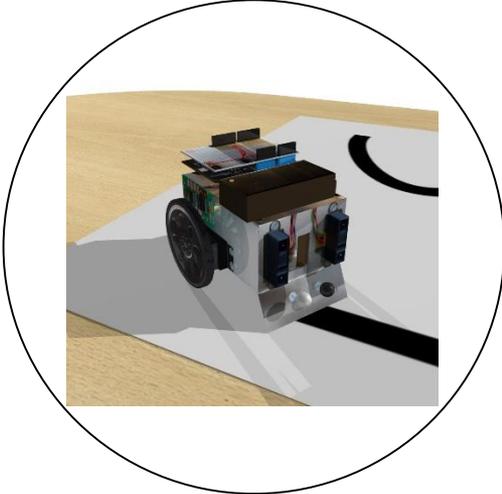
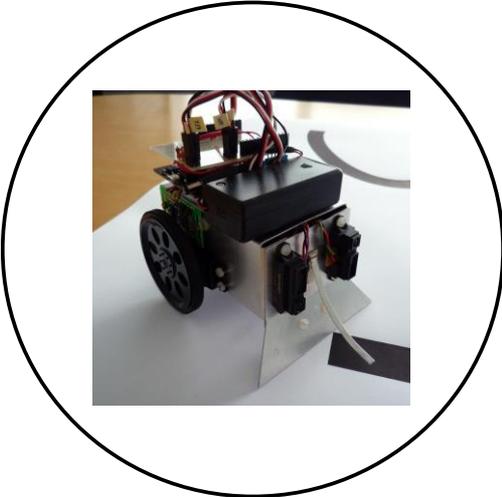


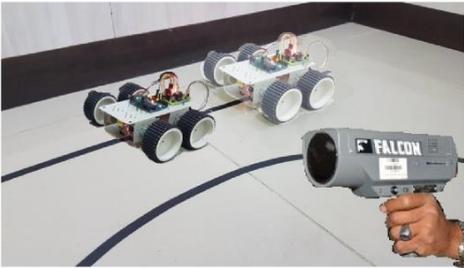
Co-simulation

Cláudio Gomes

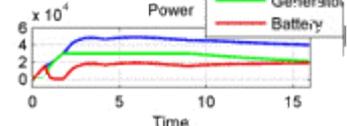
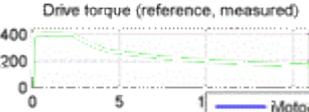
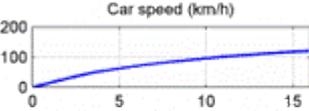
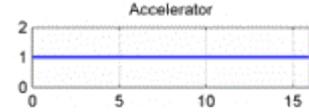
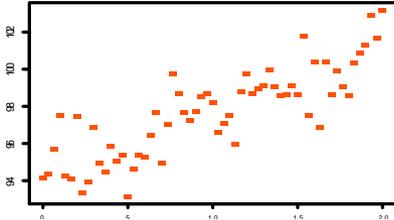
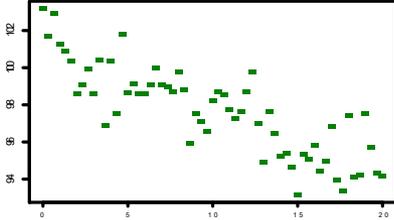
Simulation



Experimentation



Simulation

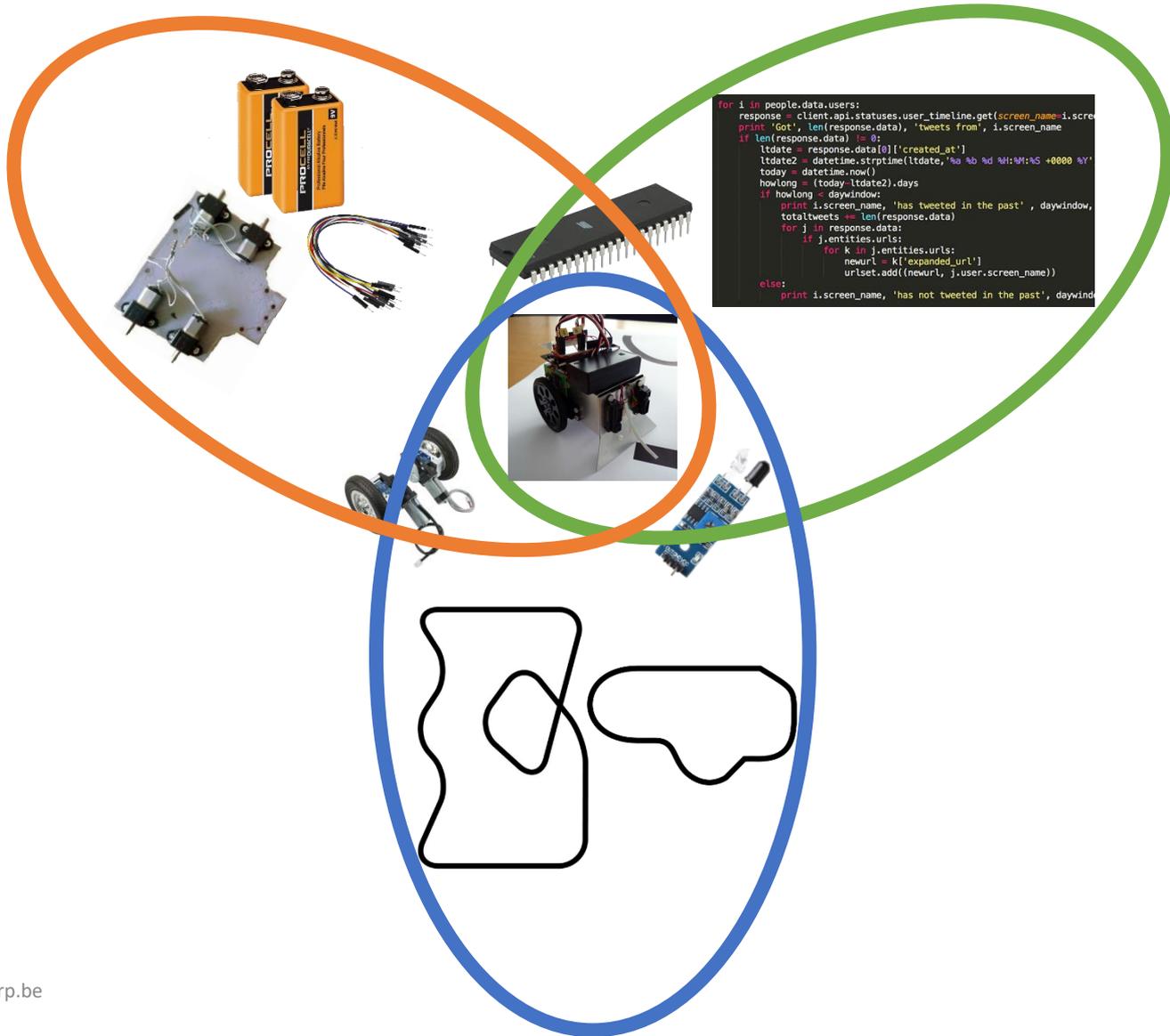


Simulation is useful



<https://www.slashgear.com/virtual-simulation-and-robotic-butt-named-patrick-offers-med-students-hands-on-practice-13305334/>

Co-Simulation



Co-Simulation

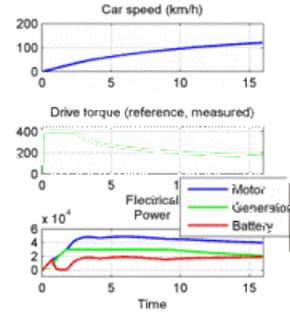
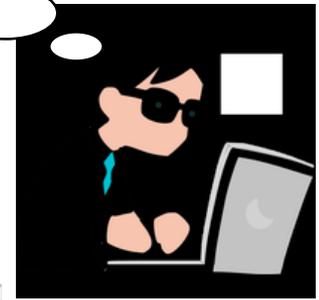
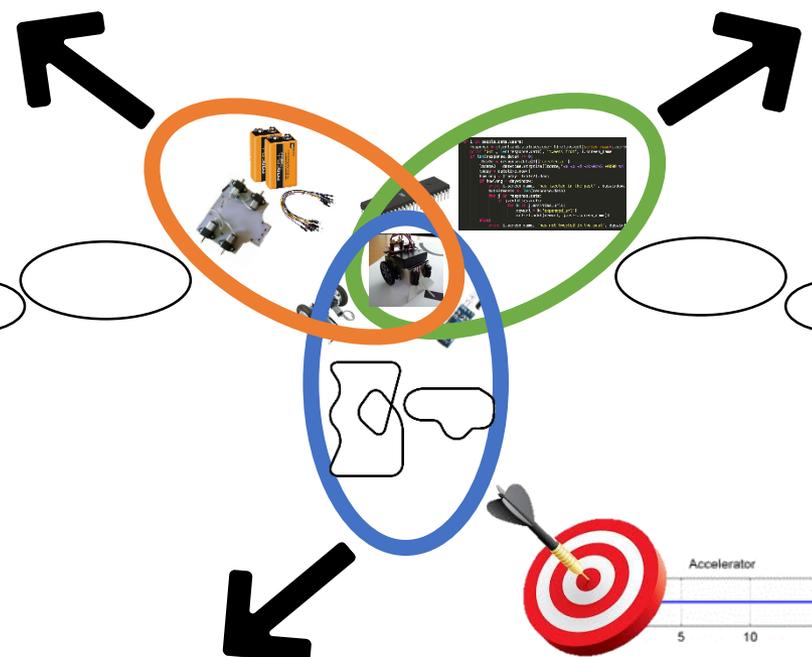
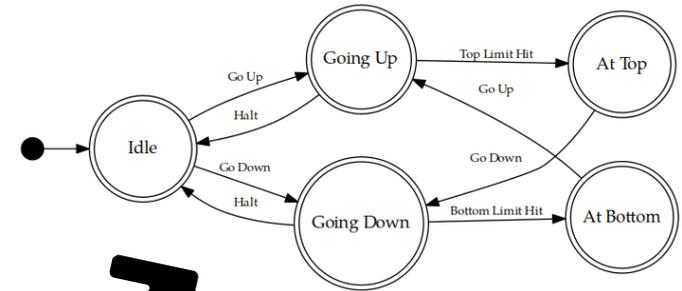
$$Y(t) = A(t) K(t)^{\frac{1}{3}} Ly(t)^{\frac{2}{3}}$$

$$\frac{d}{dt} K(t) = sY(t) - dK(t)$$

$$\frac{d}{dt} A(t) = zA(t) La(t)$$

$$Ly(t) + La(t) = L$$

$$La(t) = lL$$



Time	Data:1	Data:2	Data:3	Data:4	Data:5	Data:6	Data:7	Data:8	Data:9	Data:10
0	0	0	0	0	0	0	0	0	0	0
0.1000	0	0	0	0	0	0	0	0	0	0
0.2000	0	0	0	0	0	0	0	0	0	0
0.3000	0	0	0	0	0	0	0	0	0	0
0.4000	0	0	0	0	0	0	0	0	0	0
0.5000	32.1101	36.9662	42.1508	47.7188	53.6885	59.9579	66.7055	73.7890	81.2129	89.0659
0.6000	64.2203	73.9324	84.3016	95.4375	107.3770	119.9159	133.4111	147.5779	162.4256	178.1318
0.7000	96.3304	110.8985	126.4525	143.1563	161.0655	179.8738	200.1166	221.3669	243.6388	267.1976
0.8000	128.4405	147.8647	168.6033	190.8751	214.7540	239.8317	266.8222	295.1559	324.8517	356.2635
0.9000	160.5507	184.8309	210.7541	238.5939	268.4425	299.7897	333.5277	368.9449	406.0646	445.3294
1.0000	192.6608	221.7971	252.9049	286.3126	322.1310	359.7476	400.2333	442.7338	487.2775	534.3953
1.1000	192.6608	221.7971	252.9049	286.3126	322.1310	359.7476	400.2333	442.7338	487.2775	534.3953
1.2000	192.6608	221.7971	252.9049	286.3126	322.1310	359.7476	400.2333	442.7338	487.2775	534.3953

Co-Simulation

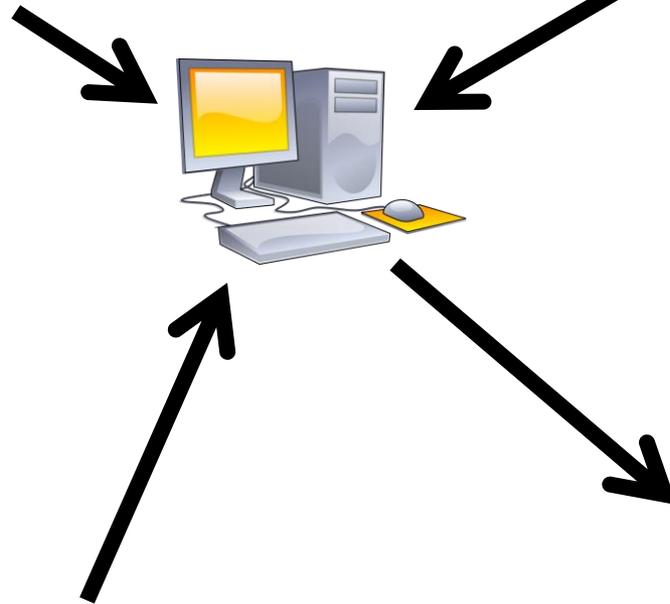
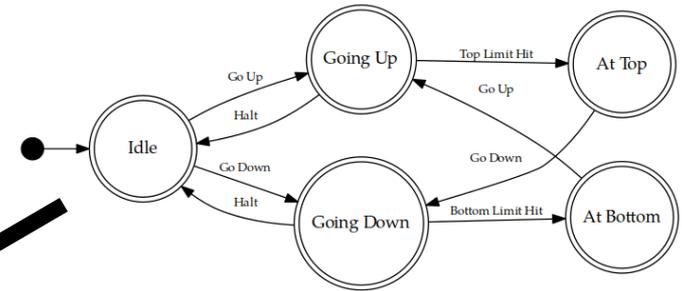
$$Y(t) = A(t) K(t)^{\frac{1}{3}} Ly(t)^{\frac{2}{3}}$$

$$\frac{d}{dt} K(t) = sY(t) - dK(t)$$

$$\frac{d}{dt} A(t) = zA(t) La(t)$$

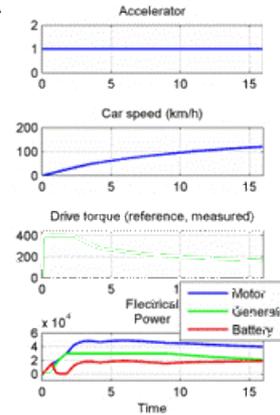
$$Ly(t) + La(t) = L$$

$$La(t) = lL$$

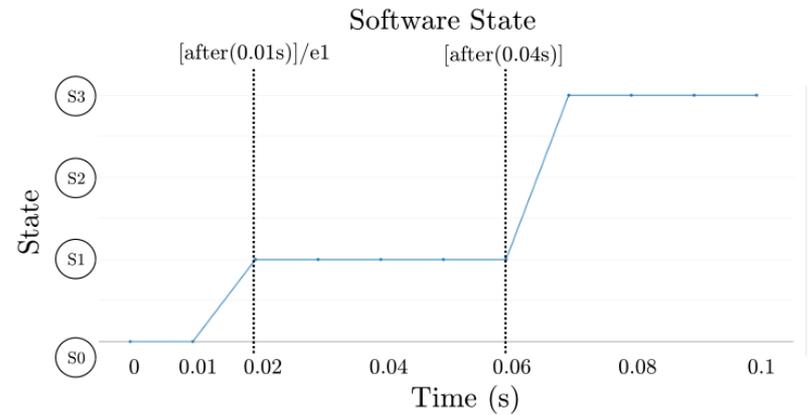
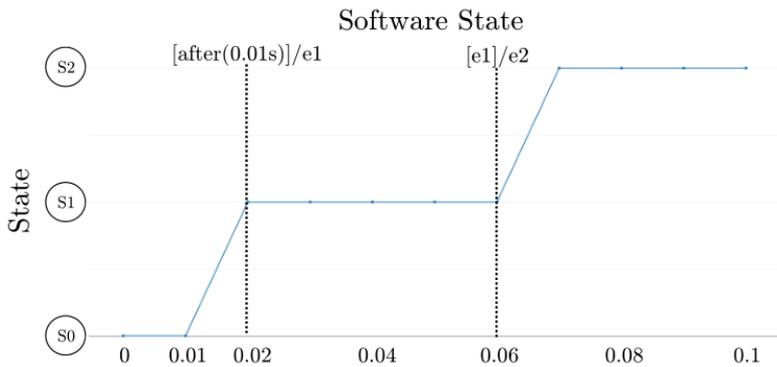
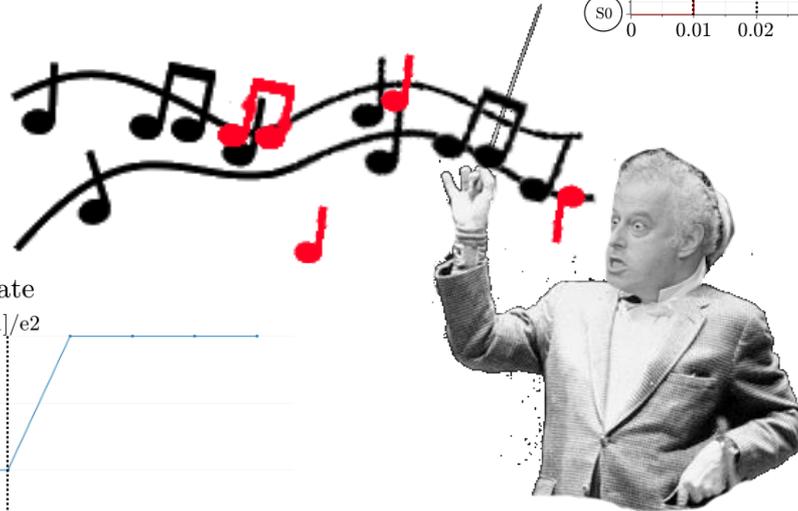
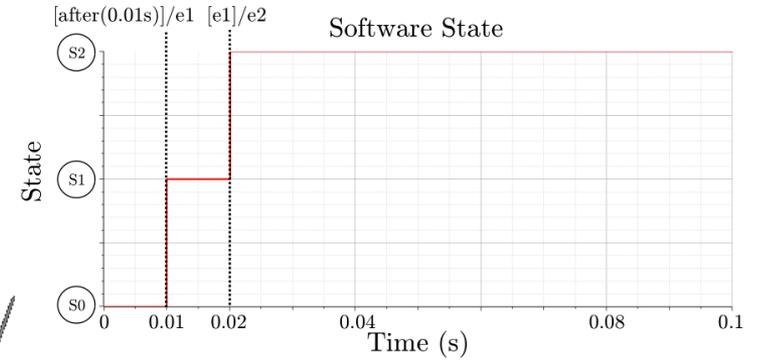


Time series name:

Time	Data:1	Data:2	Data:3	Data:4	Data:5	Data:6	Data:7	Data:8	Data:9	Data:10
0	0	0	0	0	0	0	0	0	0	0
0.1000	0	0	0	0	0	0	0	0	0	0
0.2000	0	0	0	0	0	0	0	0	0	0
0.3000	0	0	0	0	0	0	0	0	0	0
0.4000	0	0	0	0	0	0	0	0	0	0
0.5000	32.1101	36.9662	42.1508	47.7188	53.6885	59.9579	66.7055	73.7890	81.2129	89.0659
0.6000	64.2203	73.9324	84.3016	95.4375	107.3770	119.9159	133.4111	147.5779	162.4256	178.1318
0.7000	96.3304	110.8985	126.4525	143.1563	161.9655	179.8738	200.1166	221.3669	243.6388	267.1976
0.8000	128.4405	147.8647	168.6033	190.8751	214.7940	239.8317	266.8222	295.1559	324.8517	356.2635
0.9000	160.5507	184.8309	210.7541	238.5939	268.4425	299.7897	333.5277	368.9449	406.0646	445.3294
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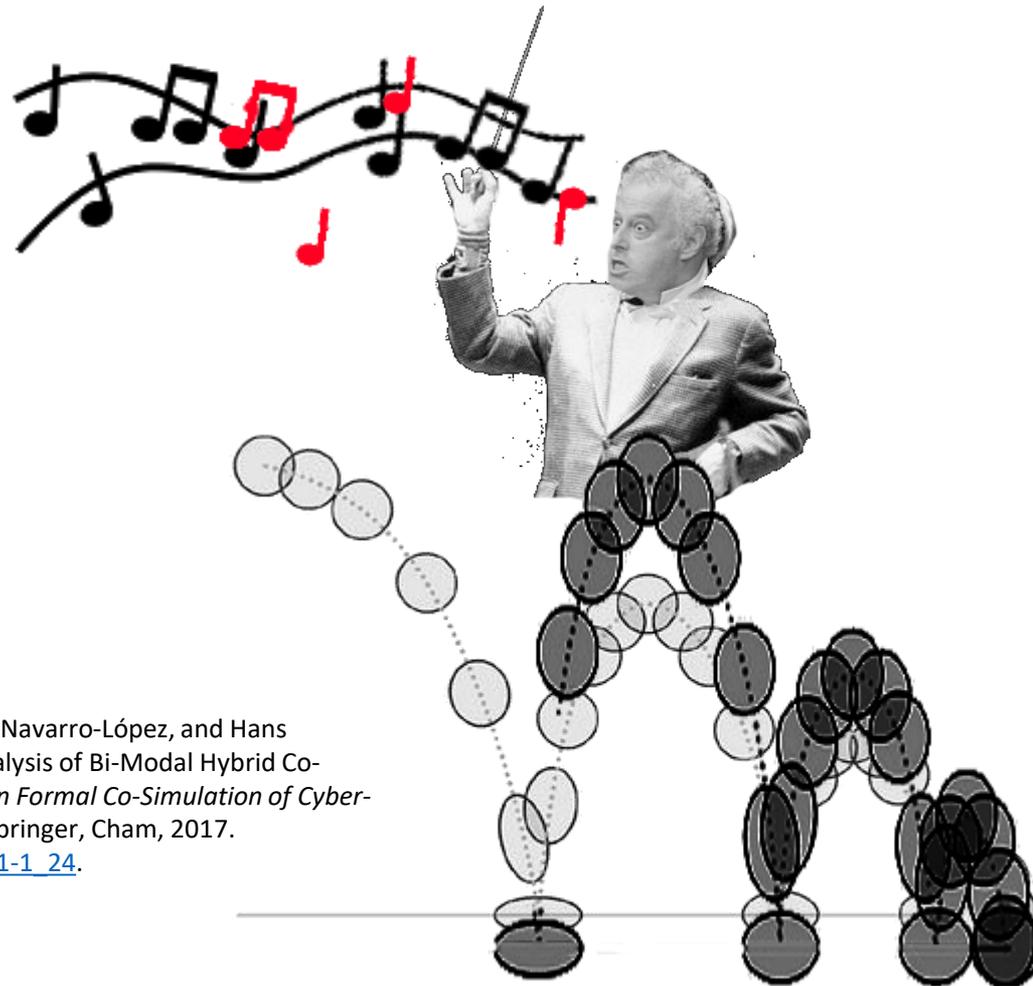


Challenge



Thule, Casper, Cláudio Gomes, Julien Deantoni, Peter Gorm Larsen, Jörg Brauer, and Hans Vangheluwe. "Towards Verification of Hybrid Co-Simulation Algorithms." In *2nd Workshop on Formal Co-Simulation of Cyber-Physical Systems*, to be published. Toulouse, France: Springer, Cham, 2018.

Challenge



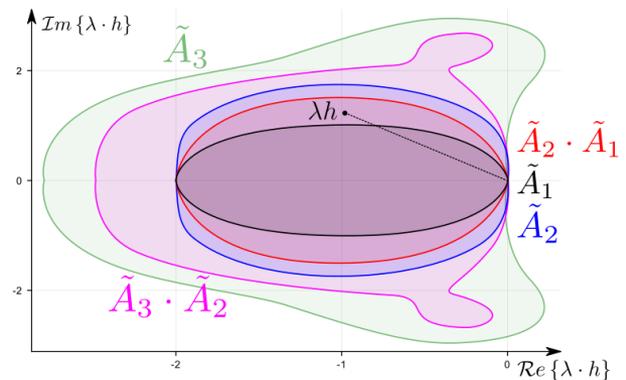
Gomes, Cláudio, Paschalis Karalis, Eva M. Navarro-López, and Hans Vangheluwe. "Approximated Stability Analysis of Bi-Modal Hybrid Co-Simulation Scenarios." In *1st Workshop on Formal Co-Simulation of Cyber-Physical Systems*, 345–60. Trento, Italy: Springer, Cham, 2017.

https://doi.org/10.1007/978-3-319-74781-1_24.

Challenge



Gomes, Cláudio, Benoît Legat, Raphaël Jungers, and Hans Vangheluwe.
“Minimally Constrained Stable Switched Systems and Application to Co-Simulation.” In *IEEE Conference on Decision and Control*, to be published.
Miami Beach, FL, USA, 2018.



Thank you!

Questions?

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[*http://msdl.cs.mcgill.ca/people/claudio*](http://msdl.cs.mcgill.ca/people/claudio)