#### Statecharts aka Harel Charts

- visual formalism
- application of higraphs
- diverse applications;

in particular: concurrent, reactive systems behaviour modelling

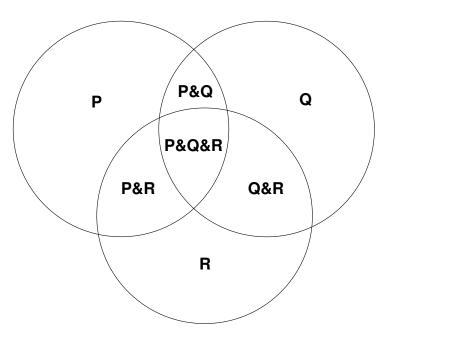
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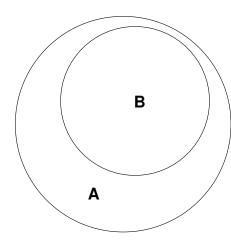
#### Visualising Information

- complex
- non-quantitative, structural
- topological, not geometrical
- Euler
  - Venn diagrams (Jordan curve: inside/outside): enclosure, intersection
  - graphs (nodes, edges: binary *relation*); hypergraphs

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#### Venn diagrams, Euler circles

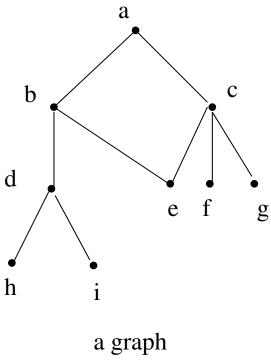


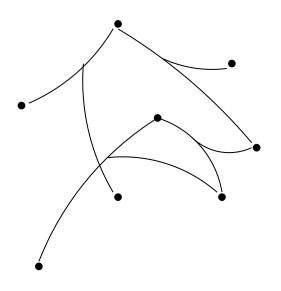


- topological notions:
  enclosure, intersection, exclusion
- Used to represent *mathematical set operations*: union, intersection, difference

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#### Hypergraph





a hypergraph

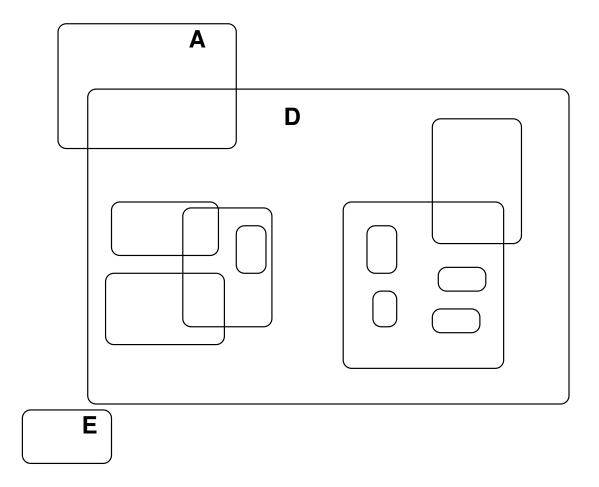
- topological notion: connectedness
- Used to represent *relations* between sets.
- Hyperedges: non longer binary relation ( $\subseteq X \times X$ ):  $\subseteq 2^X$  (undirected),  $\subseteq 2^X \times 2^X$  (directed).

# Higraphs: combining hypergraphs and Venn diagrams

- sets + cartesian product
- hypergraphs

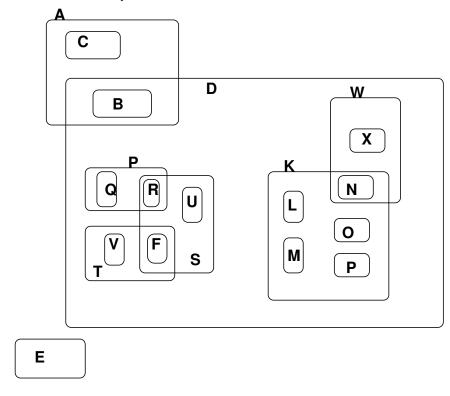
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#### Blobs: set inclusion, not membership



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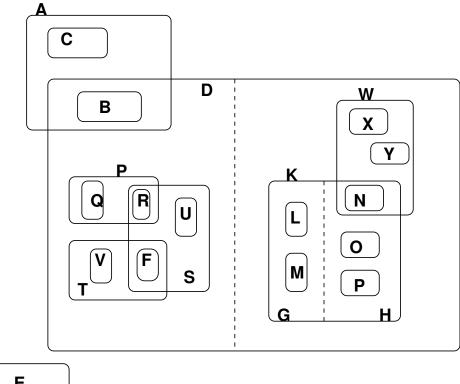
#### Unique Blobs (atomic sets, no intersection)



- empty space has no meaning, intersection must be identified
- atomic blobs are identifiable sets
- other blobs are union of enclosed sets

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#### **Unordered Cartesian Product:** Orthogonal Components

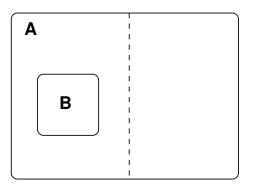


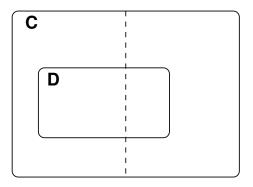
Ε

$$K = G \times H = (L \cup M) \times (N \cup O \cup P)$$

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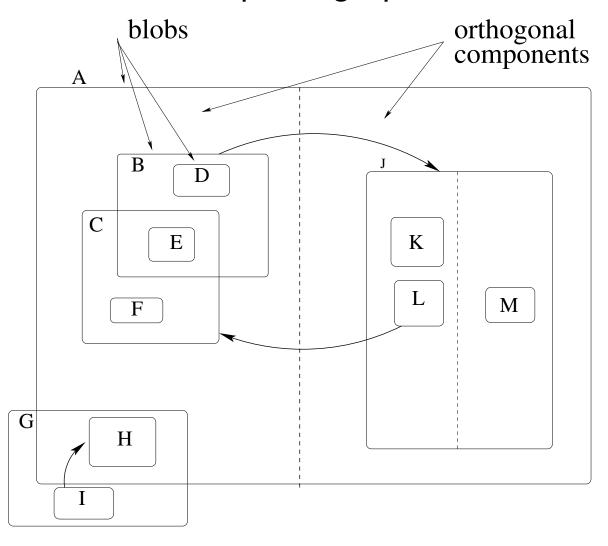
## Meaningless constructs





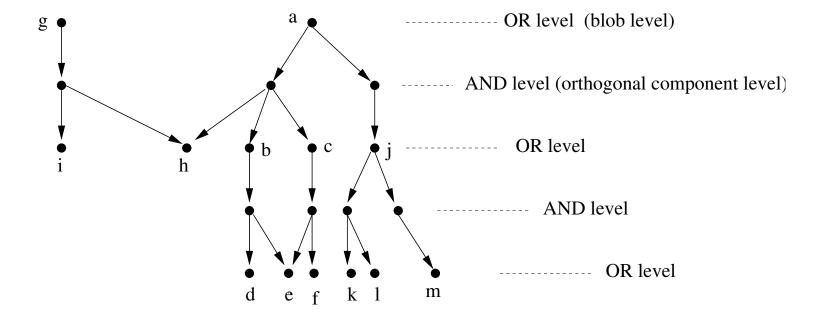
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## Simple Higraph



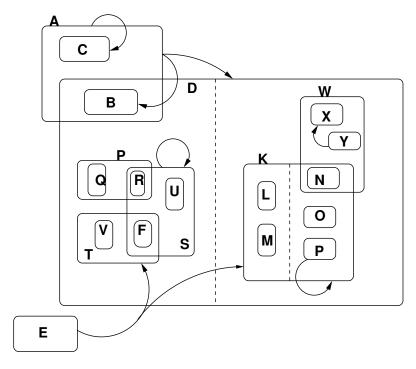
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#### Induced Acyclic Graph (blob/orth comp alternation)



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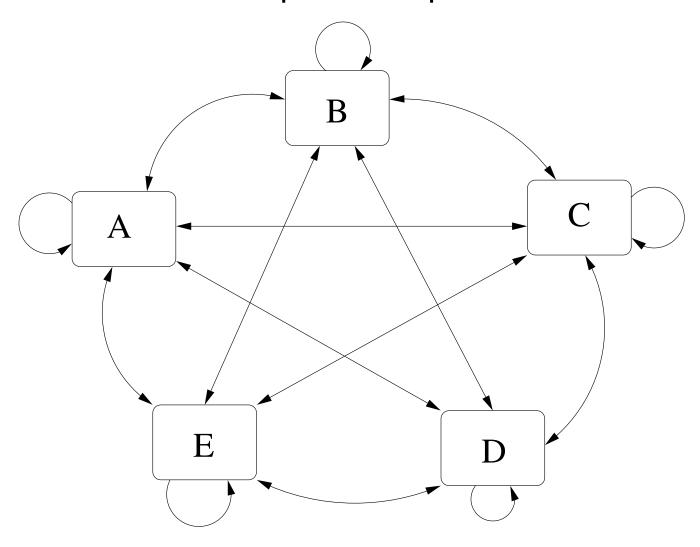
## Adding (hyper) edges



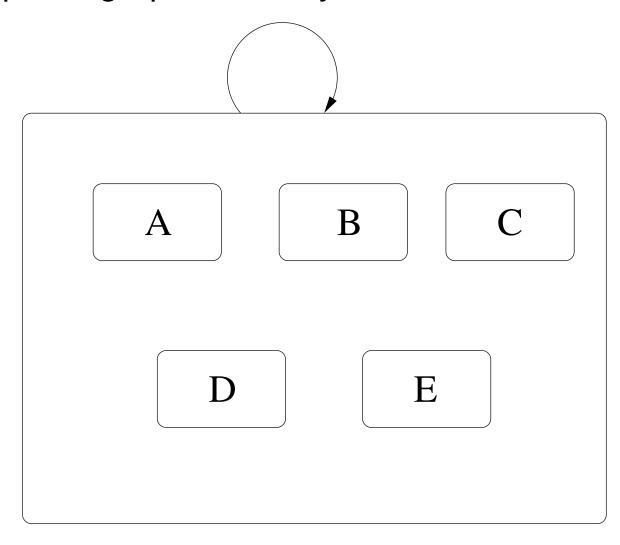
- hyperedges
- attach to contour of any blob
- inter-level possible

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## Clique Example

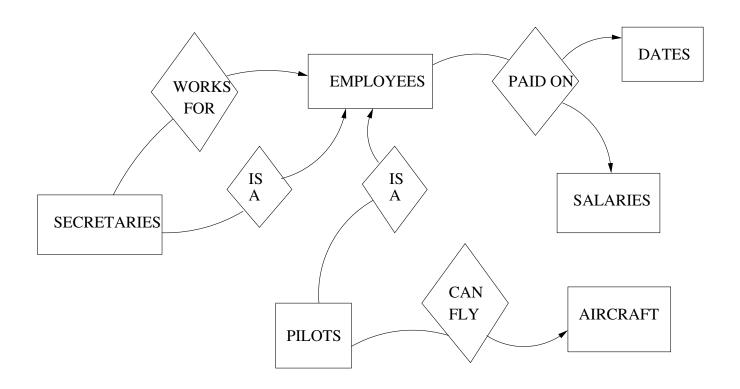


## Clique: higraph with fully connected semantics



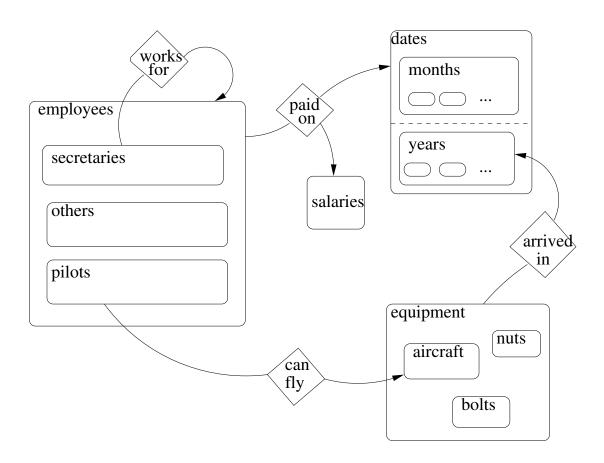
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## Entity Relationship Diagram (is-a)



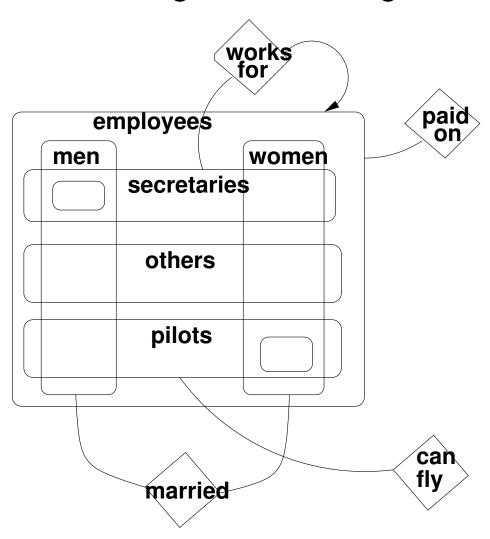
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## Higraph version of E-R diagram



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## Extending the E-R diagram



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#### Higraph applications

- E-R diagrams
- data-flow diagrams (activity diagrams)
  edges represent (flow of) data
- inheritance
- Statecharts

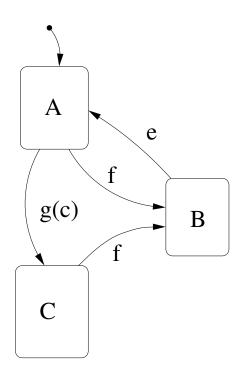
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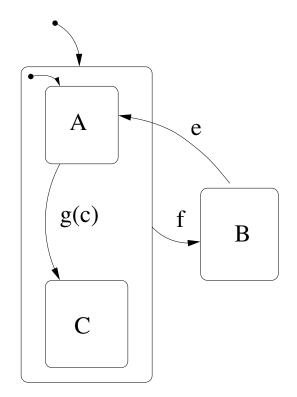
# StateCharts = state diagrams + depth + orthogonality + broadcast

- Reactive Systems (event driven, react to internal and external stimuli)
- like Petri Nets, CSP, CCS, sequence diagrams, ...
- graphical but formal and rigourous for
  - analysis
  - code generation
- solve FSA problems:
  - flat  $\Rightarrow$  hierarchy  $\Rightarrow$  re-use
  - represent large number of transitions concisely
  - represent large number of states concisely
  - sequential  $\Rightarrow$  concurrent

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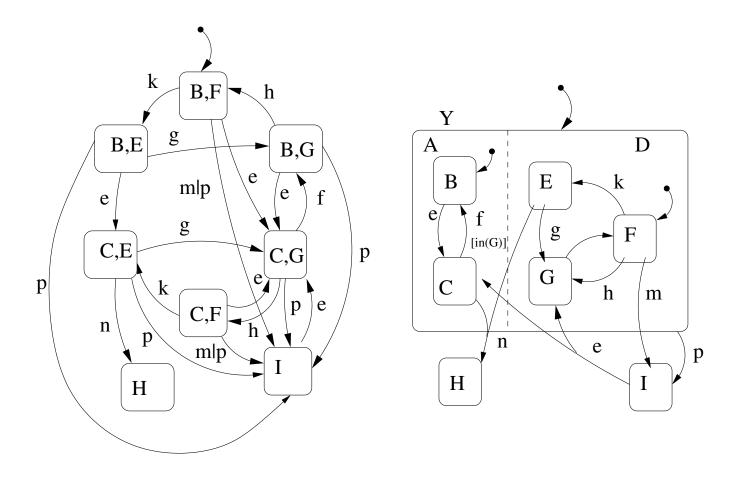
## Depth (XOR)





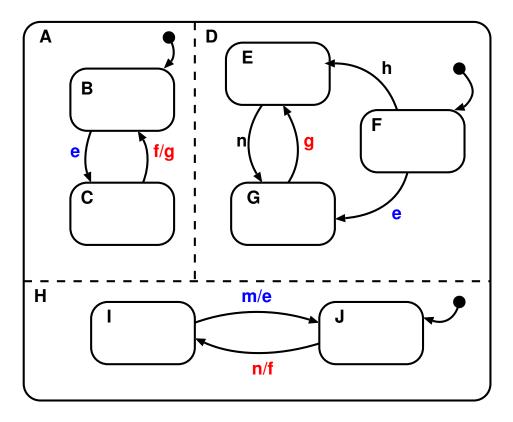
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## Orthogonality (AND), flattening ⇒ semantics



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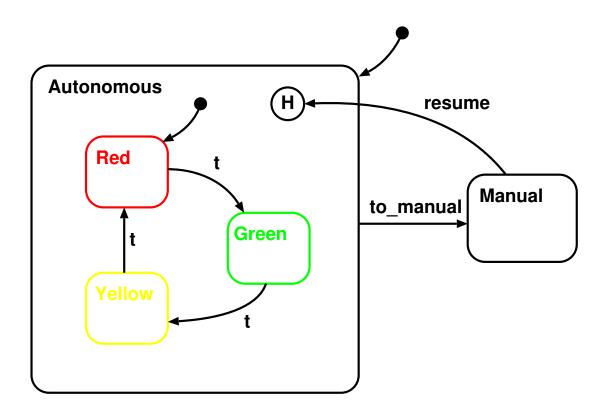
## Broadcasting (output events)



Input Segment: nmnn

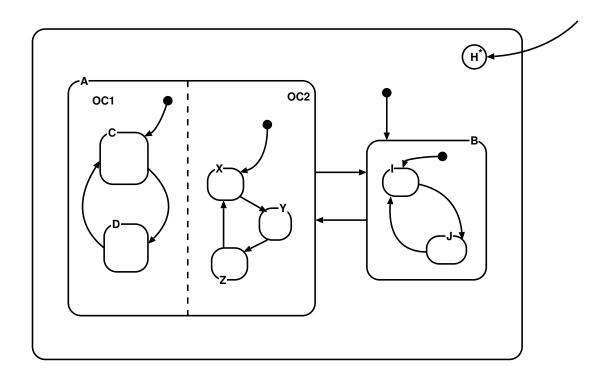
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## **History States**



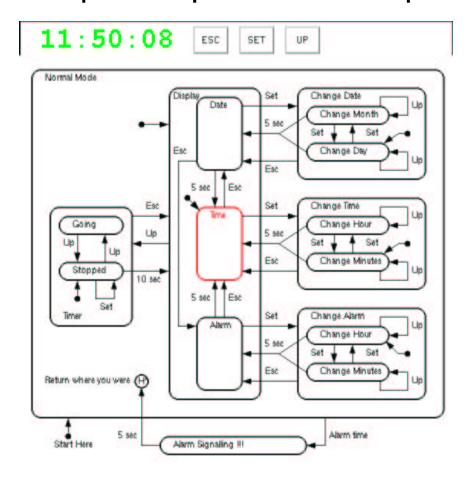
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## **Deep History**



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#### Simple Stopwatch Example

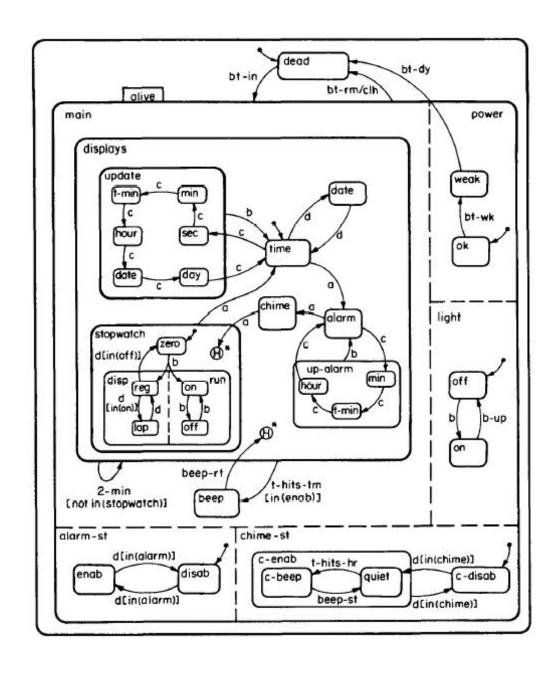


http://www.xjtek.com/products/xjcharts/demo/

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## Stopwatch Example

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#### Messages

- object.method(...) synchronous method invocation
- object->method(...) queued, a-synchronous

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