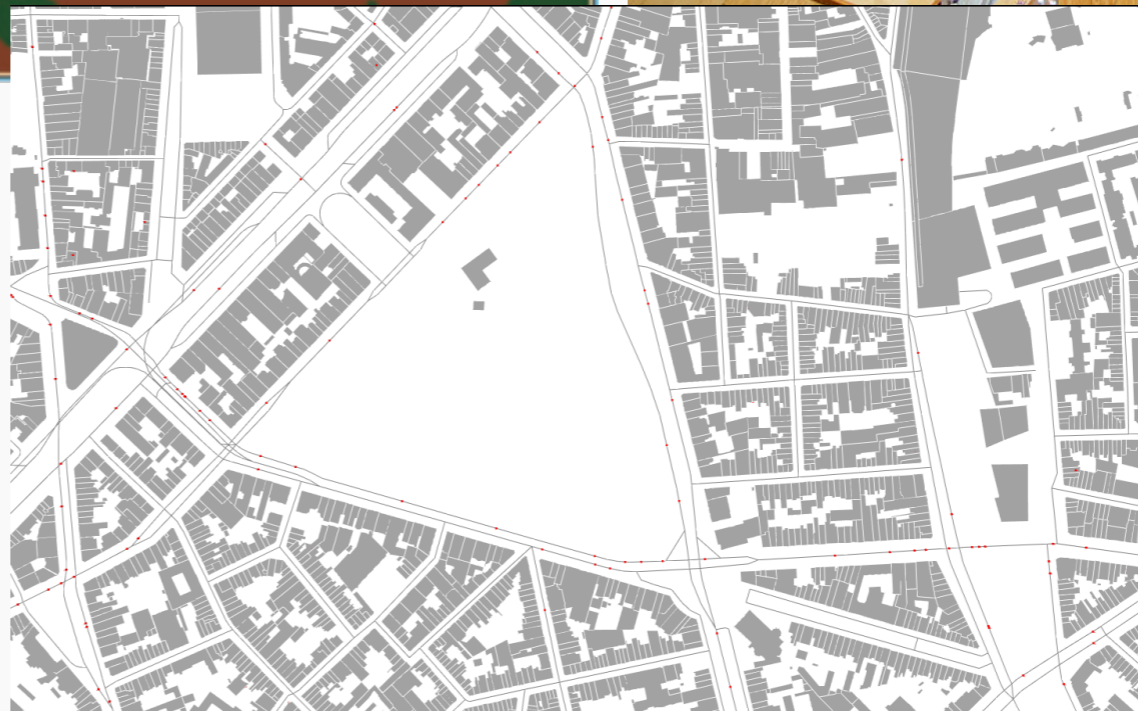
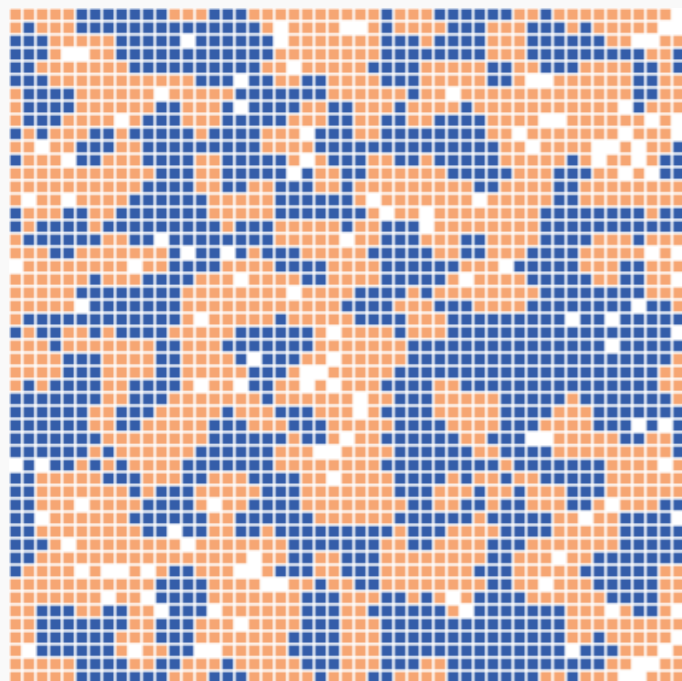
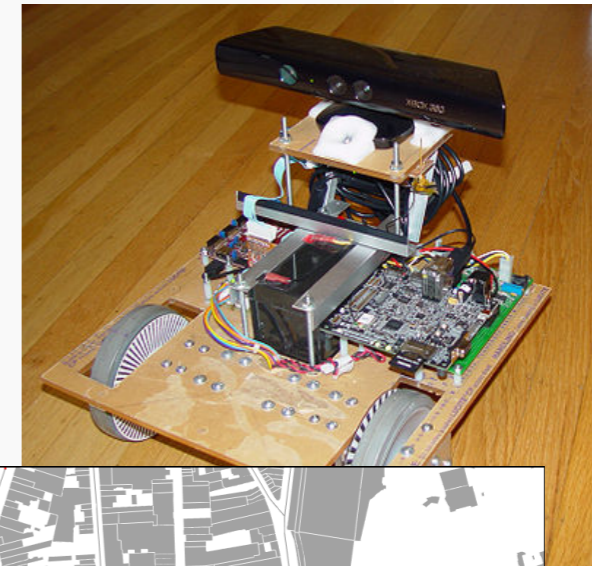
# Introduction

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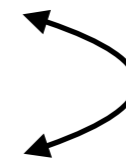
# Agent Paradigm

The agent paradigm is a collection of *concepts* used to tackle *behaviour* of Distributed, Situated, Interacting, Autonomous and Reactive Systems (agents) with Dynamic structure



## Views over agent concepts:

- Programming paradigm (Agent-Oriented Programming)
- Modelling paradigm
  - Multi-Agent System (executed on middleware)
  - **Agent-Based Modelling** (simulation)





## Distributed Artificial Intelligence

- Collective problem solving
- Communication via information sharing

## Artificial Life

- Understanding living systems
- Interactions with environment
- Evolution, survival, adaptation, reproduction, learning processes



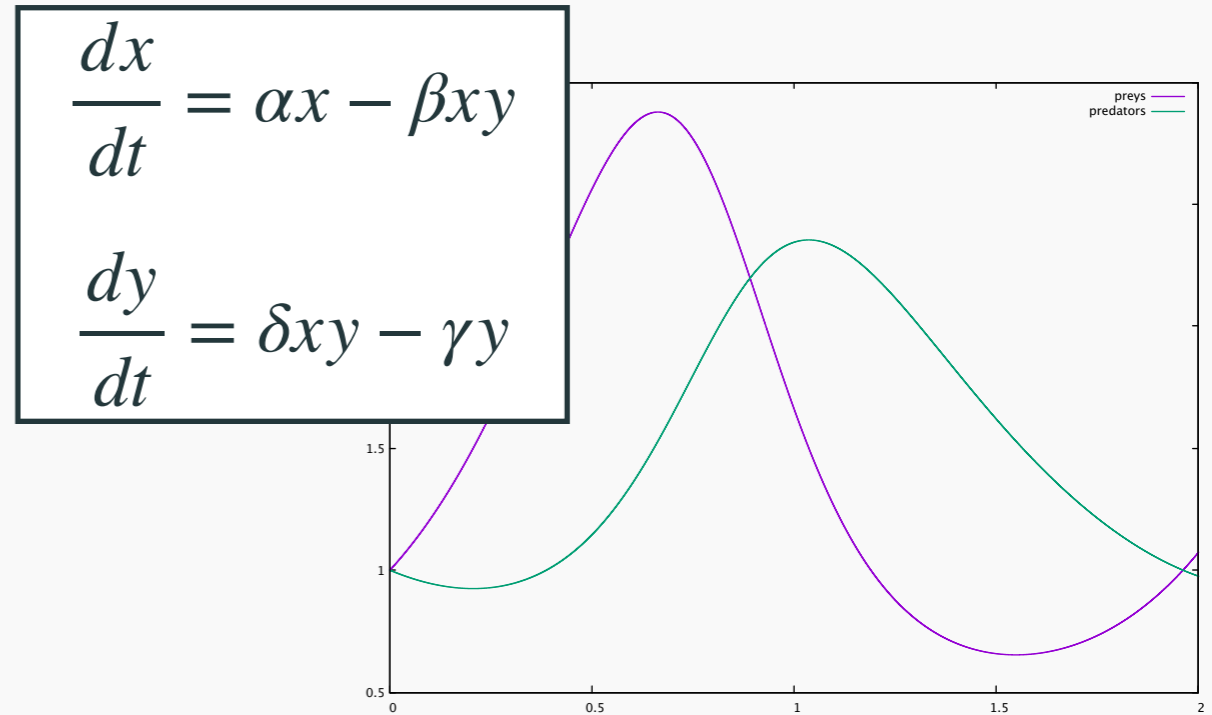
## Multi-Agent Systems

- Design *autonomous and adaptive* agents

# Origins & Why?

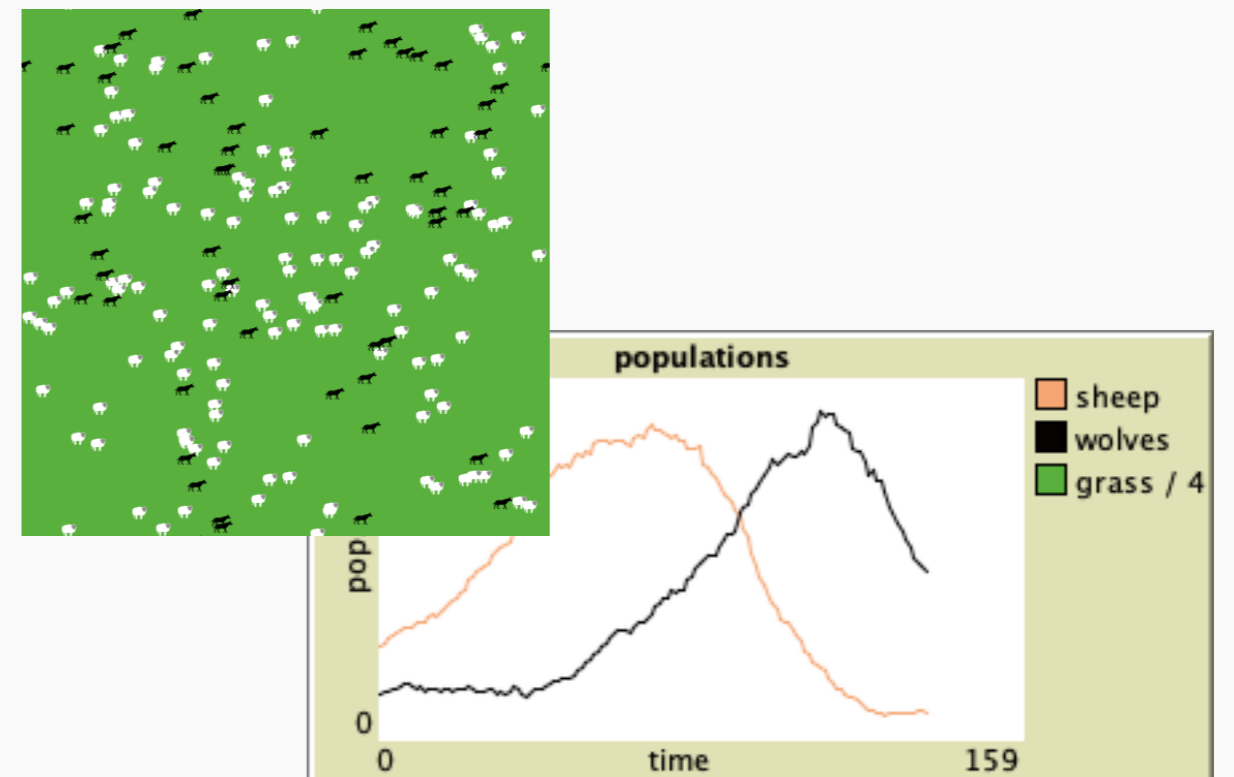
## MACROSCOPIC MODELS

- ODEs
- Monte Carlo simulation
- System Dynamics



## MICROSCOPIC MODELS

- Cellular Automata
- Individual-Based Models
- Agent-Based Models



### When to use ABM?

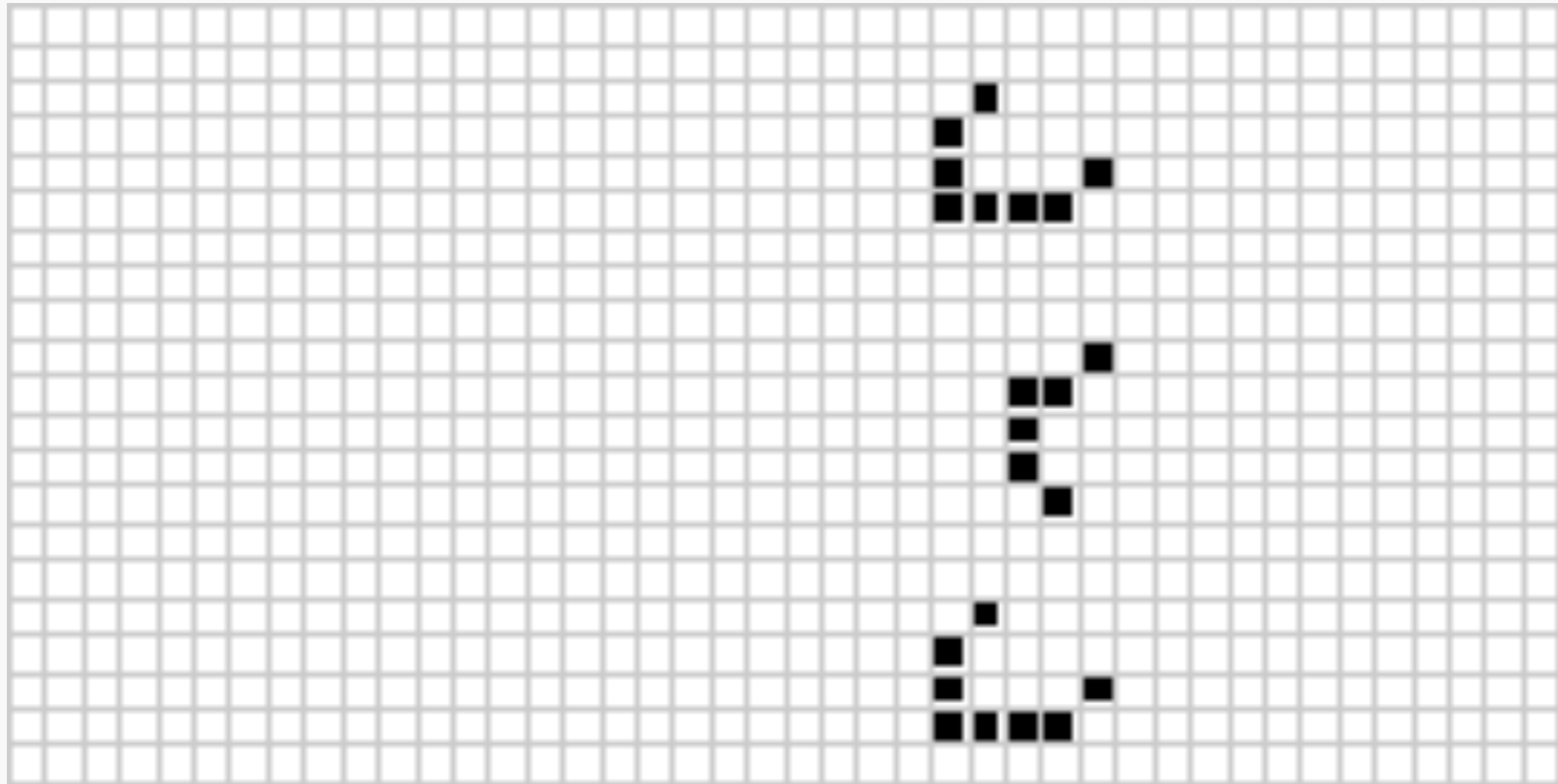
- Medium Numbers
- Heterogeneity
- Complex but Local Interactions
- Rich Environments
- Time
- Adaptation



## Related formalisms

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Idiomatic example: John Conway's Game of Life



$CA = (T, X, Y, \Omega, S, \delta, \lambda)$ , where:

$T = \mathbb{N}$  the discrete time base.

$X$  and  $Y$  the input and output sets, respectively.

$\Omega = \{ \dots, \omega : T \rightarrow X, \dots \}$  the set of input segments ( $\omega$  domain can be  $\subseteq T$ ).

$S = \times_{i \in C} V_i$  the state set, with:

$C = I^D$  the *cell index set* of a  $D$ -dimensional grid indexed by  $I$ , and

$V$  an *homogeneous* value set, such that  $\forall i \in C, V_i = V$ .

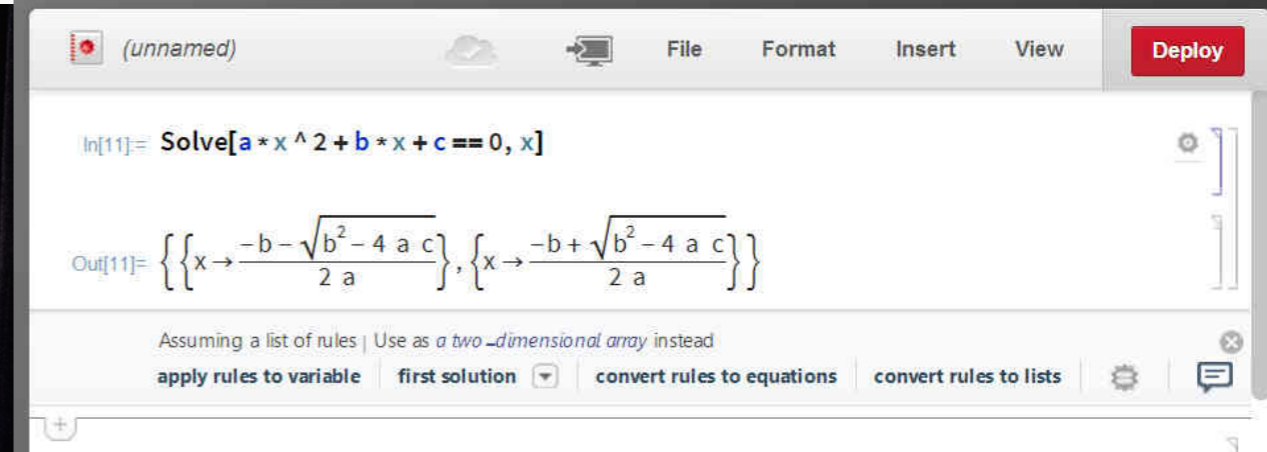
$\delta : \quad \Omega \times S \quad \rightarrow \quad S \quad \text{the total transition function}$

$(\omega_{]n, n+1]}, \times_{i \in C} v(i)) \mapsto \times_{i \in C} \delta_i(i)$

$\lambda : S \rightarrow Y$  the output function, where  $Y$  has a similar structure to  $S$ .



## Universal Cellular Automata



Physica 10D (1984) 1–35  
North-Holland, Amsterdam

### UNIVERSALITY AND COMPLEXITY IN CELLULAR AUTOMATA

Stephen WOLFRAM\*

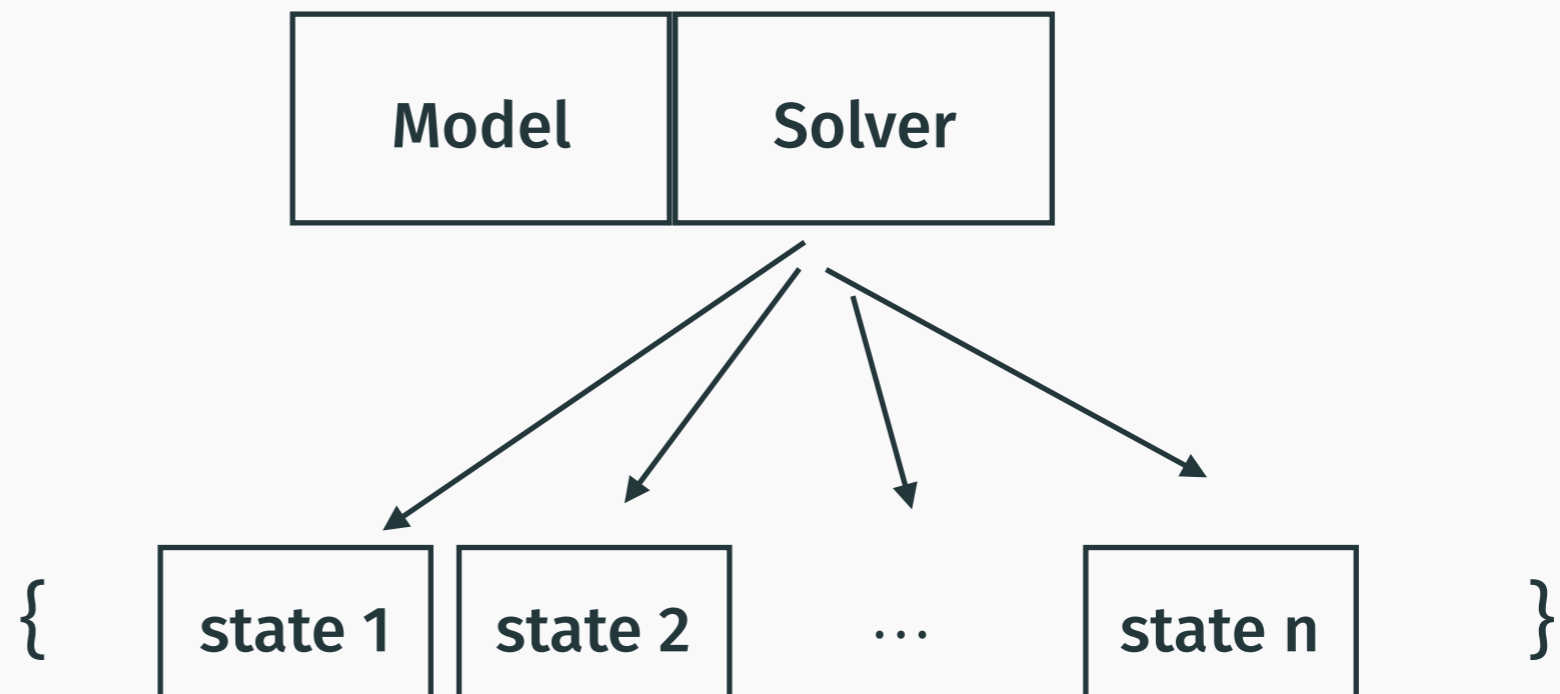
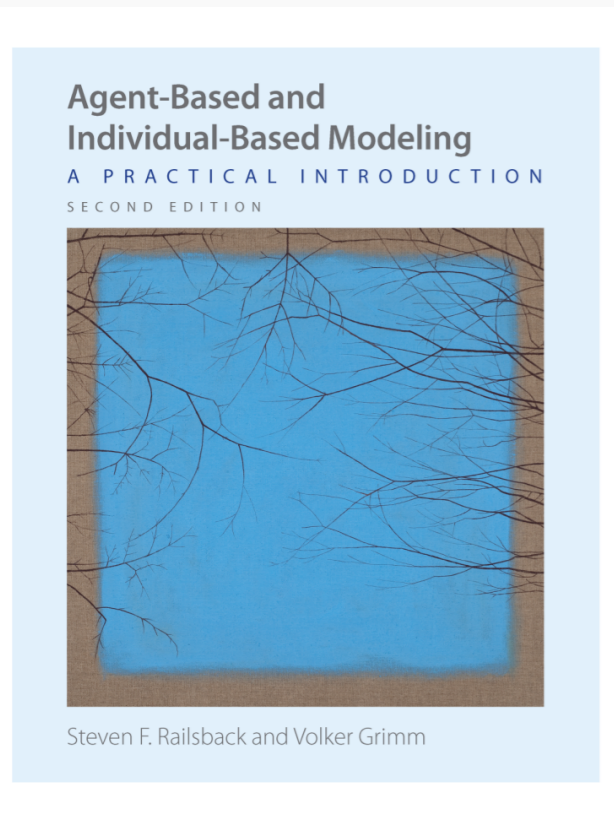
*The Institute for Advanced Study, Princeton NJ 08540, USA*

Cellular automata are discrete dynamical systems with simple construction but complex self-organizing behaviour. Evidence is presented that all one-dimensional cellular automata fall into four distinct universality classes. Characterizations of the structures generated in these classes are discussed. Three classes exhibit behaviour analogous to limit points, limit cycles and chaotic attractors. The fourth class is probably capable of universal computation, so that properties of its infinite time behaviour are undecidable.

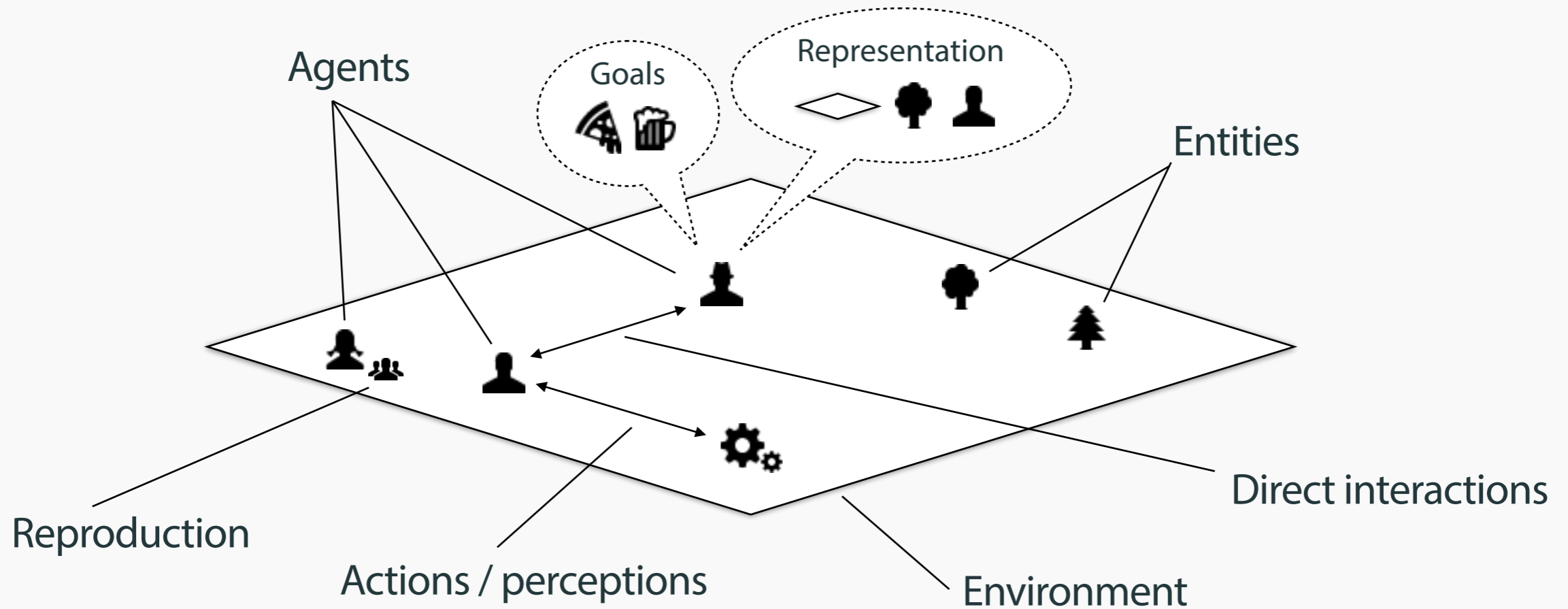
# Individual-Based Modelling

## Individual as the main modelling entity

- Set of equations modelling behaviour
- 1 state = 1 entity
- Allow variability in the population
- Evolved over time to ABM-like



# Agent-Based Modelling







GAMA



COmmon pool Resources  
and Multi-Agent Simulations



M A S O N

# Agent

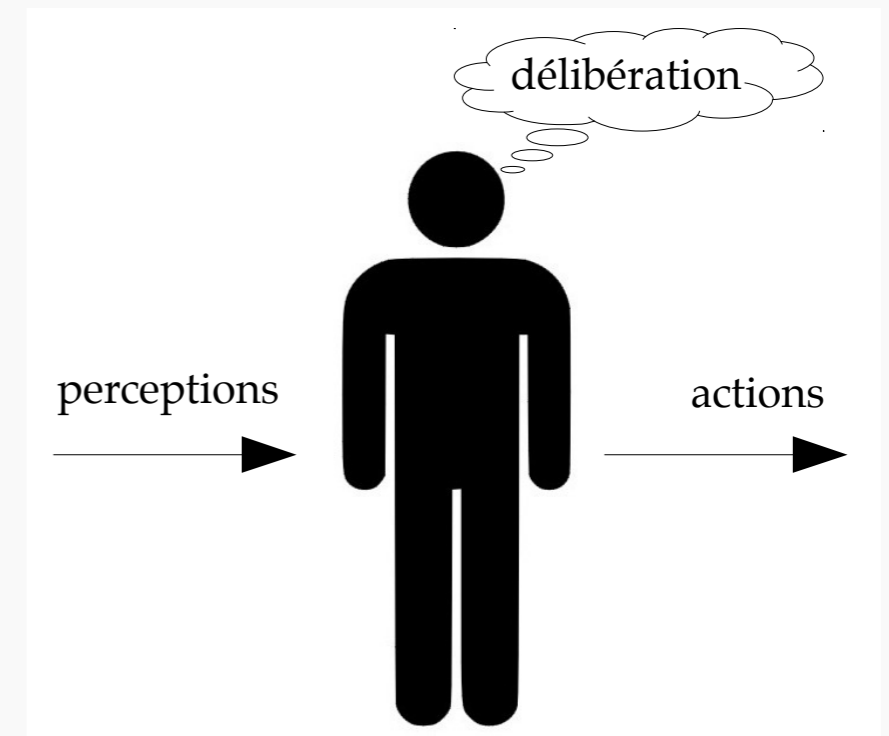
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## Properties

- Autonomous
- Social
- Reactive
- Proactive

## Two visions of intelligence:

- Cognitive
- Reactive



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<b>Agent type</b>	<b>Properties</b>
<i>Entity</i>	<i>Acts upon the environment</i>
Tropistic (purely reactive)	Perceive, acts
Hysteretic (reactive with state)	Perceive, memorise, acts
Reasoning	Perceive, memorise, reasons, acts

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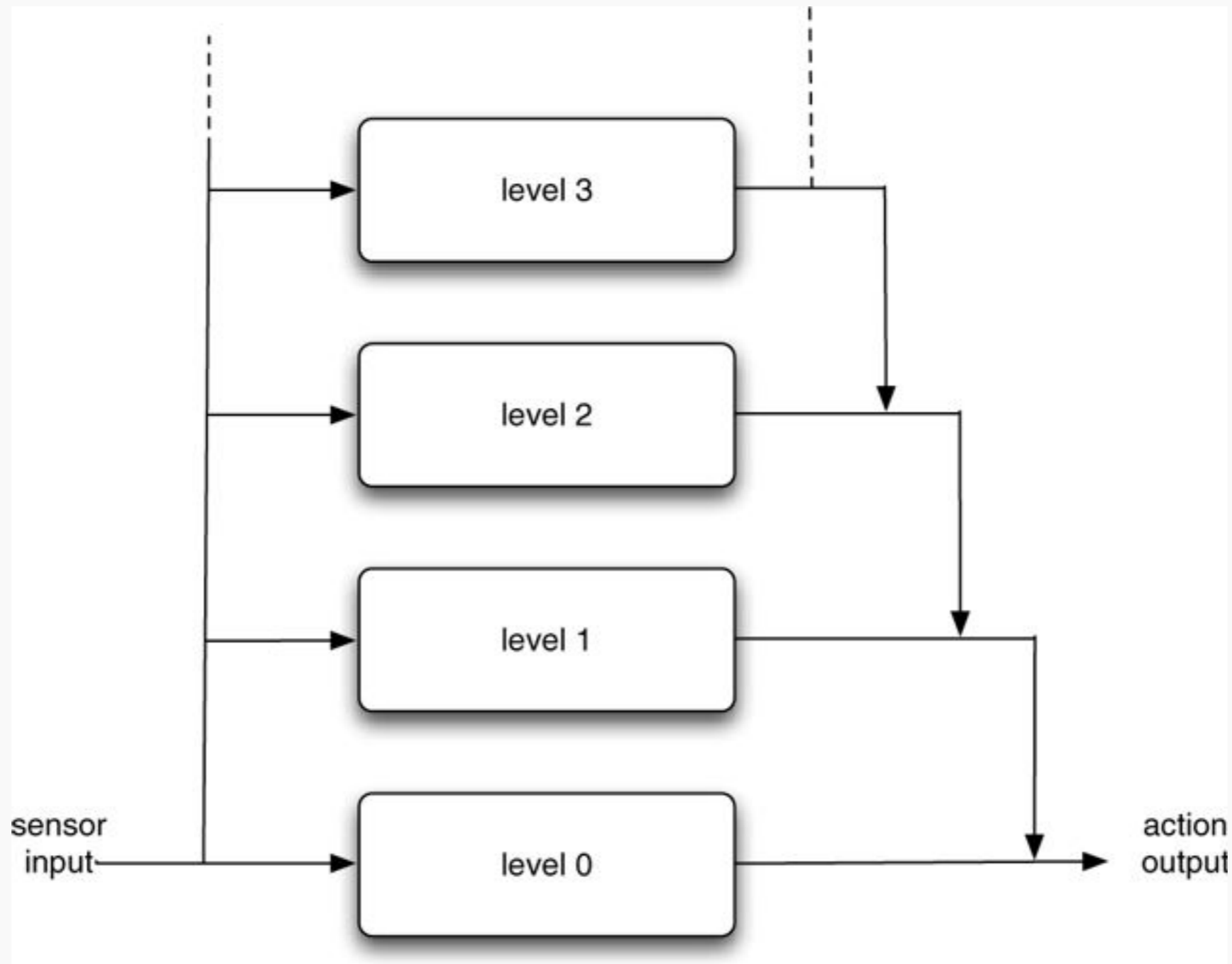
## Reactive agents (tropistic and hysteretic) architectures :

- Subsumption
- Situated automata
- Agent network architecture

## Reasoning agents :

- Logical deduction
- Belief - Desire - Intention

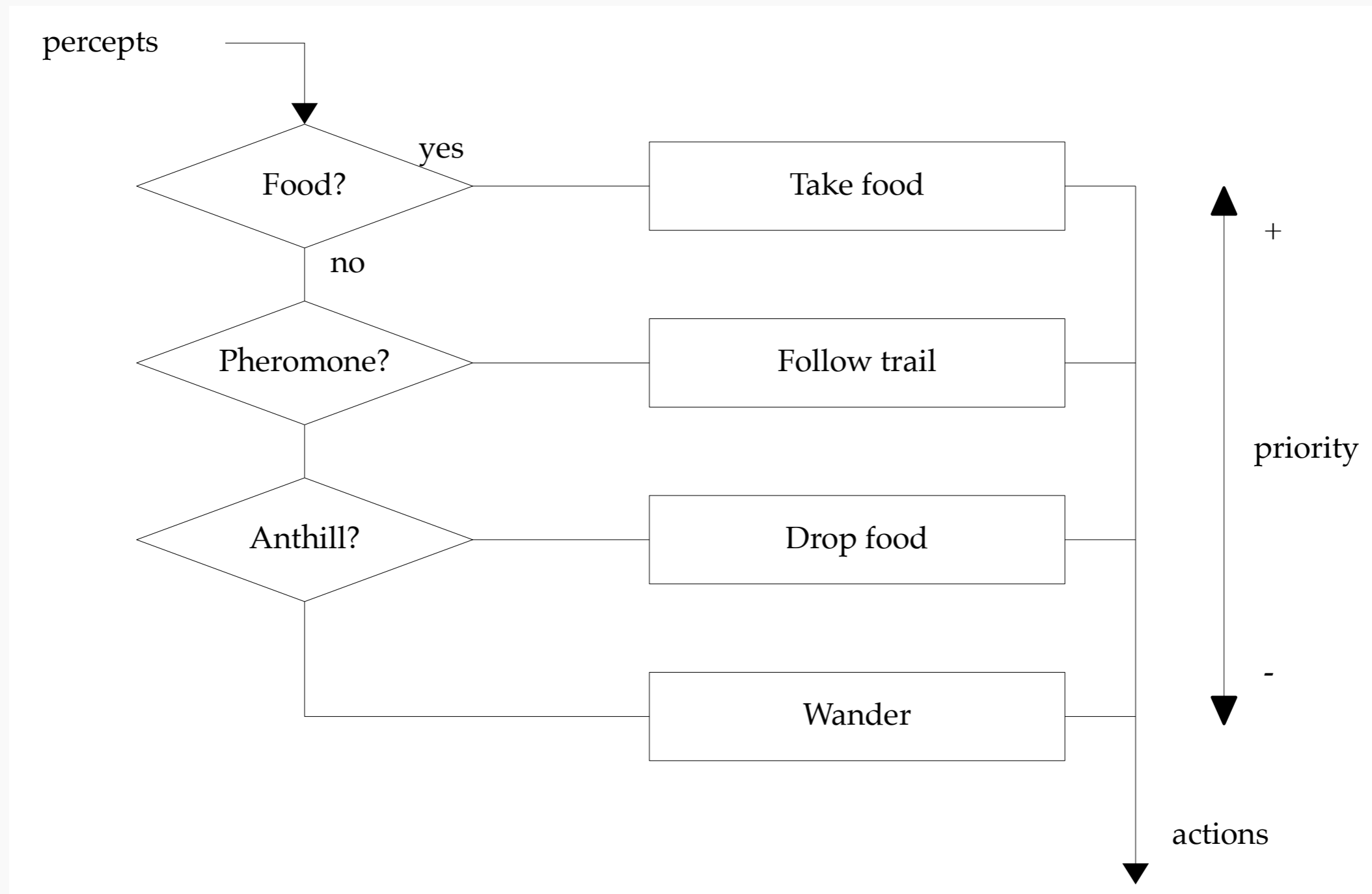
## Subsumption architecture



Brooks, Rodney A. 1991. "Intelligence without Representation." *Artificial Intelligence* 47 (1-3): 139-59. [https://doi.org/10.1016/0004-3702\(91\)90053-M](https://doi.org/10.1016/0004-3702(91)90053-M).



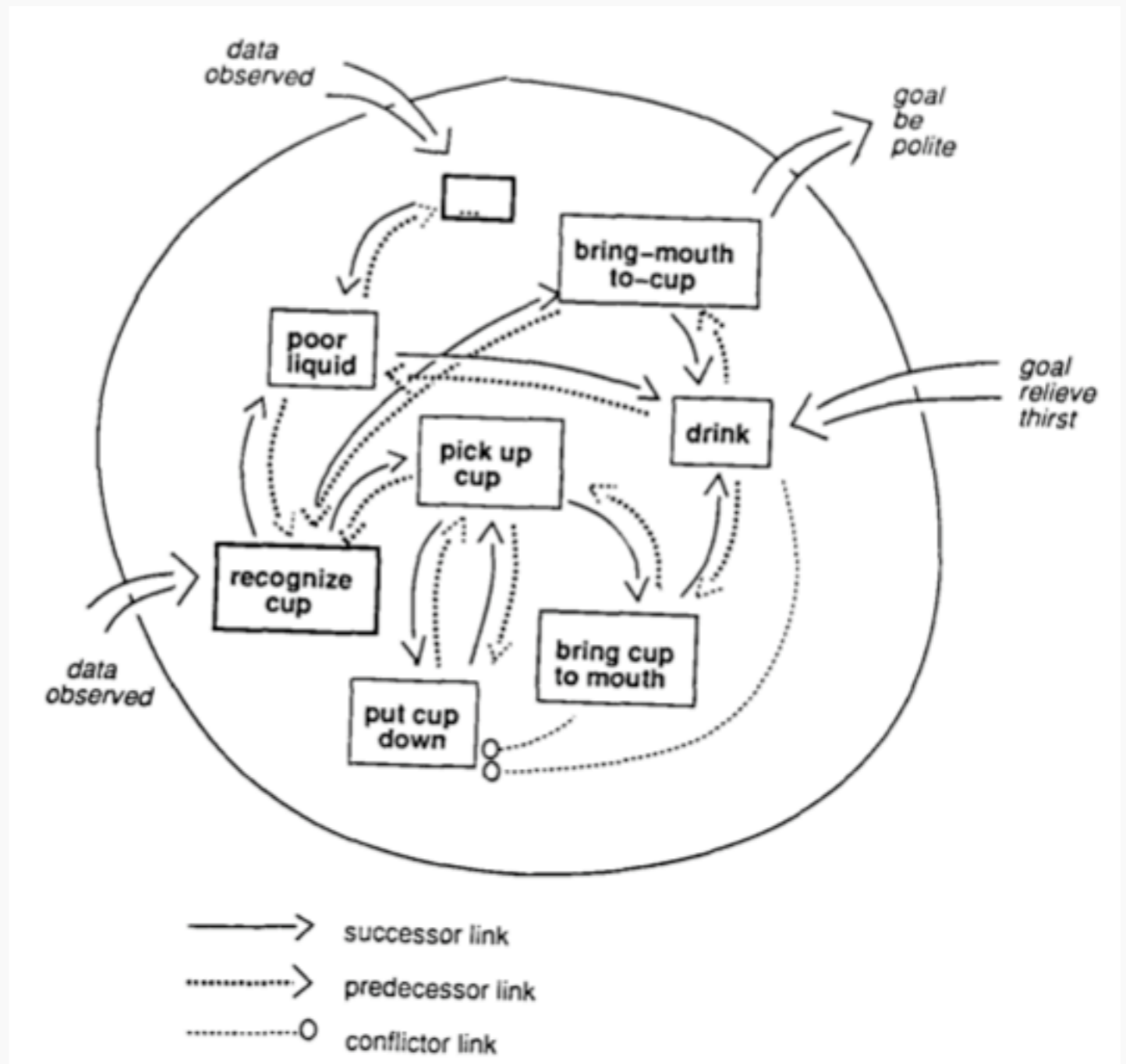
## Subsumption architecture



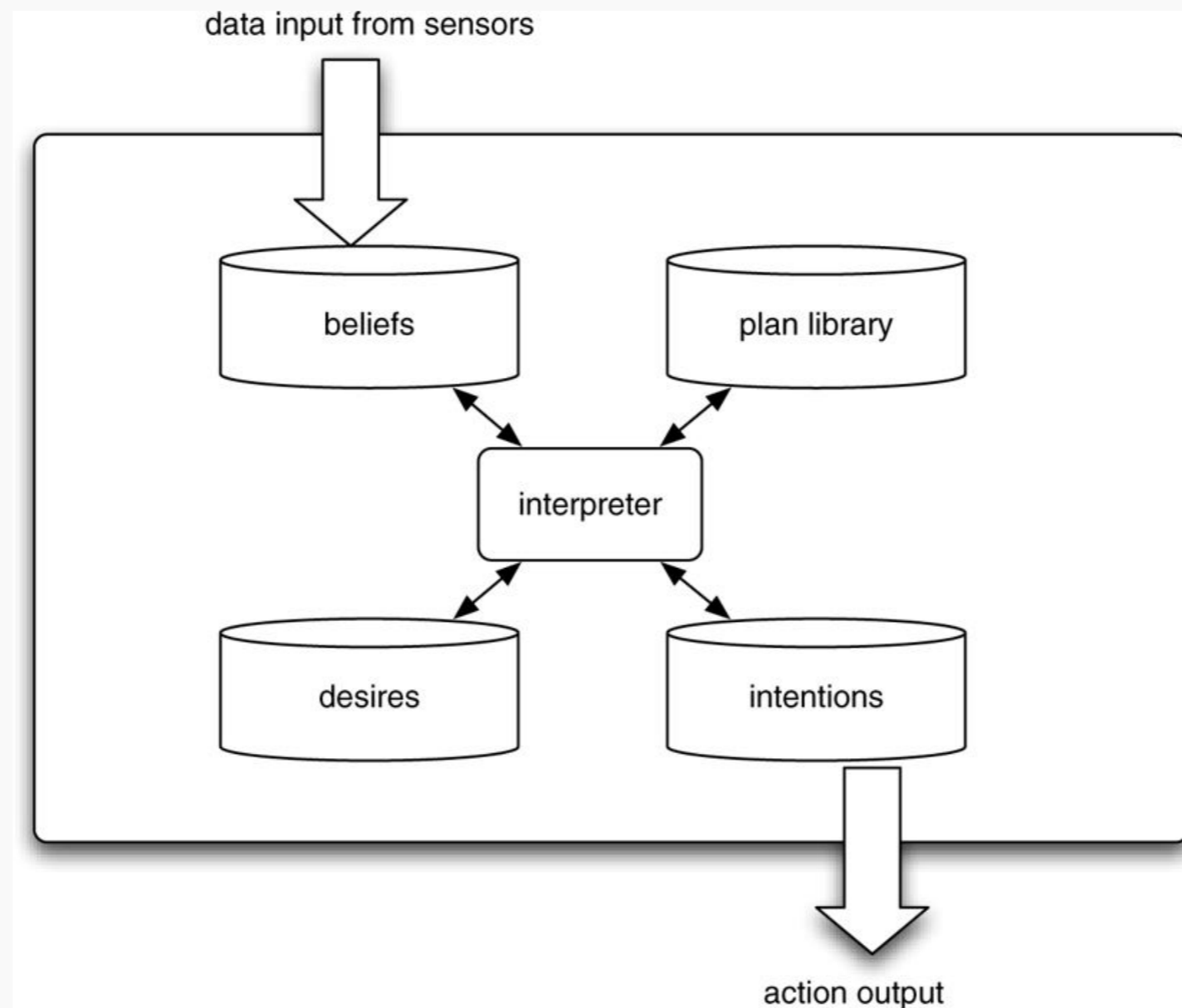
## Agent network architecture

```
defmodule RECOGNIZE CUP
  condition-list: object-observed
  add-list: cup-observed
  delete-list: object-observed
  activation-level: 53
  implementation: <some processes>
```

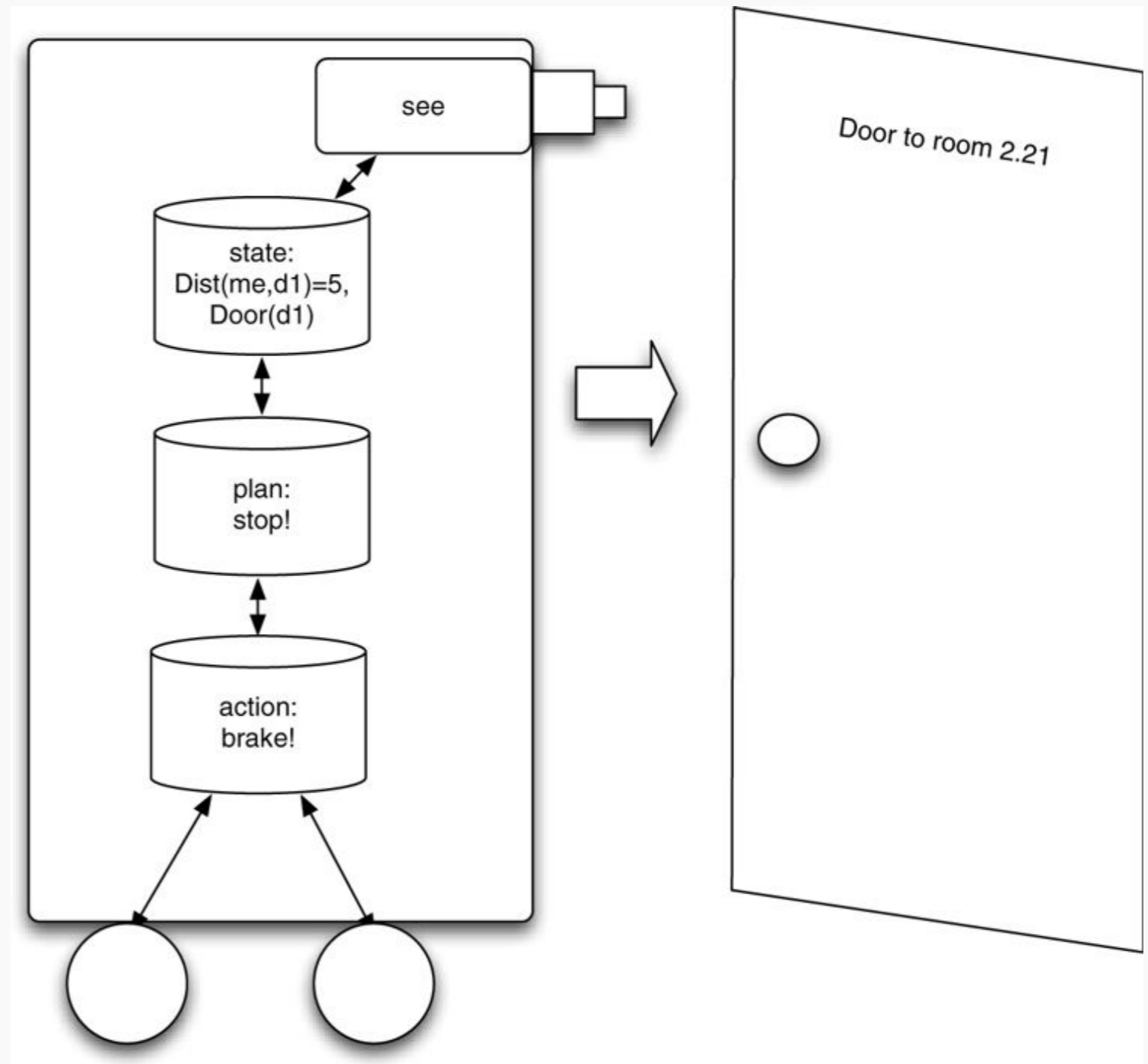
```
defmodule PICK UP CUP
  condition-list: cup-observed hand-empty
  add-list: cup-in-hand
  delete-list: hand-empty
  activation-level: 65
  implementation: <some processes>
```



## Beliefs-Desires-Intentions



## Logical deduction



# Environment

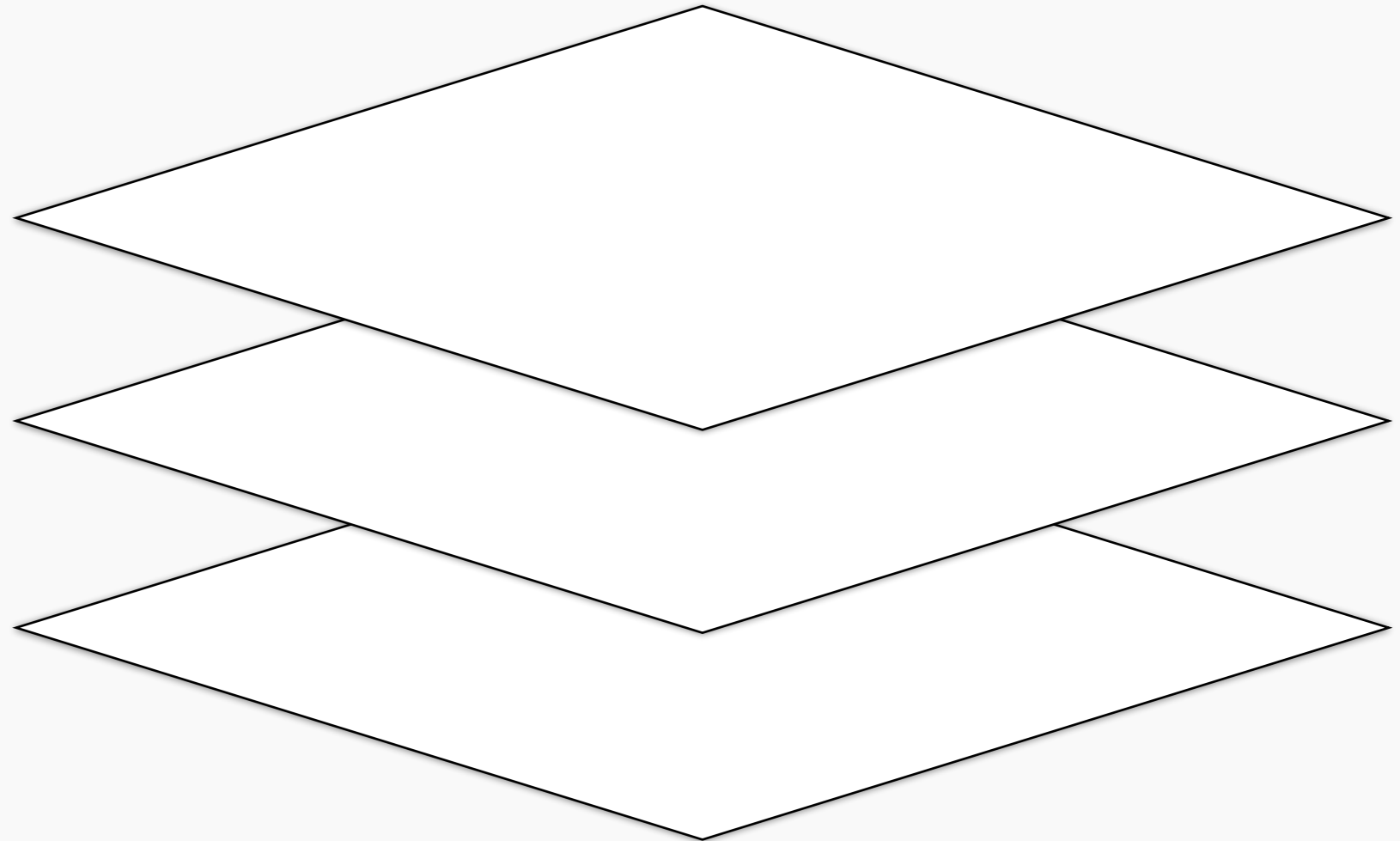
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## 3-Tier model

MAS Application  
environment

Execution platform  
(OS, VM, middleware)

Physical infrastructure  
(hardware, network)





*The environment is a first-class abstraction that provides the surrounding conditions for agents to exist and that mediates both the interaction among agents and the access to resources*

Weyns, Danny, Andrea Omicini, and James J Odell. 2006. "Environment as a First Class Abstraction in Multiagent Systems." *Autonomous Agents and Multi-Agent Systems* 14 (1): 5–30.

*Agents are **situated** in an environment that provides the conditions under which an entity (agent or objects) exists. (Odell)*

Odell, James J, H Van Dyke Parunak, Mitch Fleischer, et Sven Brueckner. 2003. « Modeling Agents and Their Environment ». In *Agent-Oriented Software Engineering III*, 16–31. Springer Berlin Heidelberg.

## Properties:

- Partially vs. totally observable
- Deterministic vs. Stochastic
- Dynamic vs. Static
- Continuous vs. Discrete

$(P, dist)$  is a *quasimetric space*, where:

- $P$  is the set of positions in the space
- $dist : P \times P \rightarrow \mathbb{R}_{\infty}^{+}$  is a metric

$\forall x, y, z \in P :$

$$dist(x, x) = 0$$

(reflexivity)

$$dist(x, y) = 0 \iff x = y$$

(identity of indiscernibles)

$$dist(x, y) \geq 0$$

(positivity)

$$dist(x, z) \leq dist(x, y) + dist(y, z)$$

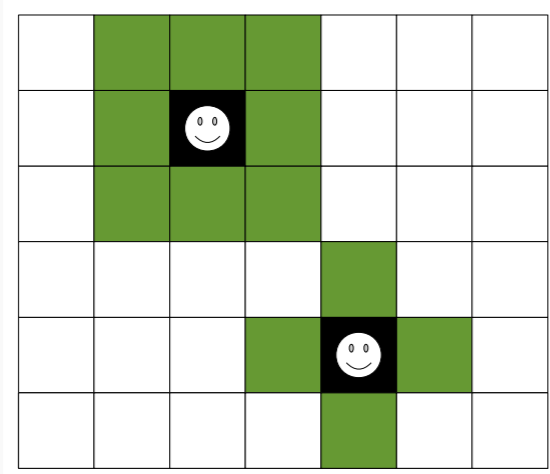
(triangular inequality)

$$\del{dist(x, y) = dist(y, x)}$$

~~(symmetry)~~

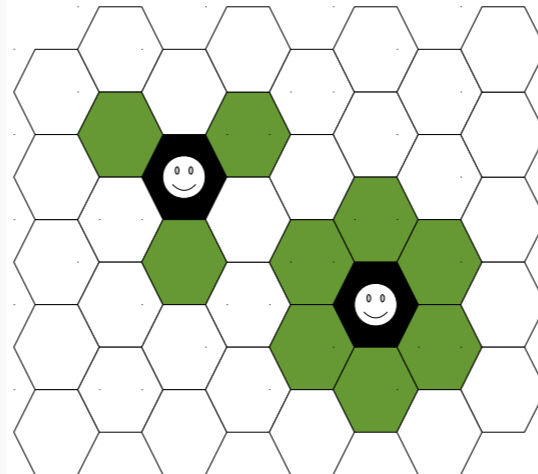
# Environment (discrete)

$$P = \mathbb{Z}^2$$

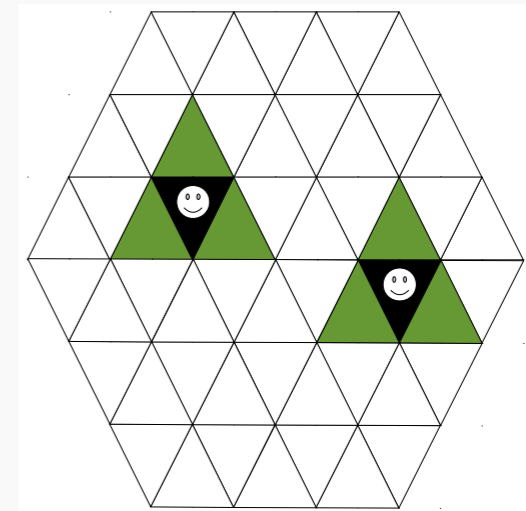


Chebyshev distance (Moore)

Manhattan distance (von Neumann)

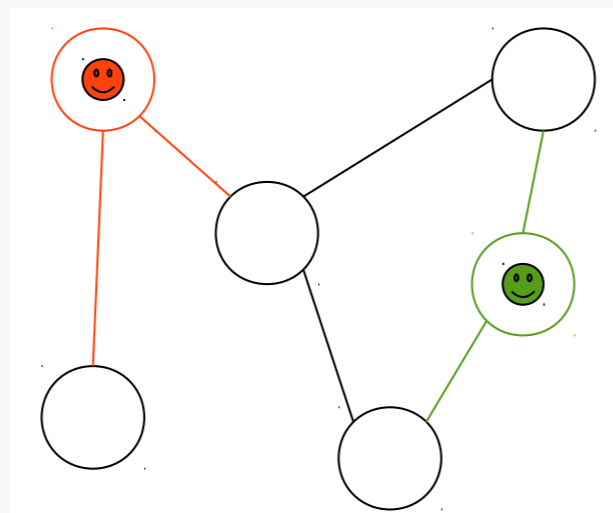


Hexagonal neighborhood



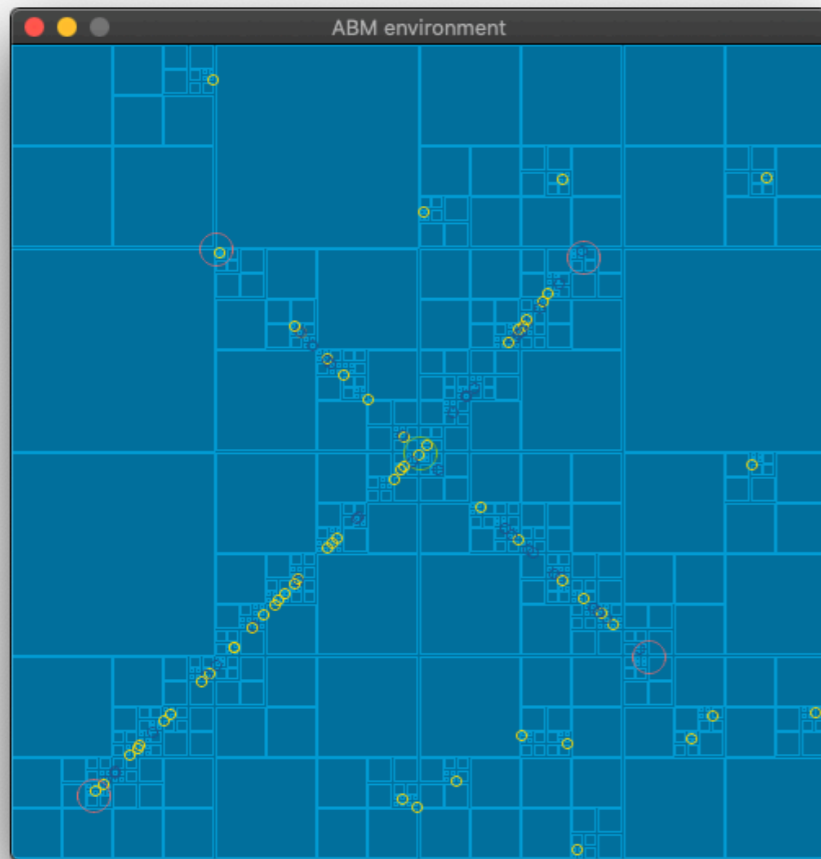
Triangular neighborhood

$$P = \textit{Vertices}$$



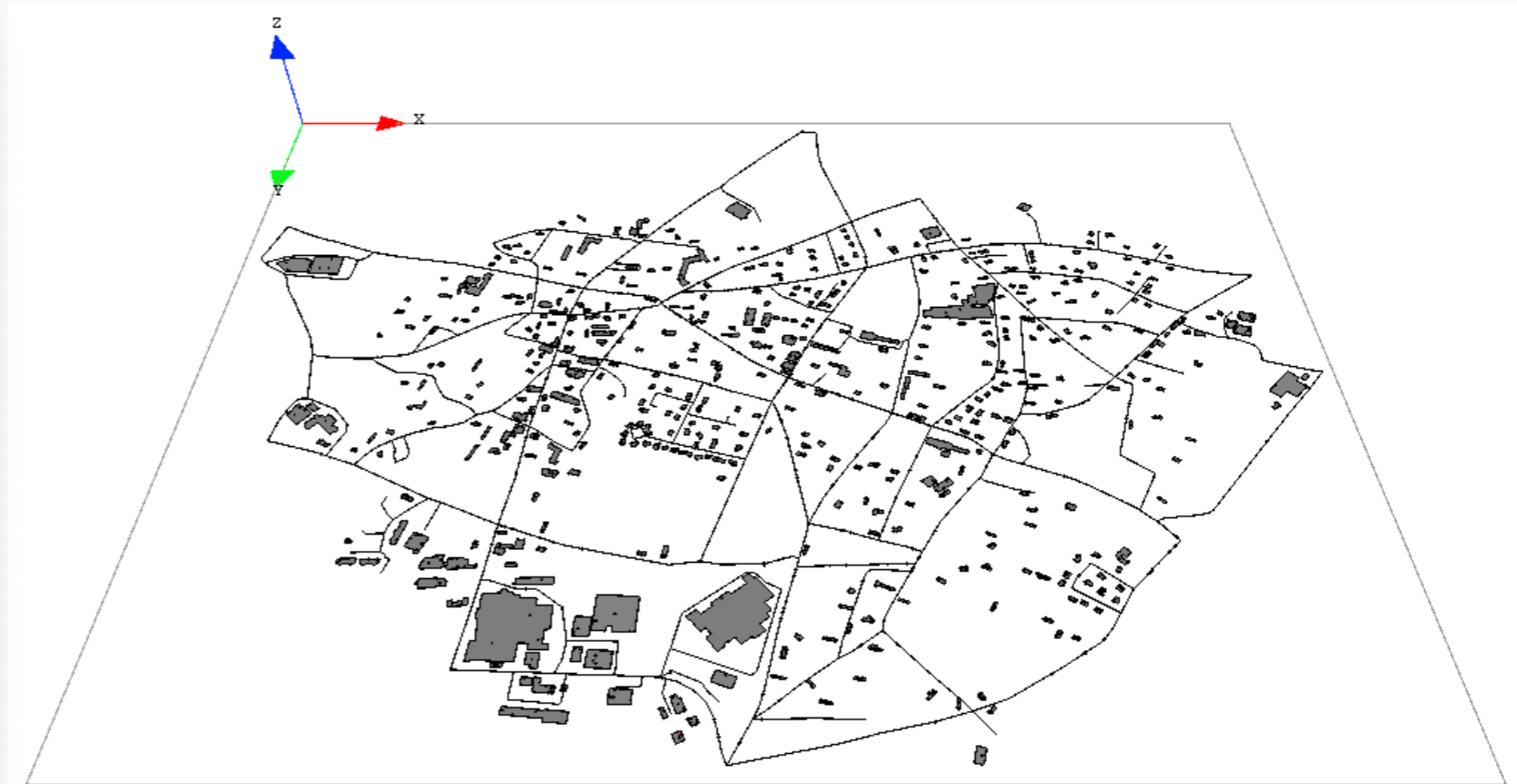
Geodesic distance  
(shortest path)

# Environment (continuous)



$$P = \mathbb{R}^2$$

Euclidean distance



$$P = \mathbb{R}^3$$

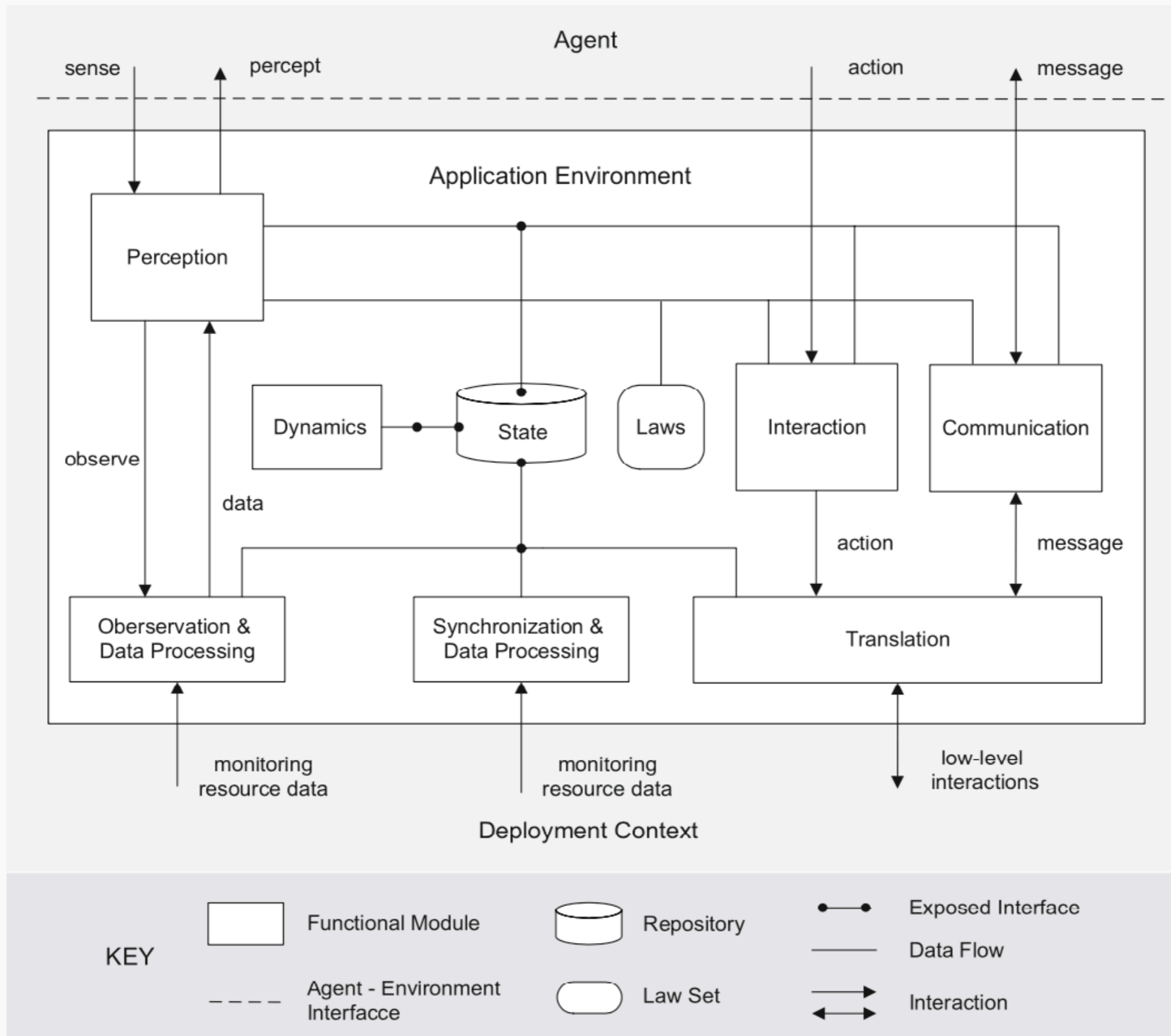
Euclidean distance

*A structuring entity:*

- *physical* structuring
- *communication* structuring
- *social* structuring



# Environment



Weyns, Danny, Andrea Omicini, and James J Odell. 2006. "Environment as a First Class Abstraction in Multiagent Systems." *Autonomous Agents and Multi-Agent Systems* 14 (1): 5–30.

# Interaction

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**Interaction** allows agents to *exchange information*, so they can *cooperate, negotiate, or solve* a conflict rather than just *compete*.

Enabler of **synergy** and **emergence**.

Two types of interaction generally distinguished:

- direct
- indirect

## Indifference, Cooperation, Antagonism

Goals	Resources	Competence	Situation	
Complete	Ok	Ok	<i>Independence</i>	
	Ok	Insufficient	<i>Cooperation</i>	Simple collaboration
	Scarce	Ok		Congestion
	Scarce	Insufficient		Coordinated collaboration
Incomplete	Ok	Ok	<i>Antagonism</i>	Individual competition
	Ok	Insufficient		Collective competition
	Scarce	Ok		Individual conflicts for resources
	Scarce	Insufficient		Collective conflicts for resources

Agents interact *through* the environment and are not necessarily aware of other agents.

Possible architectures:

- Blackboard systems
- Tuple spaces
- Stigmergy

## Blackboard systems

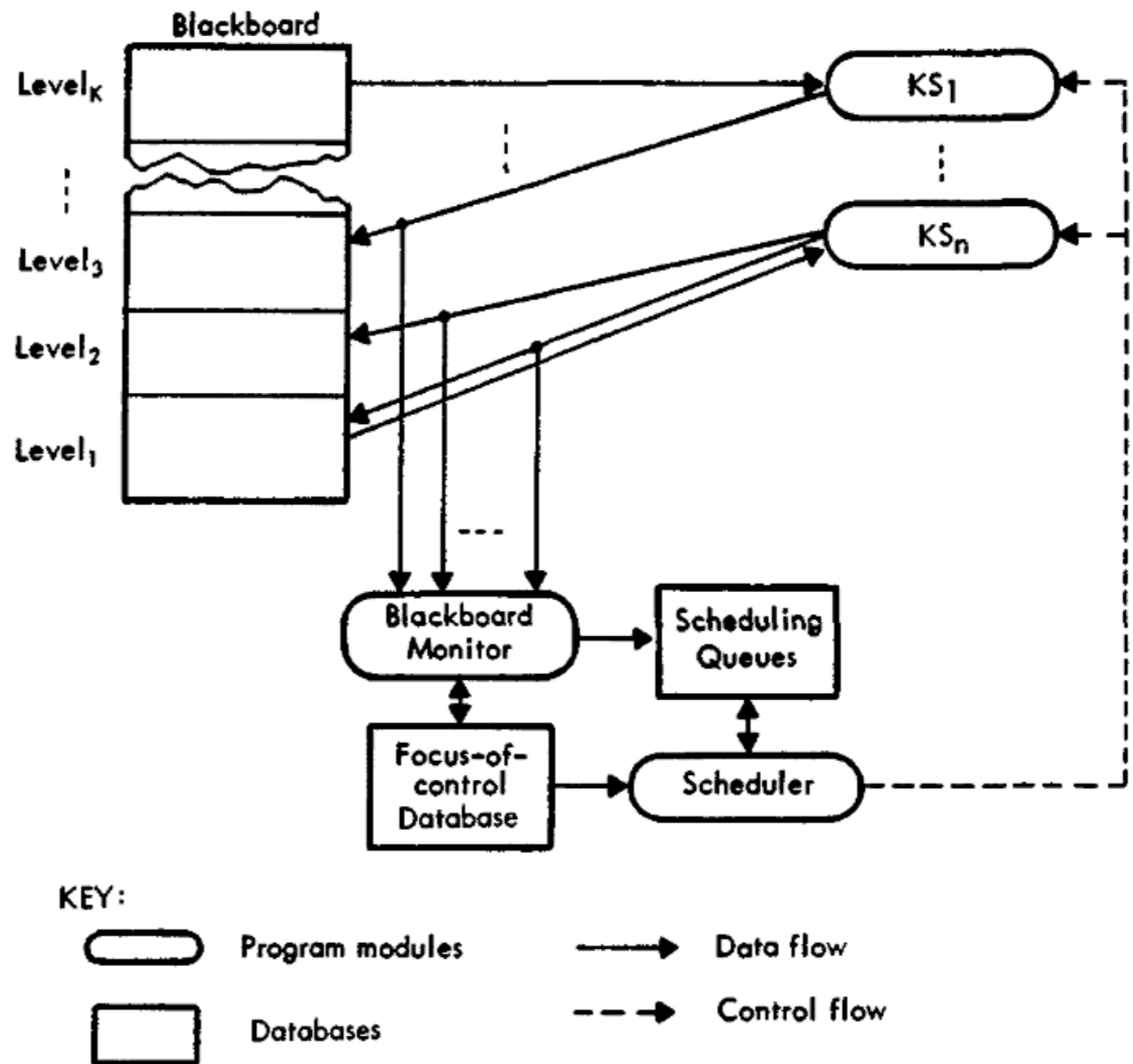


FIGURE 4. Schematic of the Hearsay-II architecture.



## Tuple spaces

Introduced by Linda :

- Coordination and communication languages
- Independent processes shares a tuple space (multiset)
- Tuples are stored and retrieved via 3 operations
  - in (atomic consume)
  - rd (read)
  - out (write)

Gelernter, David, and Nicholas Carriero. 1992. "Coordination Languages and Their Significance." *Communications of the ACM* 35 (2): 96.

LIME (Linda in a Mobile Environment) :

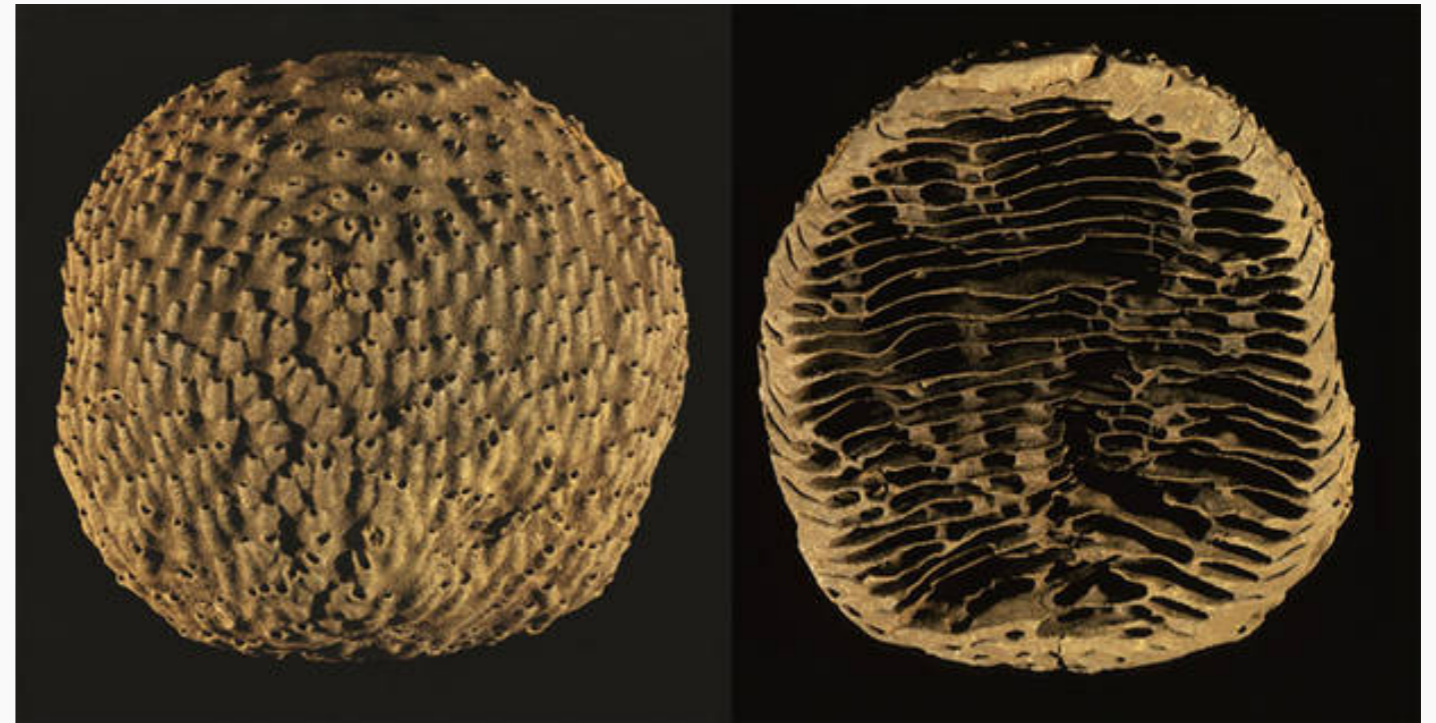
- 1 agent, 1 tuple space
- Tuple spaces merged when agents are on the same host

Murphy, A., Picco, G.P., Roman, G.C.: LIME: a Middleware for Physical and Logical Mobility. 21th International Conference on Distributed Computing Systems (2001)

# Indirect Interaction

**Stigmergy**, coined by P. Grassé

A *spontaneous* phenomenon emerges from the set of individual actions leaving traces in the environment



In practice, depends on :

- Gradient fields (attractive/repulsive)
- Resources (objects that agents can produce/manipulate)

Grassé, Plerre-P. 1959. "La Reconstruction Du Nid et Les Coordinations Interindividuelles Chez Bellicositermes Natalensis et Cubitermes Sp. La Théorie de La Stigmergie: Essai d'interprétation Du Comportement Des Termites Constructeurs." *Insectes Sociaux* 6 (1): 41–80.

Agents communicate through message passing using dedicated channels.

Requires a shared *communication language*:

- FIPA-ACL
- KQML

Influenced by the *speech act* theory (John R. Searle, 1960s):

- *Fact vs. performative* statements
- Explicitly model the *intention* as well as the content of a message

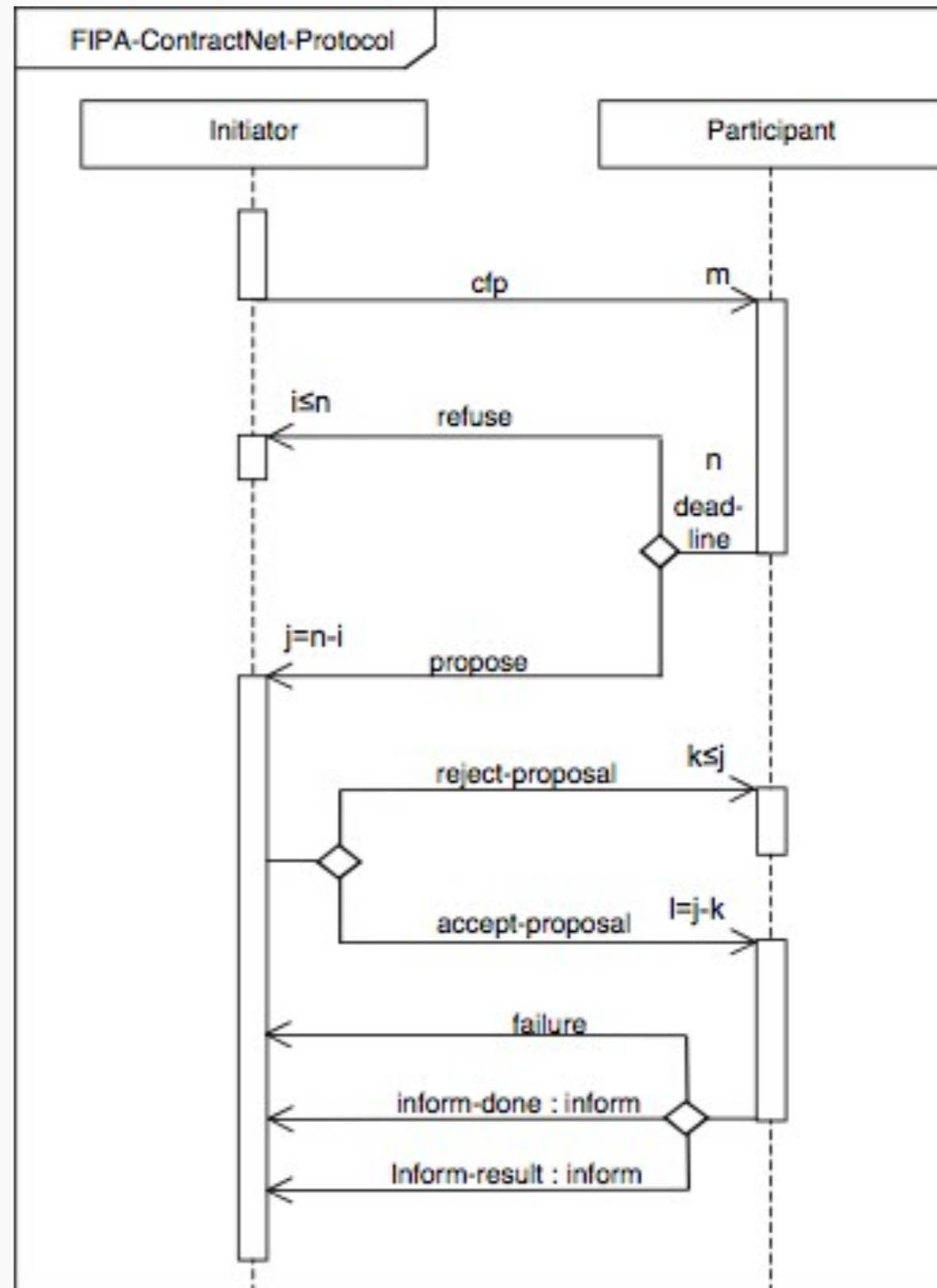
## FIPA-ACL

Parameter	Category of Parameters
performative	Type of communicative acts
sender	Participant in communication
receiver	Participant in communication
reply-to	Participant in communication
content	Content of message
language	Description of Content
encoding	Description of Content
ontology	Description of Content
protocol	Control of conversation
conversation-id	Control of conversation
reply-with	Control of conversation
in-reply-to	Control of conversation
reply-by	Control of conversation

**Table 1:** FIPA ACL Message Parameters

3	FIPA Communicative Acts.
3.1	Accept Proposal .....
3.2	Agree .....
3.3	Cancel .....
3.4	Call for Proposal .....
3.5	Confirm .....
3.6	Disconfirm.....
3.7	Failure.....
3.8	Inform .....
3.9	Inform If .....
3.10	Inform Ref .....
3.11	Not Understood.....
3.12	Propagate .....
3.13	Propose .....
3.14	Proxy.....
3.15	Query If .....
3.16	Query Ref .....
3.17	Refuse .....
3.18	Reject Proposal .....
3.19	Request .....
3.20	Request When .....
3.21	Request Whenever .
3.22	Subscribe .....

## FIPA-ContractNet



# Organisation

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Organisation is about forming virtual societies of agents in terms of:

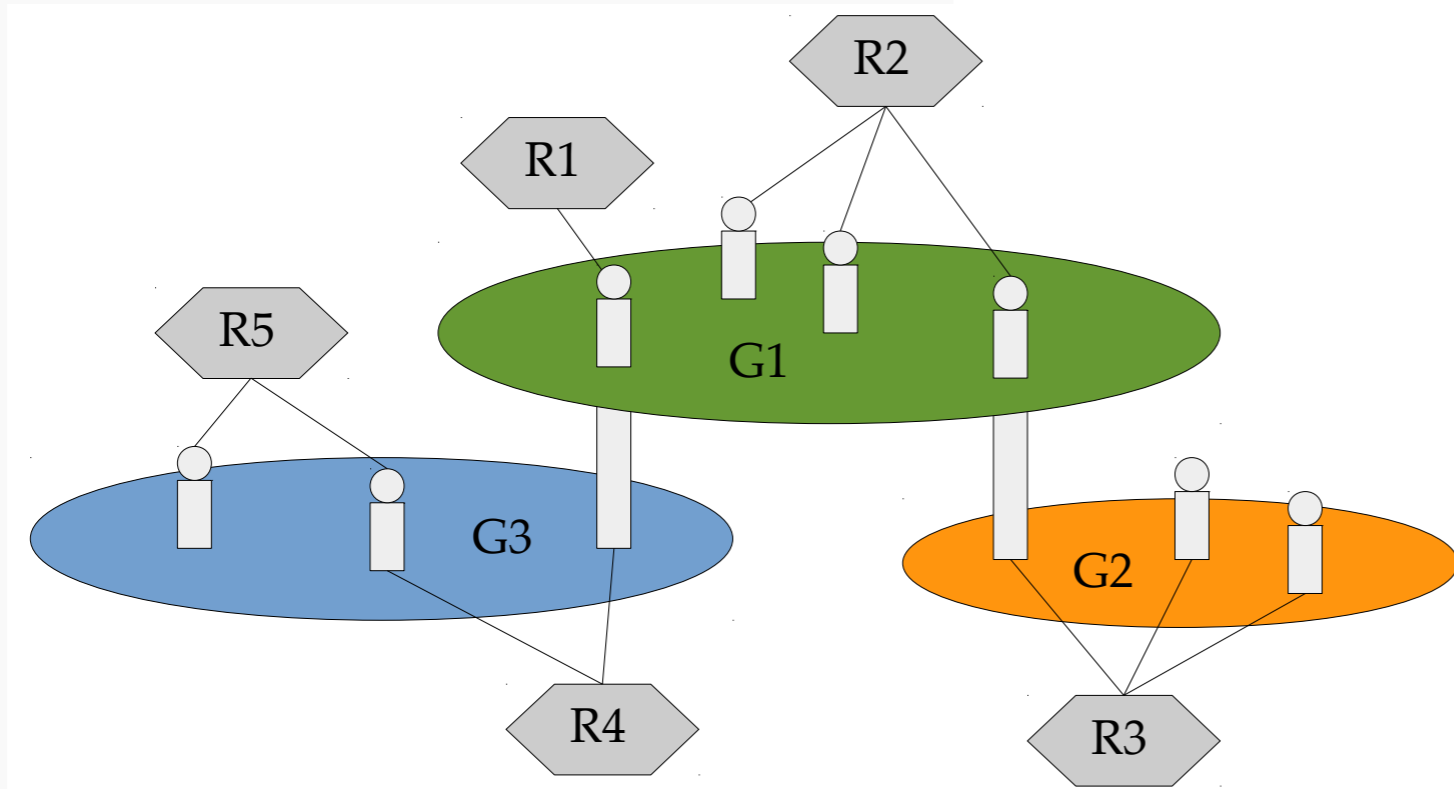
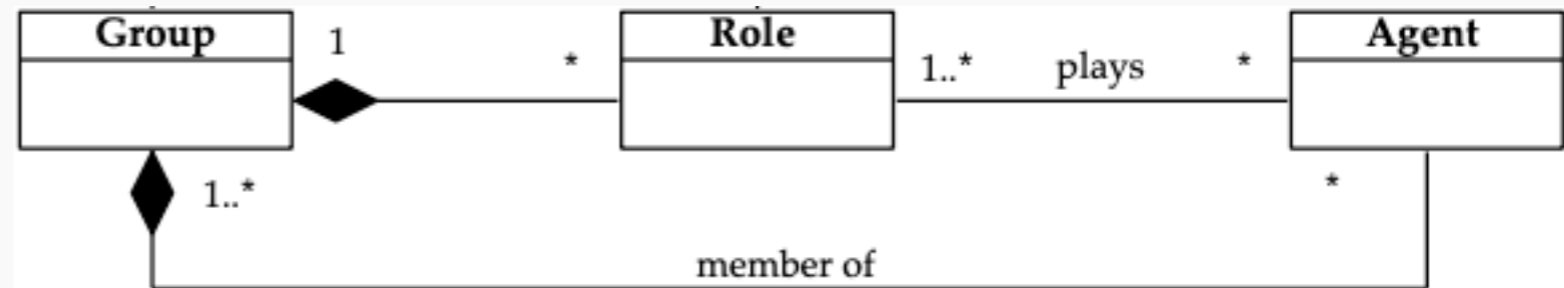
- Structure (groups, roles)
- Behaviour (norms, sanctions)
- Collective knowledge (institutions, culture)

# Structural organisation

Establish the links that unite (or oppose) agents (OCMAS)

- Helps managing complexity (who to interact with)
- Hierarchy between agents, roles, groups
- Part of the environment responsibilities

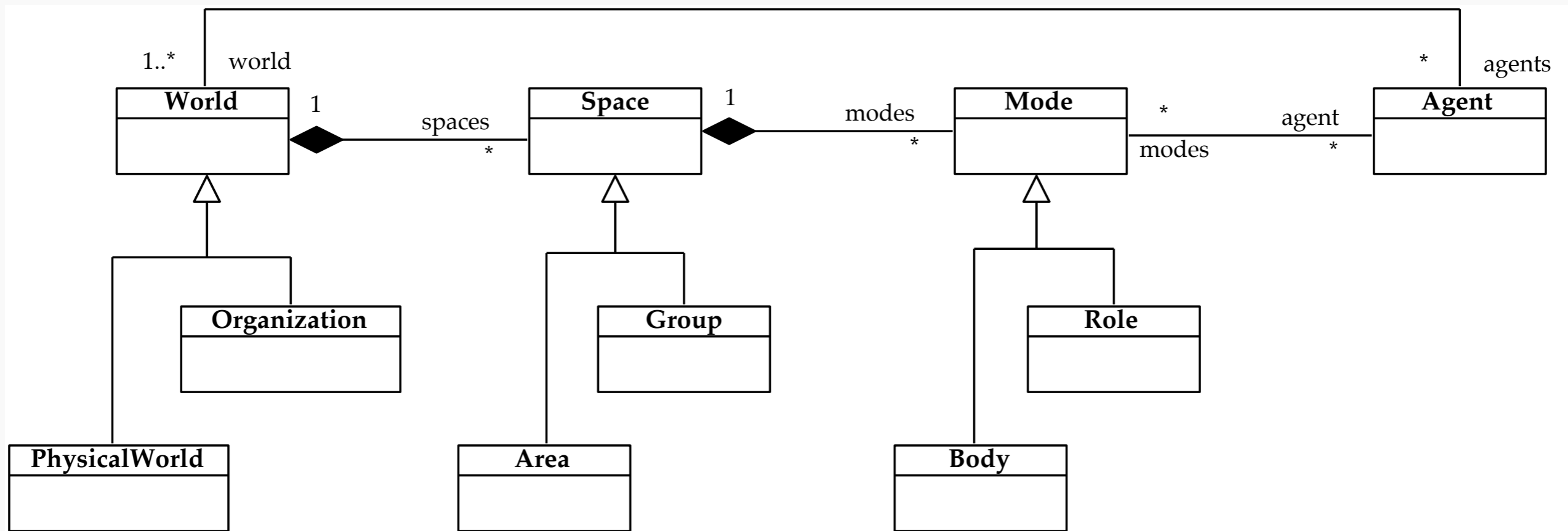
Example: AGR metamodel





# Structural organisation, an environment?

## AGRE (Agent-Group-Role-Environment)



# Structural organisation as a topology

$(P, dist)$  is a ~~quasimetric~~ *hemimetric space*, where:

- $P$  is the set of positions in the space
- $dist : P \times P \rightarrow \mathbb{R}_\infty^+$  is a metric

$\forall x, y, z \in P :$

$$dist(x, x) = 0$$

(reflexivity)

$$\del{dist(x, y) = 0} \iff \del{x = y}$$

~~(identity of indiscernibles)~~

$$dist(x, y) \geq 0$$

(positivity)

$$dist(x, z) \leq dist(x, y) + dist(y, z)$$

(triangular inequality)

$$P = \{ \text{R1} \text{ } \text{R2} \cdots \text{RN} \}$$

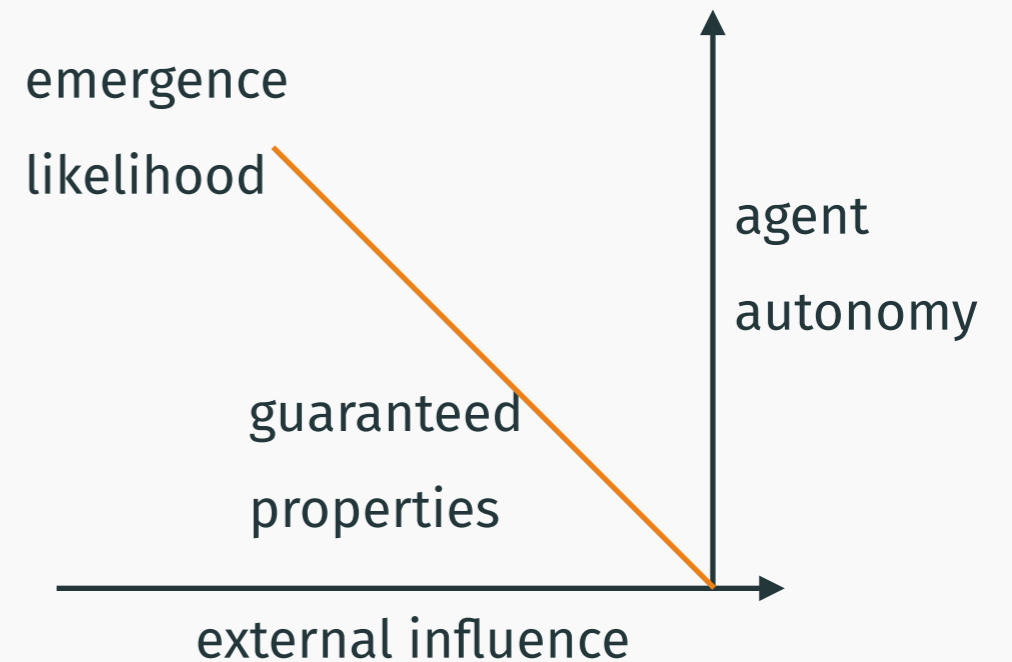
# Behavioral organisation

## Controlling agents behaviour

- Influence agents
- Contradicts autonomy property

## Borrow concepts from social sciences

- Norms
- Social commitment
- Sanctions



## Normative MAS

Norm = Principle of good deed

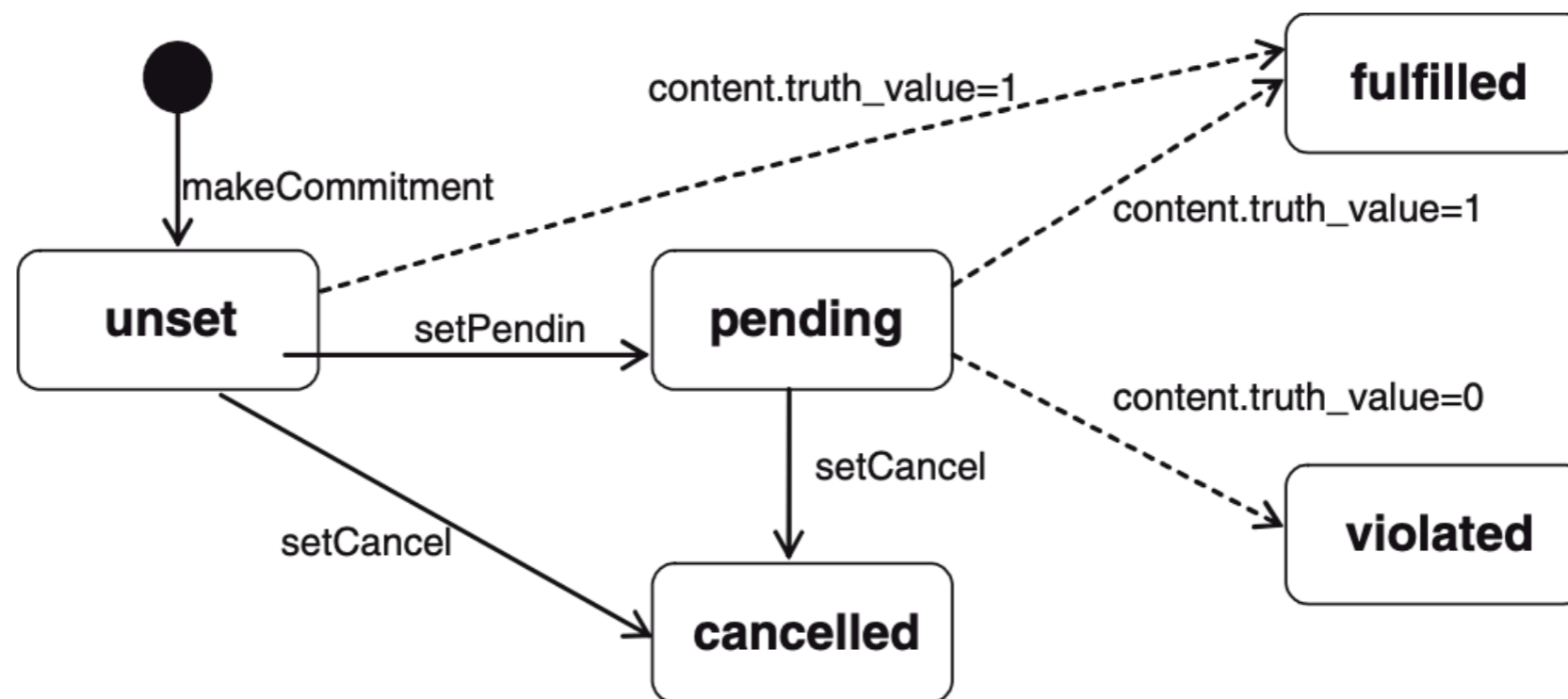
- Guides or regulates agent behavior
- Norms shared by a group
- Members can judge conformance or deviance
- Norms may evolve

From agent perspective

- Can choose conformance or deviance
- Can anticipate behavior of other agents
- Still fully autonomous

**Social commitment** is about modelling expectation.

A commitment is made by a *debtor* to a *creditor*



**Fig. 2** The life-cycle of commitments

## Sanction (or reward)

### Types:

- automatic (carried by action)
- material (e.g. violence/healing)
- social (e.g. reputation)
- psychological (emotions, e.g. guilt)

### Styles:

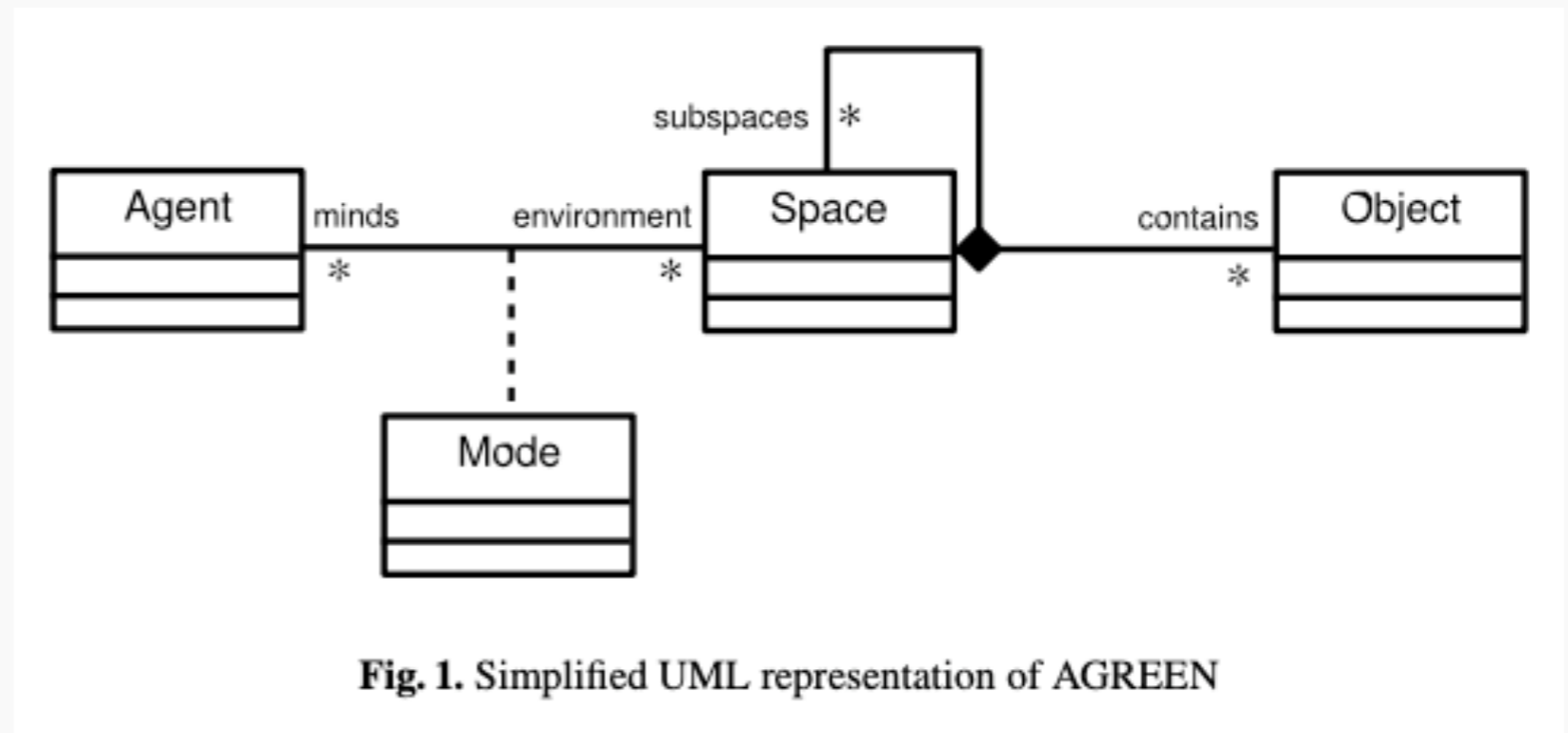
- implicit (self-inflicted)
- explicit (public)

### Application policies:

- deterrence (severe immediate sanctions, reduces flexibility)
- retribution (revenge)
- invalidation (isolation)

## Norms as a regulation system

- Makes sense for a community
- What about distinct communities?



## Institution

- Rule-based system
- Regulate interactions
- Institutional facts
- Assigns status to entities/agents
- Capability
- Relations between social and physical world
  - *count as* operator (X counts as Y in context C)





# Scheduling

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Let

$E = \{e, e', \dots\}$  a finite set of discrete instantaneous environment states, and

$Ac = \{a, a', \dots\}$  the set of possible actions available to agents.

A run,  $r$ , of an agent in an environment is a sequence of *interleaved* environment states and actions:

$$r : e_0 \xrightarrow{a_0} e_1 \xrightarrow{a_1} e_2 \xrightarrow{a_2} e_3 \xrightarrow{a_3} \dots \dots \xrightarrow{a_{n-1}} e_n.$$

- **In-place vs. out-place**

$$Mem_a : P_a \times S_a \rightarrow S_a$$

$$Percept_a : \Sigma \rightarrow P_a$$



$$Decision_a : P_a \times S_a \rightarrow \Sigma$$

$$Behavior_a : \Sigma \rightarrow \Sigma$$

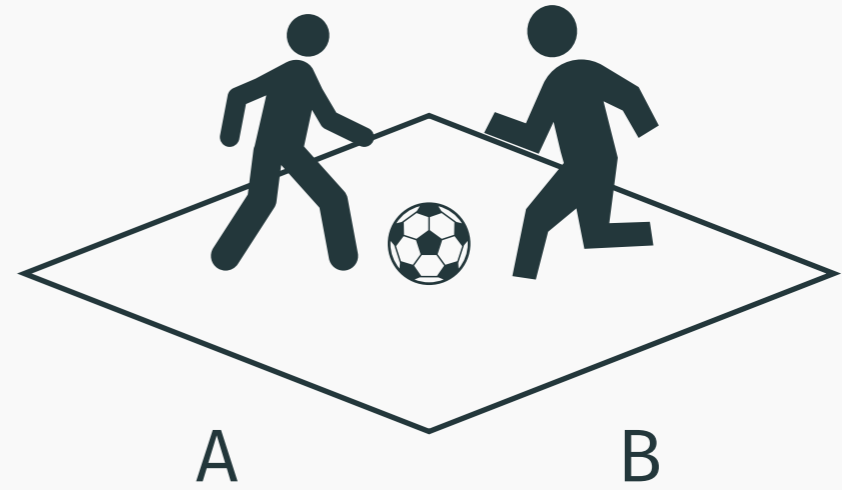
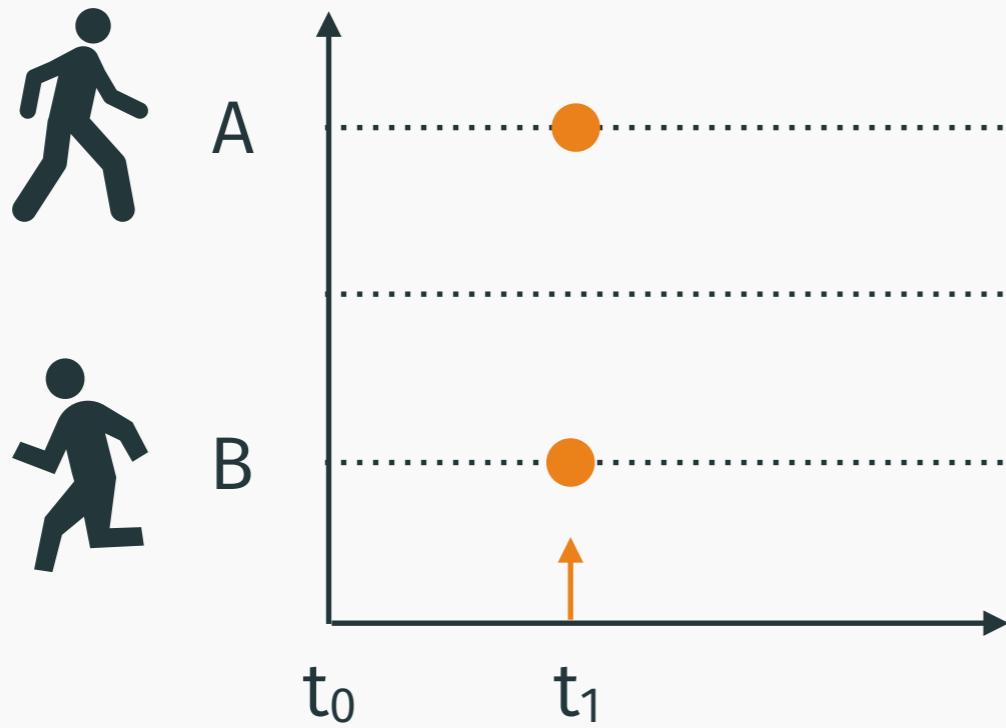
$$\sigma \mapsto Decision_a(p_a, Mem_a(p_a, s_a))$$

with

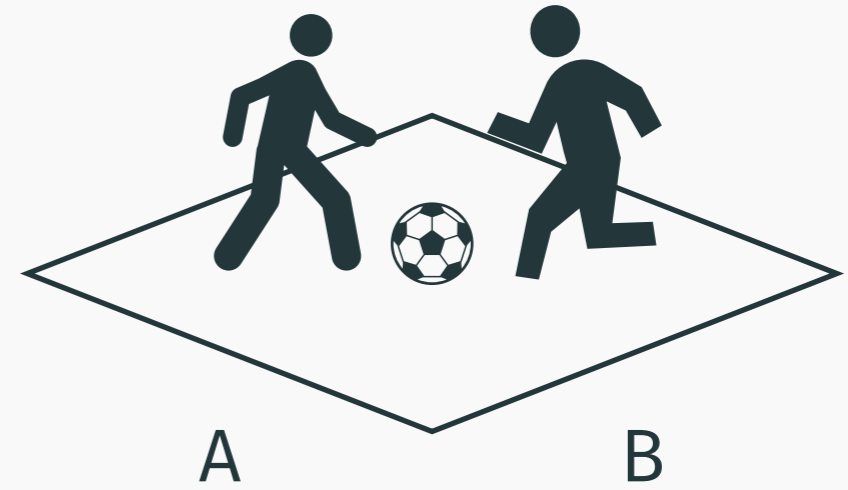
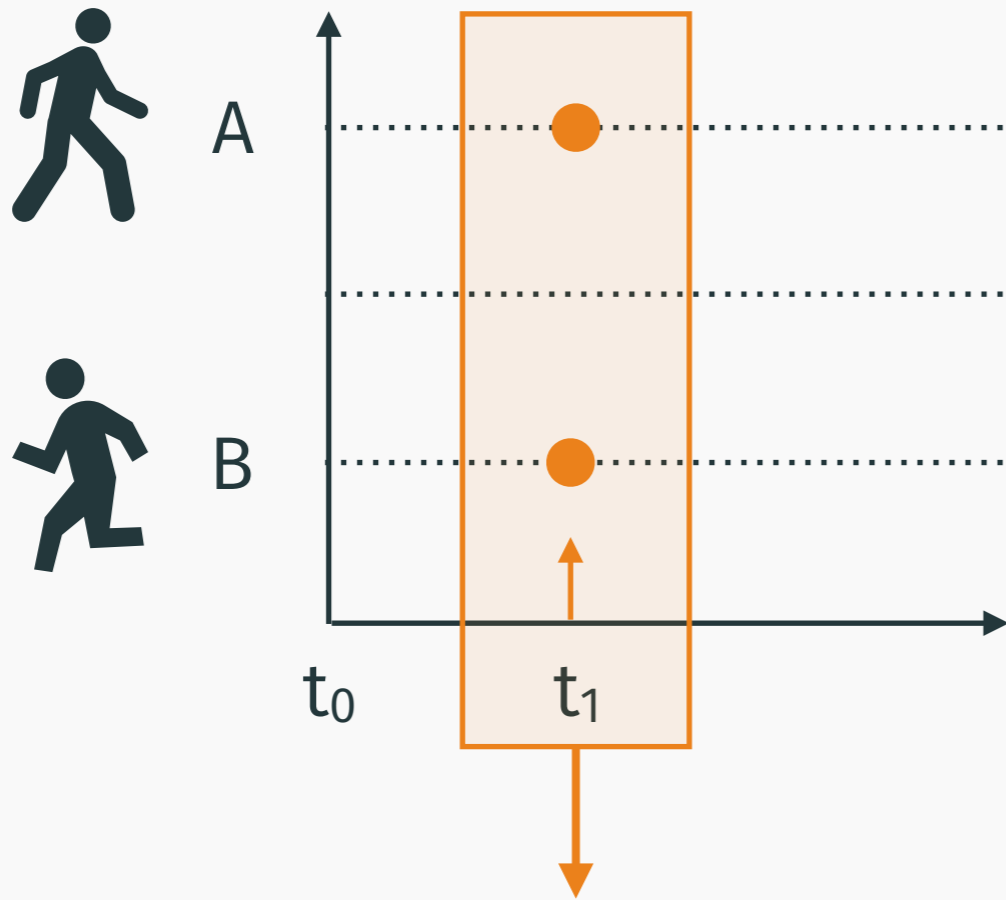
$$p_a = Percept_a(\sigma)$$

```
0 def simulate(abm: ABM) {
1   time = 0
2   env = abm.env
3   env.state = env.initial_state
4   for (ag in abm.agents) {
5     ag.state = ag.initial_state
6   }
7   while (not termination_condition()) {
8     for (ag in abm.agents) {
9       percept = ag.percept(env.state)
10      ag.state = ag.mem(percept, ag.state)
11      env.state = ag.decision(percept, ag.state)
12    }
13    time += 1
14  }
15 }
```

# Scheduling



# Scheduling

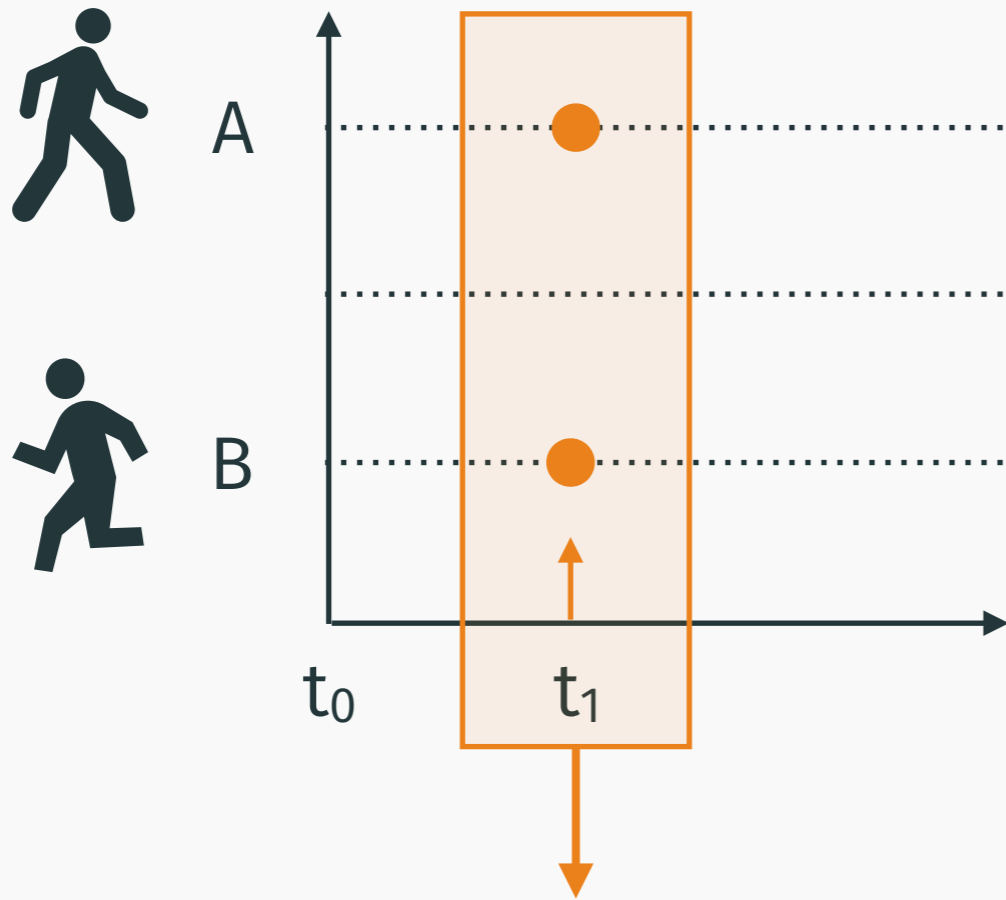


Sequential application

1  
memory layout



# Scheduling

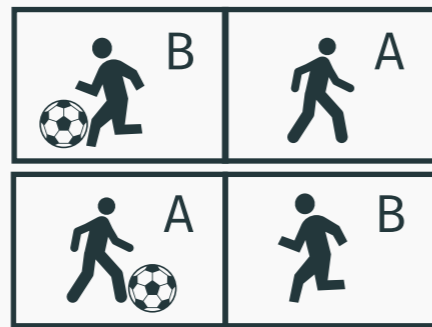


Sequential application

1  
memory layout



2  
random

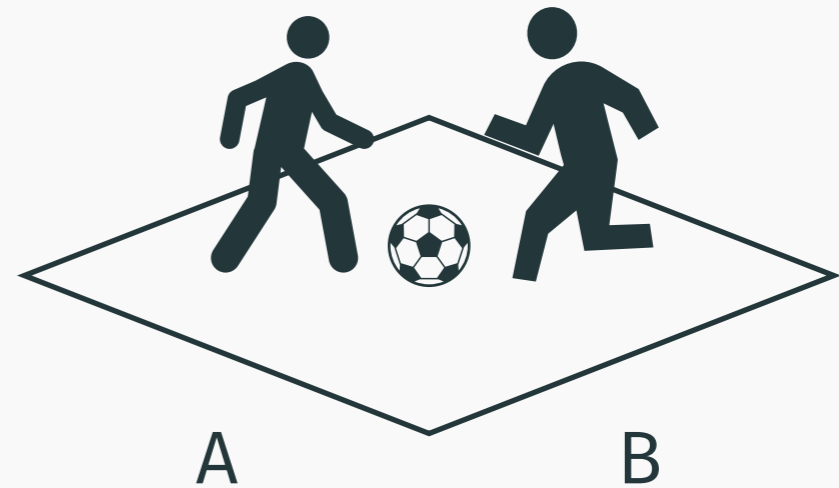
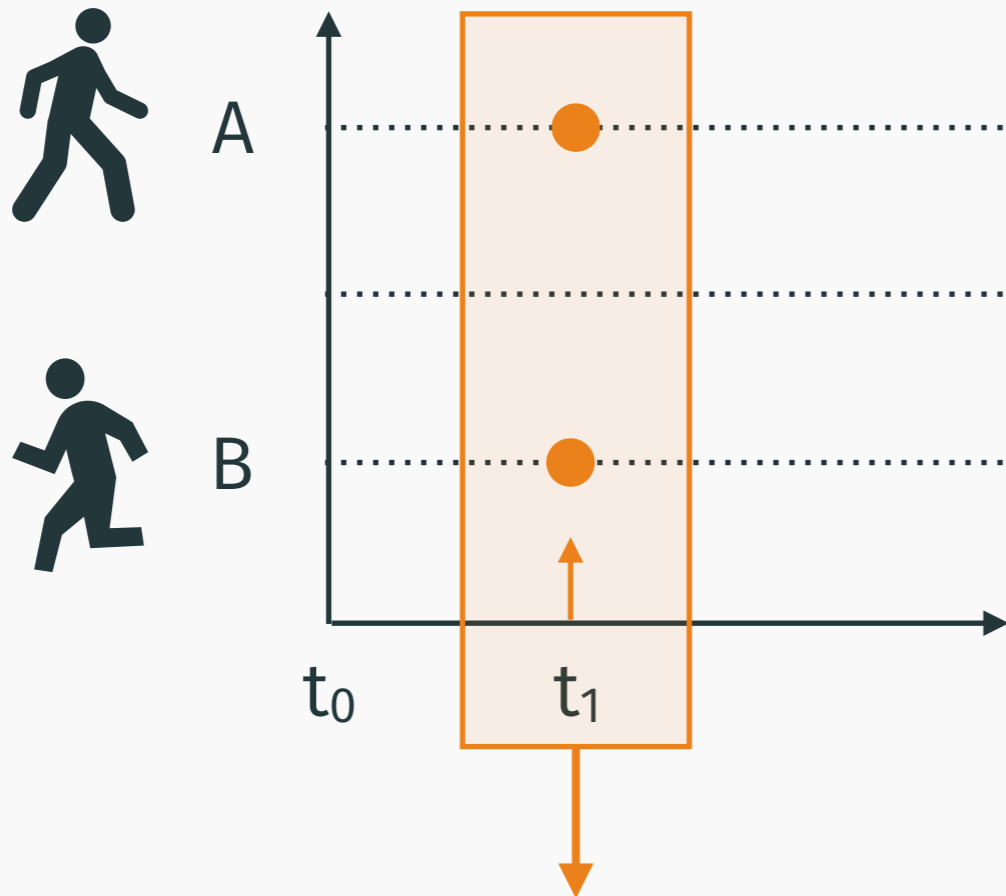




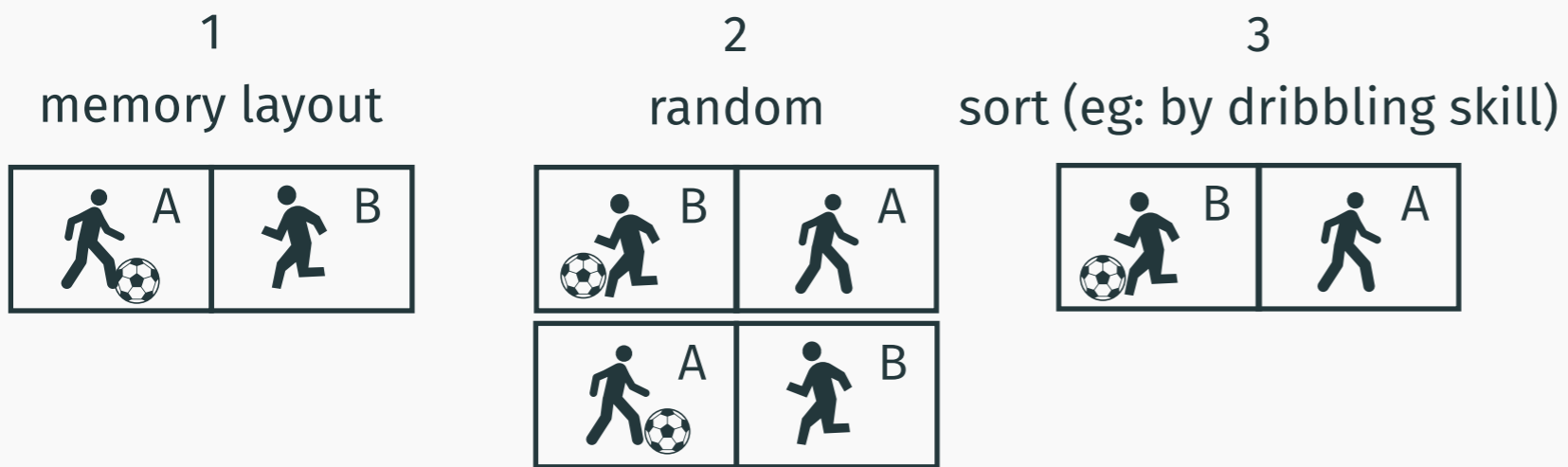
# Operational semantics (random)

```
0 def simulate(abm: ABM) {
1   time = 0
2   prng_seed = abm.seed
3   env = abm.env
4   env.state = env.initial_state
5   for (ag in abm.agents) {
6     ag.state = ag.initial_state
7   }
8   while (not termination_condition()) {
9     for (ag in shuffle(abm.agents)) {
10      percept = ag.percept(env.state)
11      ag.state = ag.mem(percept, ag.state)
12      env.state = ag.decision(percept, ag.state)
13    }
14    time += 1
15  }
16 }
```

# Scheduling



## Sequential application

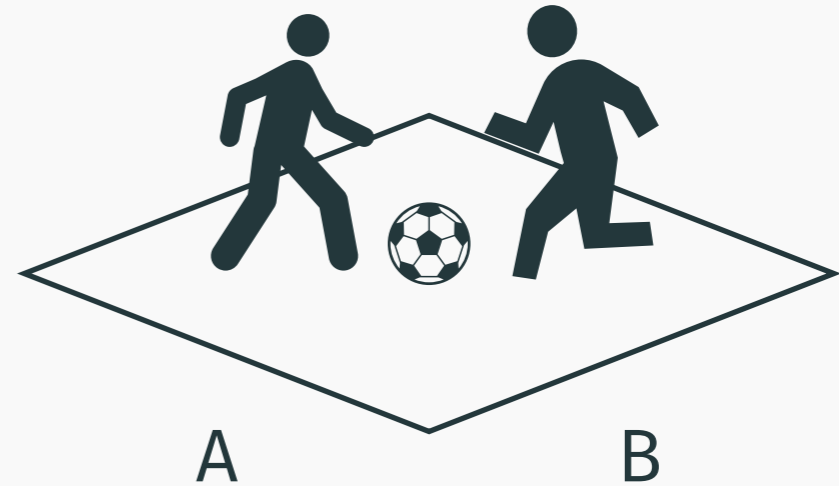
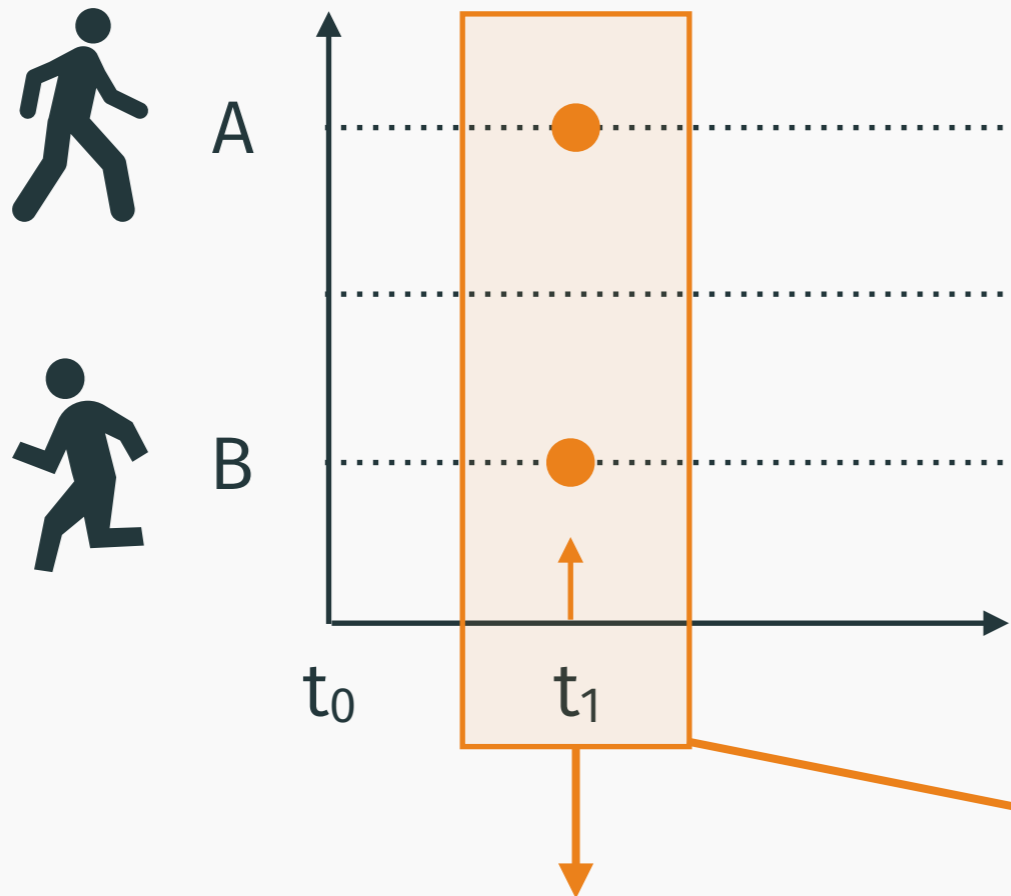


# Operational semantics (explicit order)

```
0 def simulate(abm: ABM) {
1   time = 0
2   env = abm.env
3   env.state = env.initial_state
4   for (ag in abm.agents) {
5     ag.state = ag.initial_state
6   }
7   while (not termination_condition()) {
8     for (ag in sort(abm.agent_comparator, abm.agents)) {
9       percept = ag.percept(env.state)
10      ag.state = ag.mem(percept, ag.state)
11      env.state = ag.decision(percept, ag.state)
12    }
13    time += 1
14  }
15 }
```

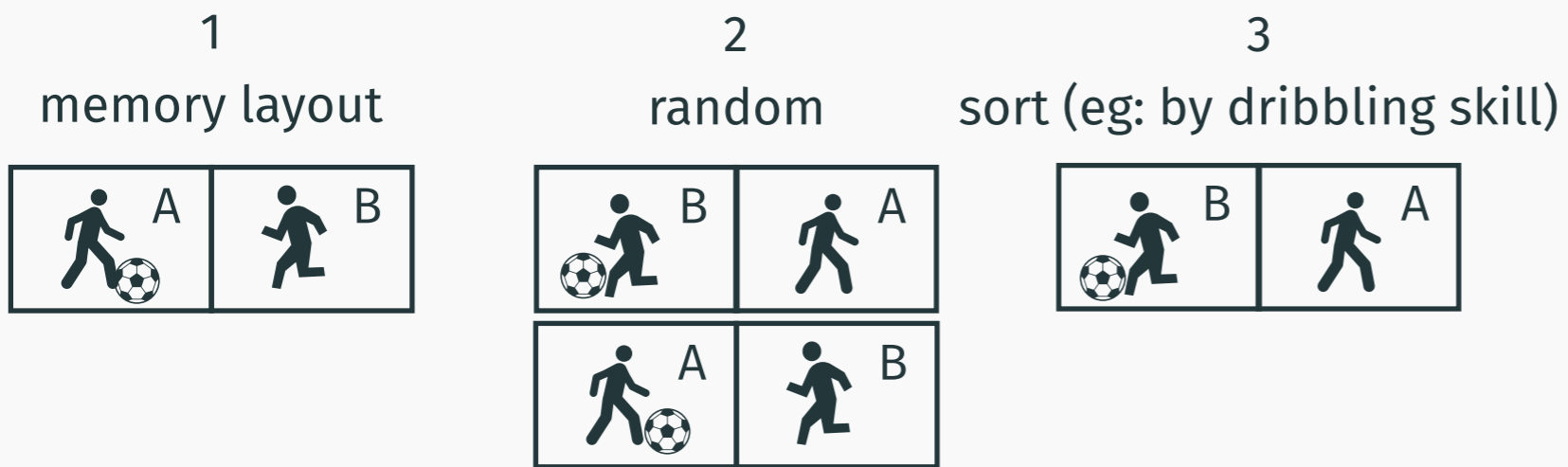
```
abm.agent_comparator = lambda(ag) { ag.dribbling_skill }
```

# Scheduling



Sequential application

Explicit simultaneity



The environment is given all possible actions

## The IRM4S model

System:  $\Delta = \langle \Sigma, \Gamma \rangle$ , where

- $\Sigma$  is the set of environment states
- $\Gamma$  is the set of influences

$$\textit{Behaviour}_a : \Sigma \times \Gamma \rightarrow \Gamma$$

$$\textit{Natural}_e : \Sigma \times \Gamma \rightarrow \Gamma$$

$$\textit{Evolution} : \Delta \rightarrow \Delta$$

$$(\sigma, \gamma) \mapsto \textit{Reaction}(\sigma, \textit{Influence}(\sigma, \gamma))$$

$$\textit{Influence} : \Sigma \times \Gamma \rightarrow \Gamma$$

$$(\sigma, \gamma) \mapsto \bigcup_{a \in Ag} \textit{Behaviour}_a(\sigma, \gamma) \cup \textit{Natural}_e(\sigma, \gamma)$$

$$\textit{Reaction} : \Sigma \times \Gamma \rightarrow \Sigma \times \Gamma$$

# Operational semantics

```
0 def simulate(abm: ABM) {
1   time = 0
2   env = abm.env
3   env.state = env.initial_state
4   for (ag in abm.agents) {
5     ag.state = ag.initial_state
6   }
7   while (not termination_condition()) {
8     influences = []
9     for (ag in abm.agents) {
10      percept = ag.percept(env.state)
11      ag.state = ag.mem(percept, ag.state)
12      influences.add(ag.decision(percept, ag.state))
13    }
14    influences.add(env.natural(percept, ag.state))
15    env.state = reaction(env.state, influences)
16    time += 1
17  }
18 }
```

## Case study

---

# Traffic system example

The screenshot shows the NetLogo interface for a traffic simulation. At the top, there are tabs for 'Interface', 'Info', and 'Code'. Below the tabs is a 'normal speed' slider set to 208 ticks. The main interface contains several sliders and buttons: 'number-of-cars' (set to 3), 'red car speed' (set to 0.005), 'max-acceleration' (set to 0.09), 'max-deceleration' (set to 0.11), and 'red-car-desired-speed' (set to 0.00). There are 'setup' and 'go' buttons. A graph titled 'Car speeds' plots speed (0 to 1.1) against time (0 to 300). The graph shows three lines: a red line that starts at 0.431 and drops to 0, a green line that peaks at approximately 1.0, and a blue line that remains at 0. Below the graph is a visual representation of a road with three cars (two red, one blue) and a circular inset showing a zoomed-in view of the cars. At the bottom, there is a 'Command Center' with a 'Clear' button and a command prompt 'observer>'.

