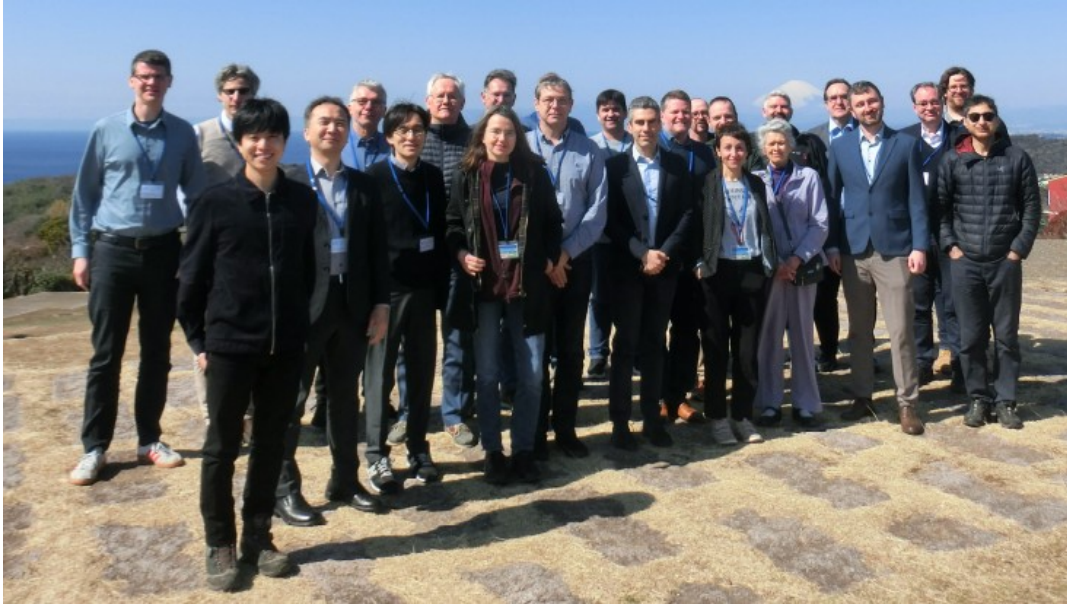


Relating (Multi-Paradigm) Modelling Concepts

Joachim Denil and Hans Vangheluwe

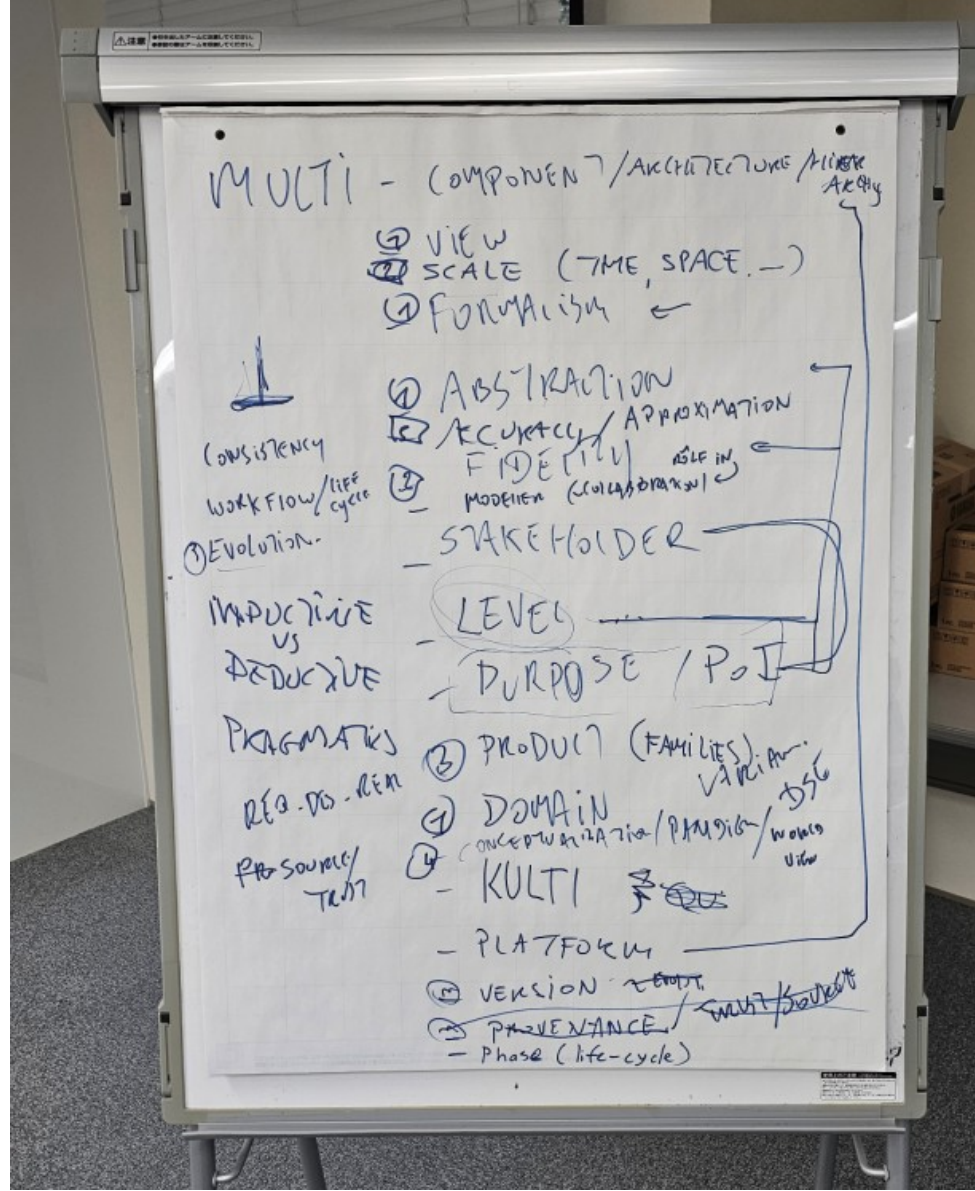
Tuesday 25 March 2025

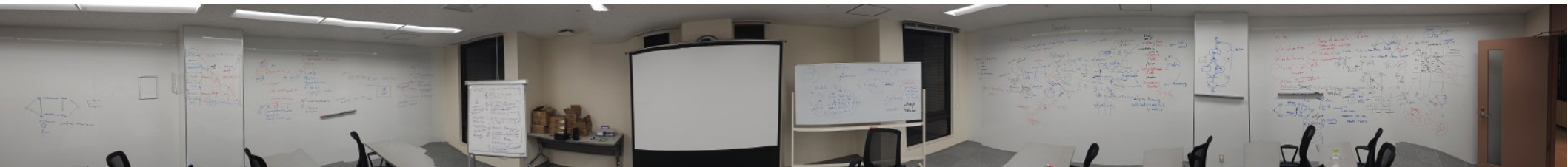


Multi-*

==

Ambitious





Paradigm

M. Botz

Conceptualization defines

Concept

Abstraction

Domain (Discipline)

+

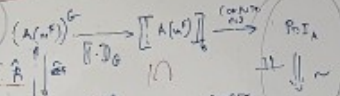
- rules
- axioms
- analyses
- decision procedure

Commonly used

View (deriving transformation)

Formalism

Abstraction A



Formalism

Models

Pragmatics

Languages

Abstraction

Multi-to-one relation

Special case composition

TYPE \neq ABSTRACTION

KIRSELL

Pragmatics

C.S

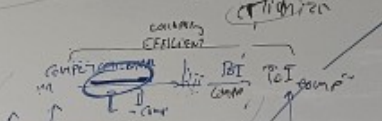
WORKATION

TARIT

GOAL/PURPOSE CRITERION

Real world system + PoI

Multi-Level



Validity

Approximation

Fidelity

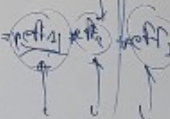
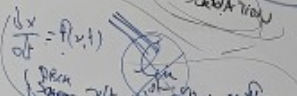
Accuracy

Fidelity \Rightarrow Accuracy

Multi-level \Rightarrow Multi-scale

\Rightarrow Multi- \neq

execution of the semantics



Herbert Stachowiak

*Allgemeine
Modelltheorie*

Springer-Verlag
Wien New York

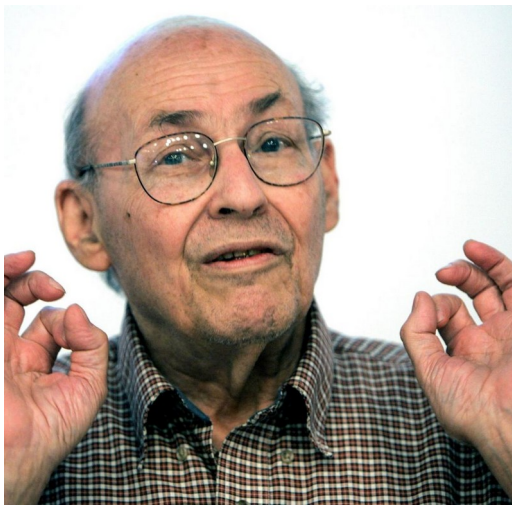


1973

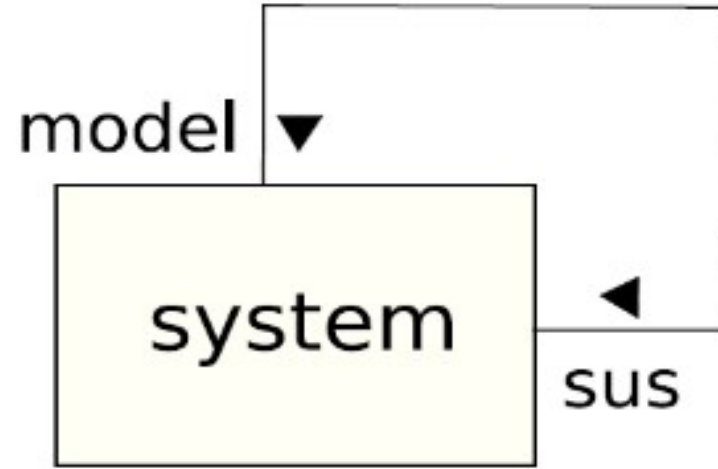


“Model” Features

mapping feature	A model is based on an original. ⁴
reduction feature	A model only reflects a (relevant) selection of an original’s properties.
pragmatic feature	A model needs to be usable in place of an original with respect to some purpose.



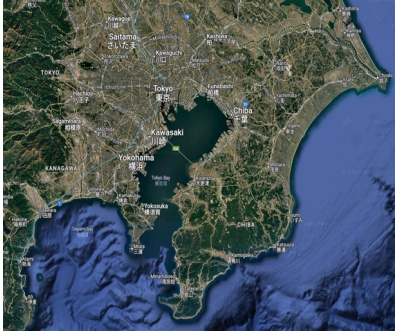

Marvin L. Minsky





To an observer B, an object A^* is a model of an object A to the extent that B can use A^* to answer questions that interest him about A.

Matter, Mind and Models



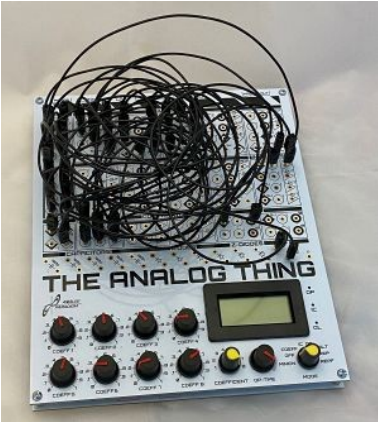
System under Study (SuS) vs. Model

	Real-World Model	Virtual Model
Real-World SuS	 	
Virtual SuS		




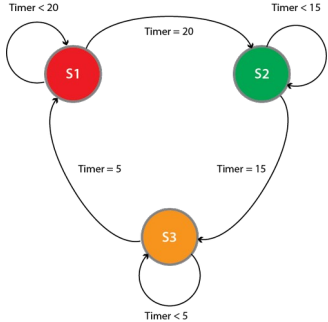
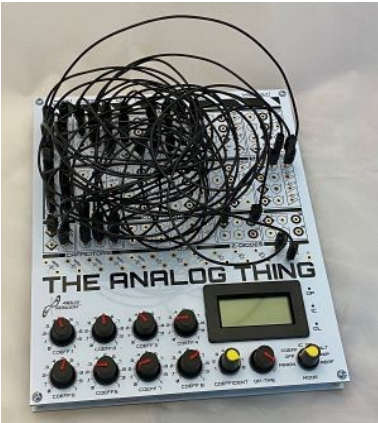
System under Study (SuS) vs. Model

	Real-World Model	Virtual Model
Real-World SuS	 	
Virtual SuS		




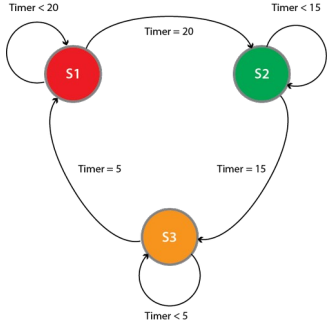
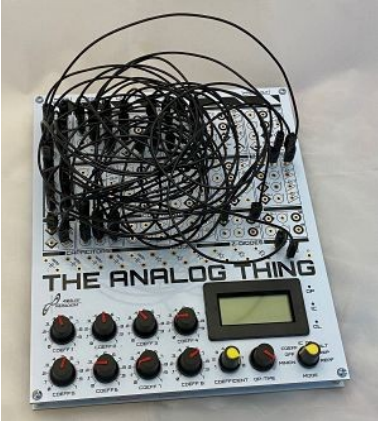
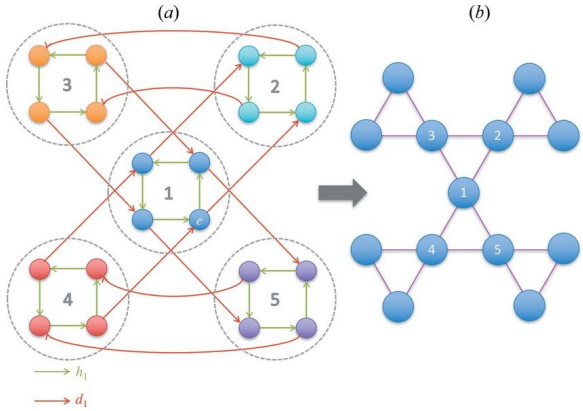
System under Study (SuS) vs. Model

	Real-World Model	Virtual Model
Real-World SuS	 	
Virtual SuS	$\frac{dx}{dt} = \alpha x - \beta xy,$ $\frac{dy}{dt} = -\gamma y + \delta xy,$ 	

System under Study (SuS) vs. Model

	Real-World Model	Virtual Model
Real-World SuS	 	 
Virtual SuS	$\frac{dx}{dt} = \alpha x - \beta xy,$ $\frac{dy}{dt} = -\gamma y + \delta xy,$ 	

System under Study (SuS) vs. Model

	Real-World Model	Virtual Model
Real-World SuS	 	 
Virtual SuS	 $\frac{dx}{dt} = \alpha x - \beta xy,$ $\frac{dy}{dt} = -\gamma y + \delta xy,$	

Triangle of Reference, Semiotic Triangle

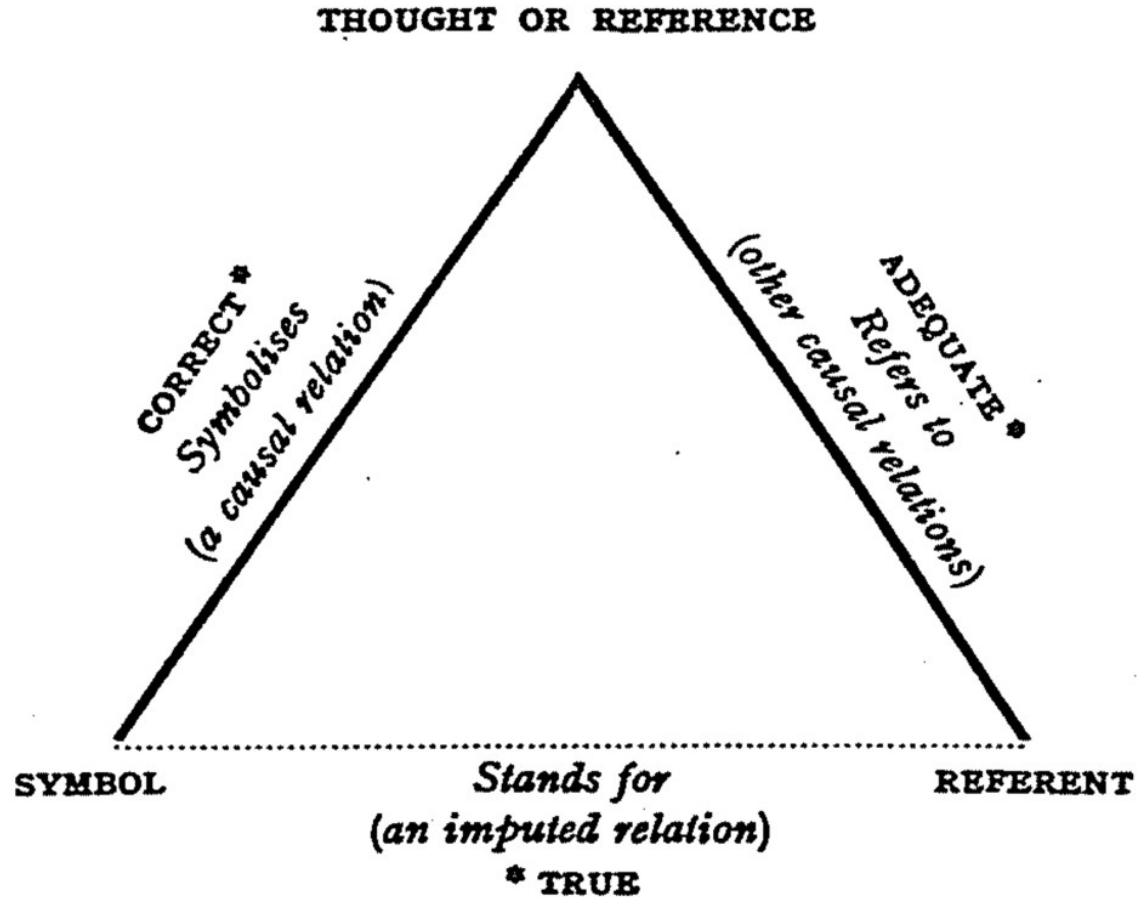
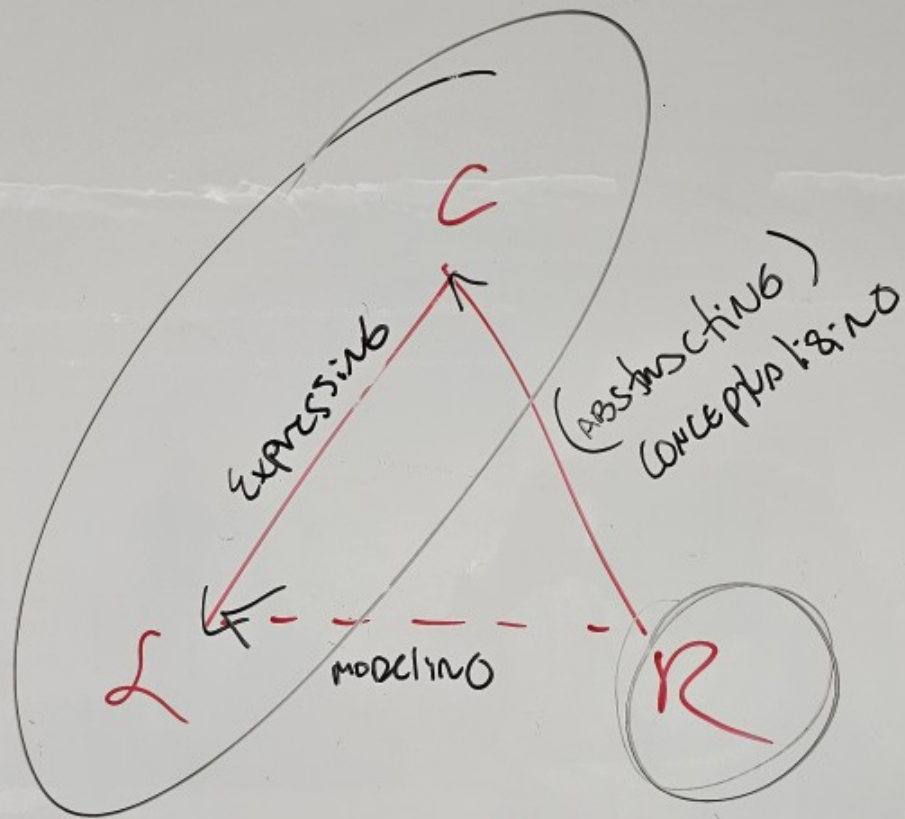


Figure taken from page 11, [The Meaning of Meaning: A Study of the Influence of Language upon Thought and of the Science of Symbolism](#), 1923, was co-authored by [C. K. Ogden](#) and [I. A. Richards](#), [Magdalene College, University of Cambridge](#)

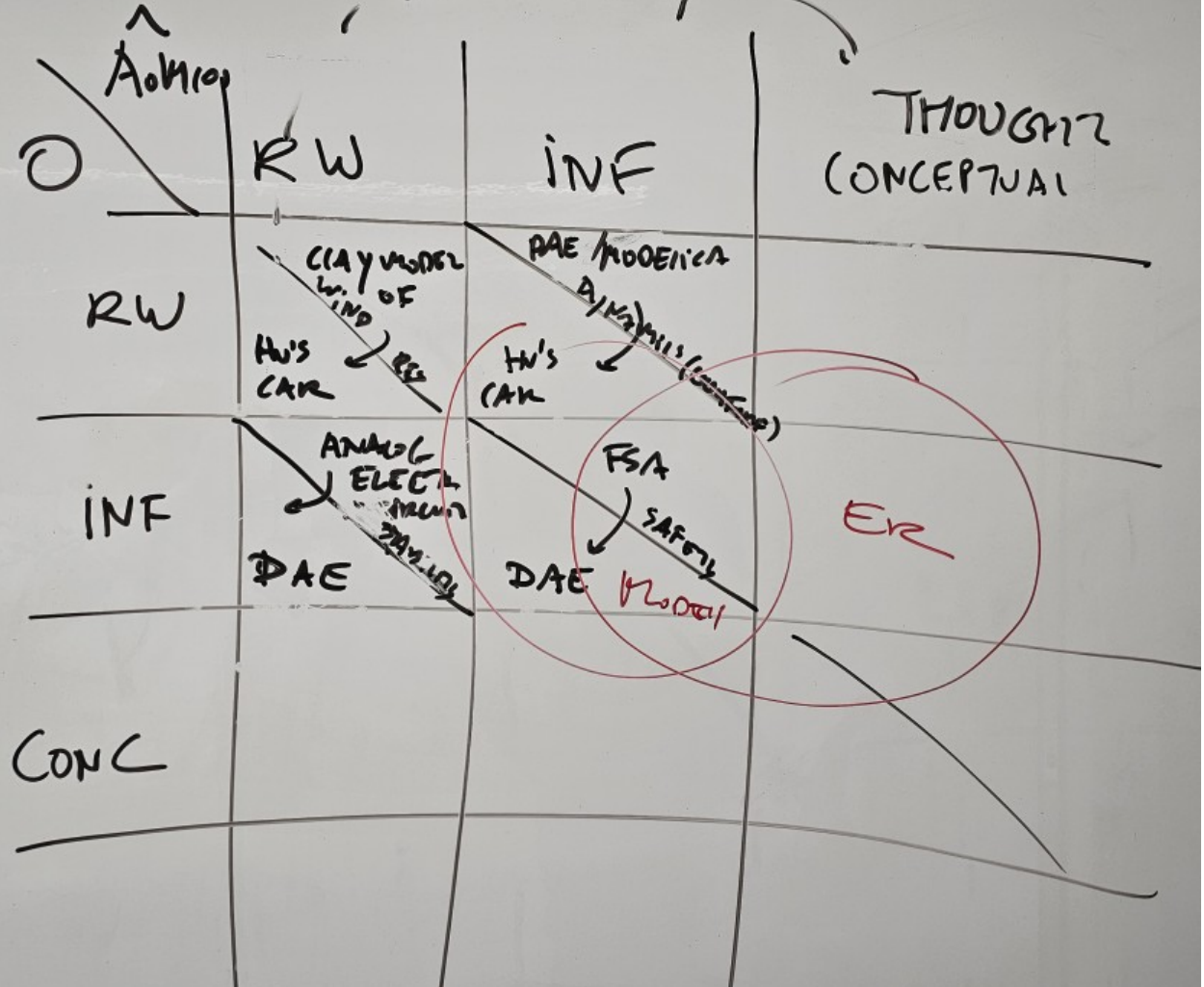


Modeling = Conceptualizing ; Expressing
(including representing in language)

1/27. PROP. / PURPOSE

MODELLING = ACTIVITY

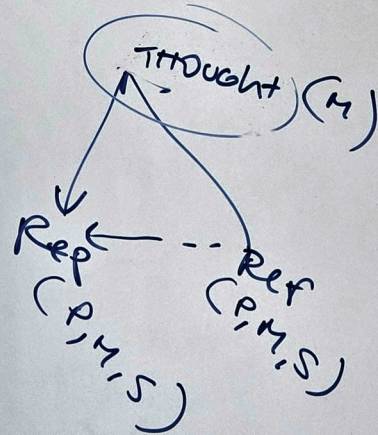
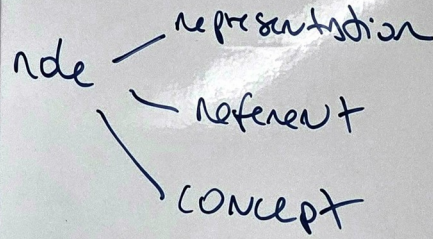
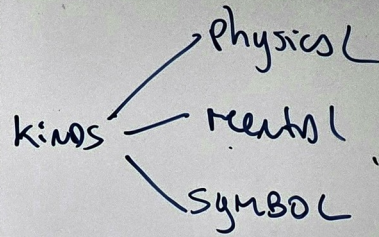
MEDIATED BY



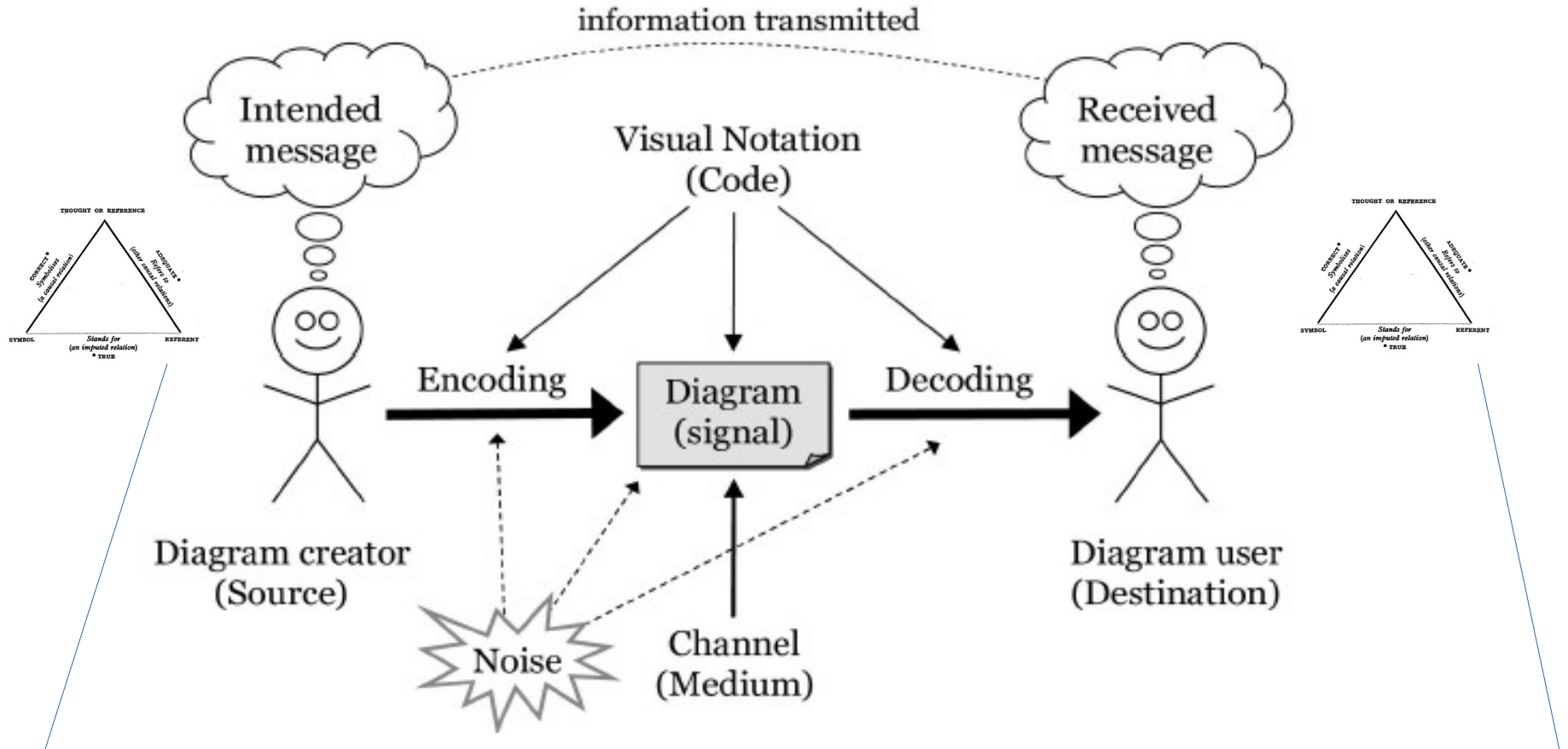
kinos — physical
 — mental
 — symbol

nde — representation
 — referent
 — concept

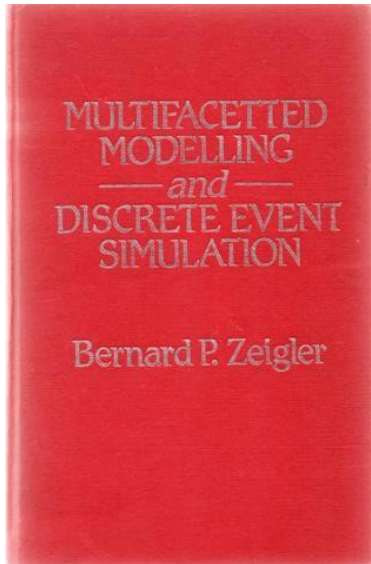
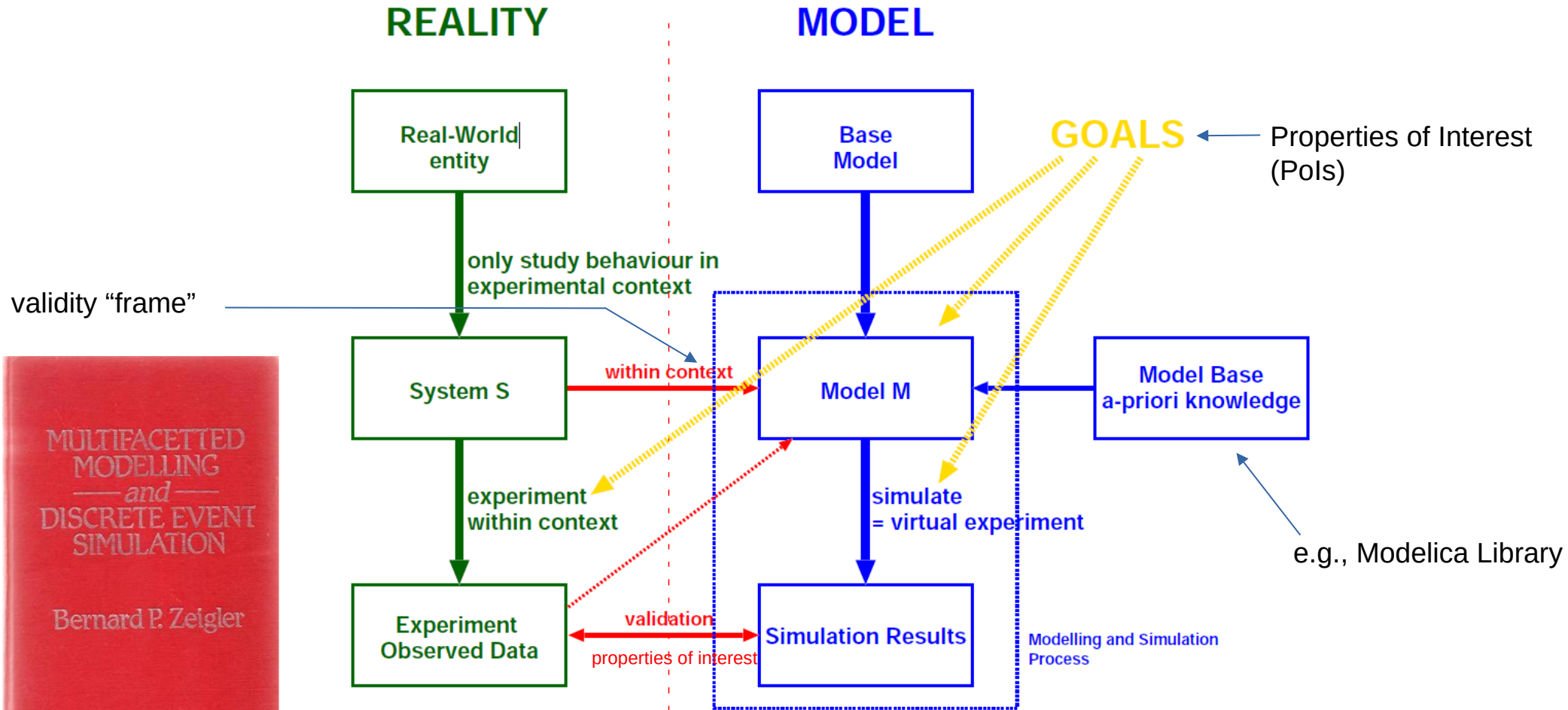




Moody "Physics of Notation": communication theory

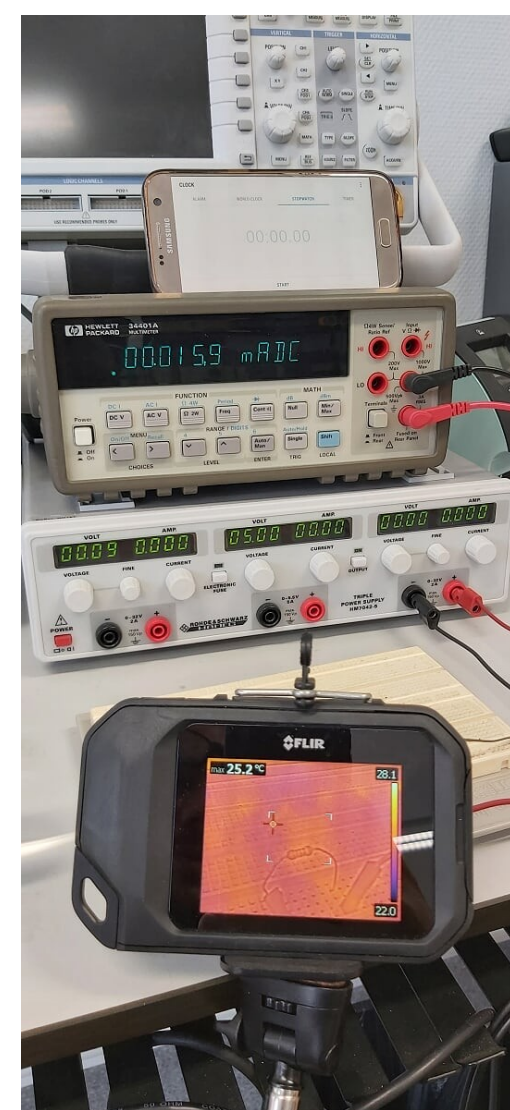
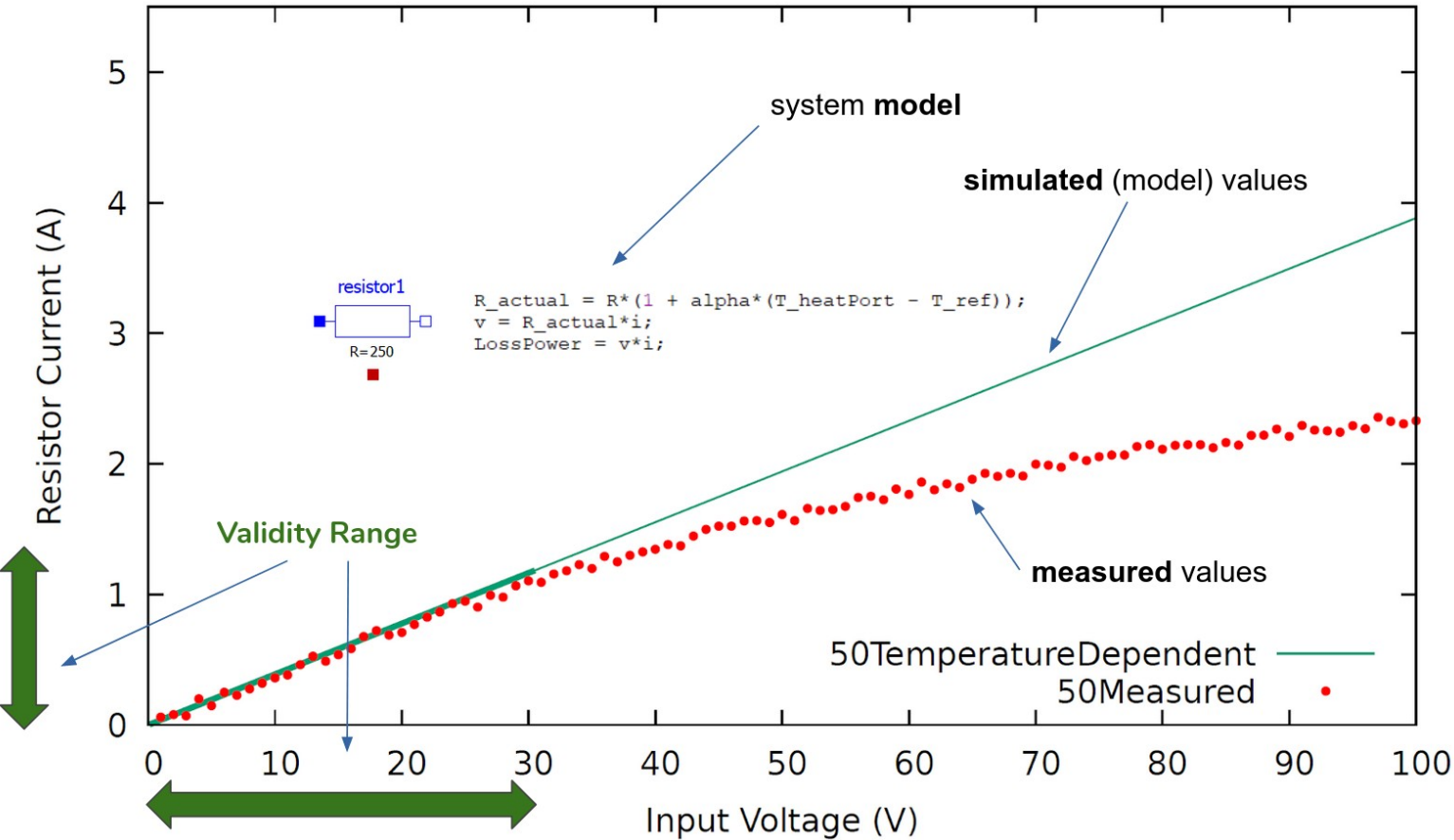


purpose of modelling: substitutability (engineering), explainability (science)



Bernard P. Zeigler. *Multi-faceted Modelling and Discrete-Event Simulation*. Academic Press, 1984.

A Resistor Model's Validity Range



Abstract (In)Validity Frame

The (possibly infinite) **Set of Experiments e** for which the **Distance d** between the obtained (computed) **Properties of Interest P_{OI}** from e carried out in the **REAL** world and e carried out in the **VIRTUAL** world is (larger)smaller than a **threshold Tr** .

$$AVF_{\mu_n} \cup AIF_{\mu_n} = \mathbb{U}_{\mu_n}$$

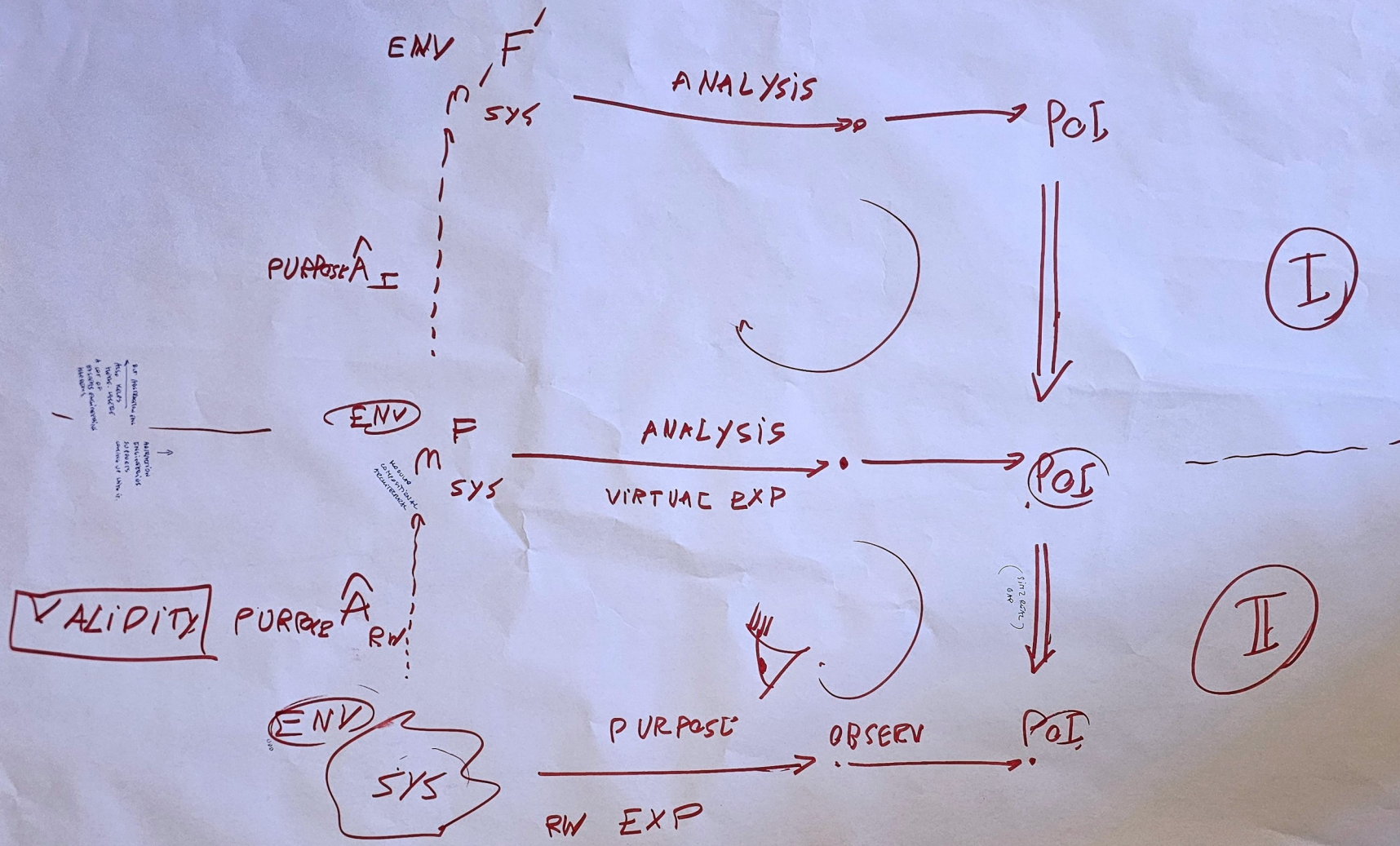
$$AVF_{\mu_n} \cap AIF_{\mu_n} = \emptyset$$

Thanks to Rhys Goldstein
for the notion of abstract
frame  AUTODESK.

Concrete (In)Validity Frame

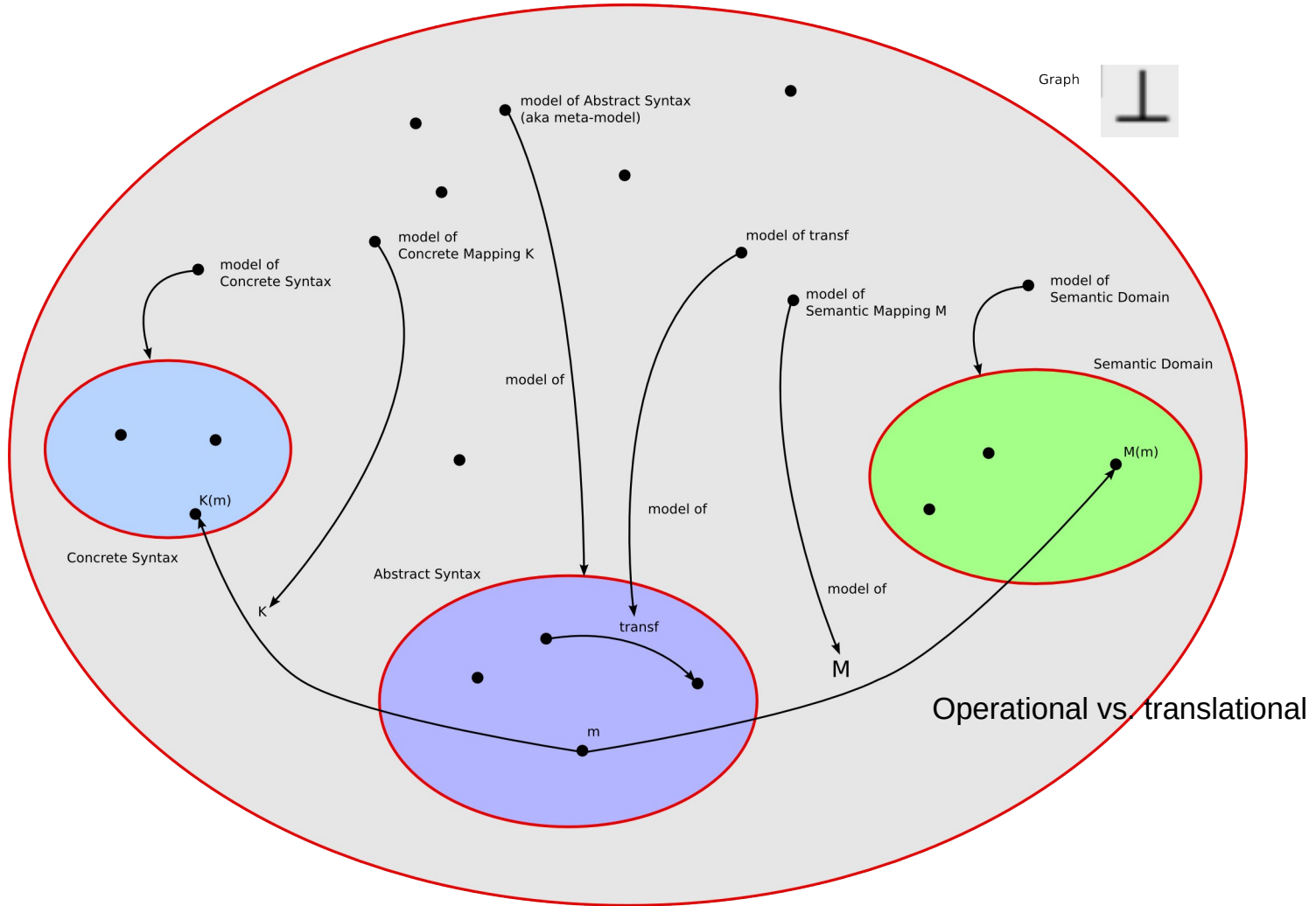
- Concrete Validity Frame (CVF)
The finite set of **performed experiments** in which a model is valid
- Concrete Invalidity Frame (CIF)
The finite set of **performed experiments** in which a model is invalid

$$CVF_{\mu_n} \cap CIF_{\mu_n} = \emptyset$$

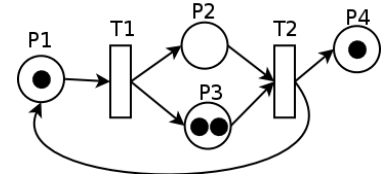
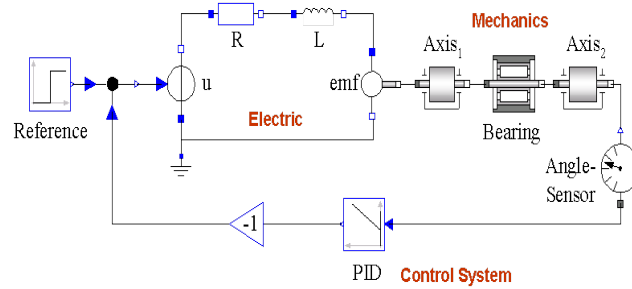
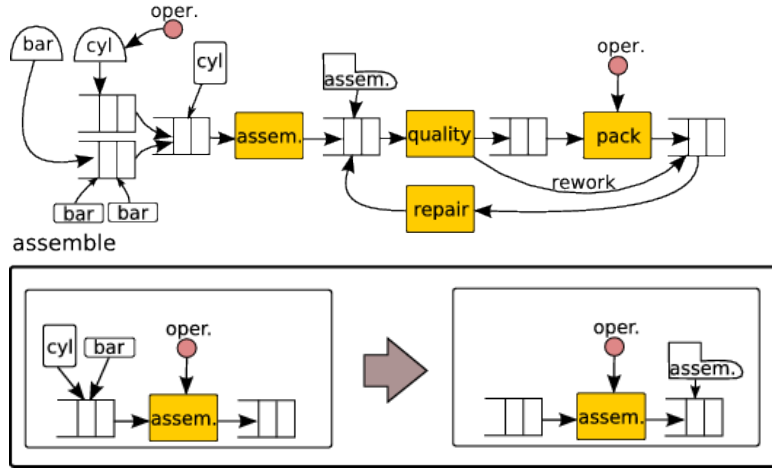
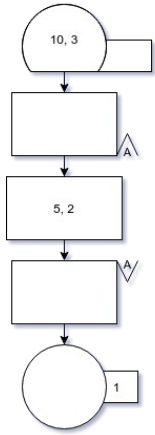


++ Workflows
 ++ Inductive vs. Deductive

Explicit Modelling of Modelling Languages/Formalisms (++ debugging)



Using the most appropriate formalism(s)



1. for $\{0 \leq z \leq z_f - \sigma\}$:

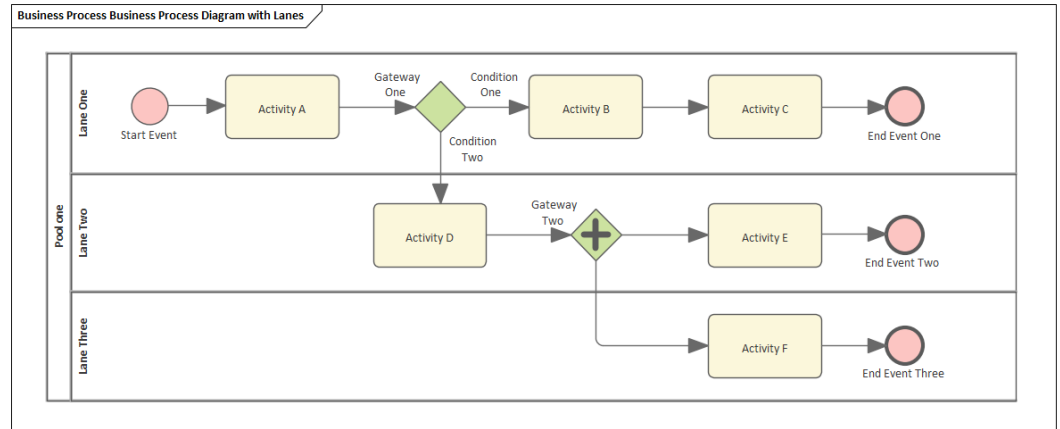
$$\frac{\partial X(z,t)}{\partial t} = - \left[(1 - nX(z,t)) v_0 e^{-nX(z,t)} + \frac{Q_n(t)}{A} \right] \frac{\partial X(z,t)}{\partial z} + D_0 \frac{\partial^2 X(z,t)}{\partial z^2};$$

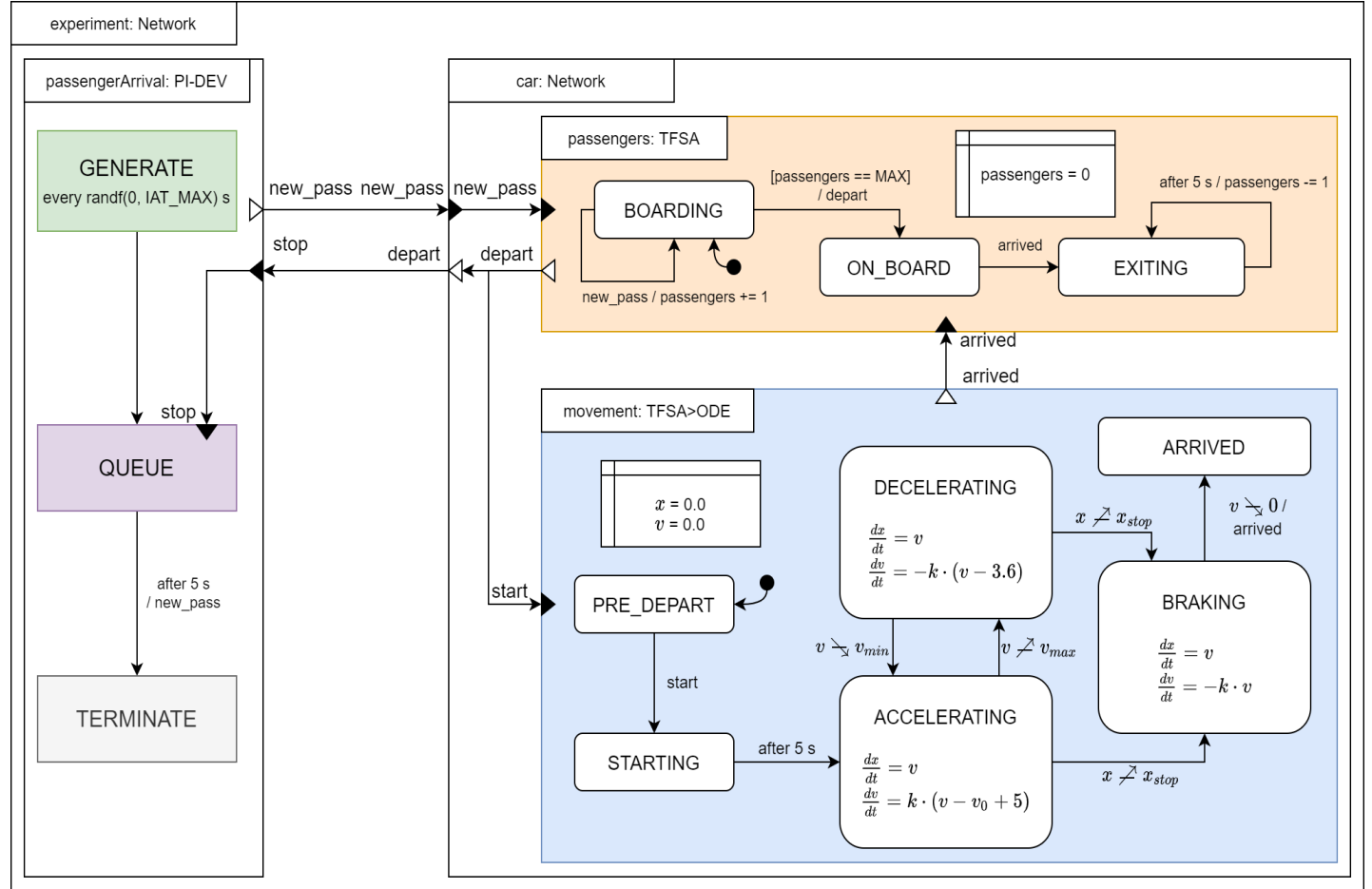
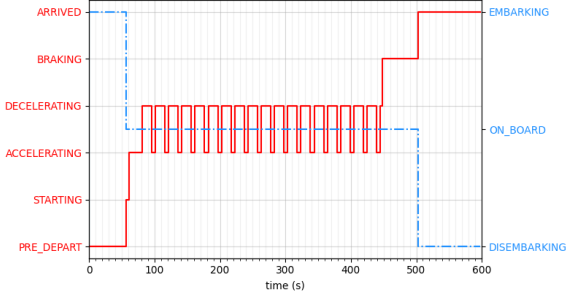
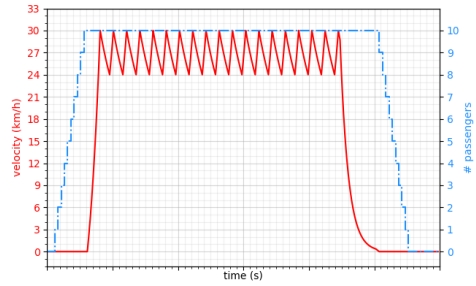
2. for $\{z_f - \sigma < z < z_f + \sigma\}$:

$$\frac{\partial X(z,t)}{\partial t} = - \left[(1 - nX(z,t)) v_0 e^{-nX(z,t)} + \frac{Q_n(t)}{A} \right] \frac{\partial X(z,t)}{\partial z} + X_f(t) \frac{Q_f(t)}{A} \frac{1}{2\sigma} + D_0 \frac{\partial^2 X(z,t)}{\partial z^2};$$

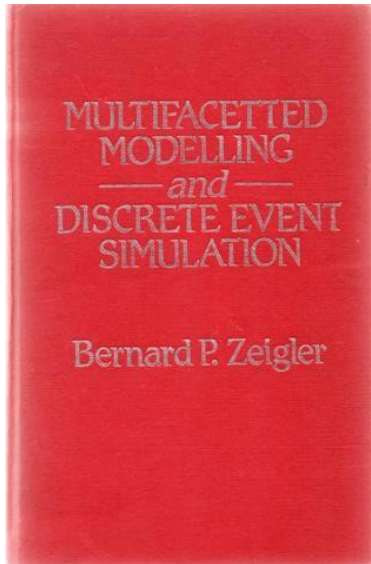
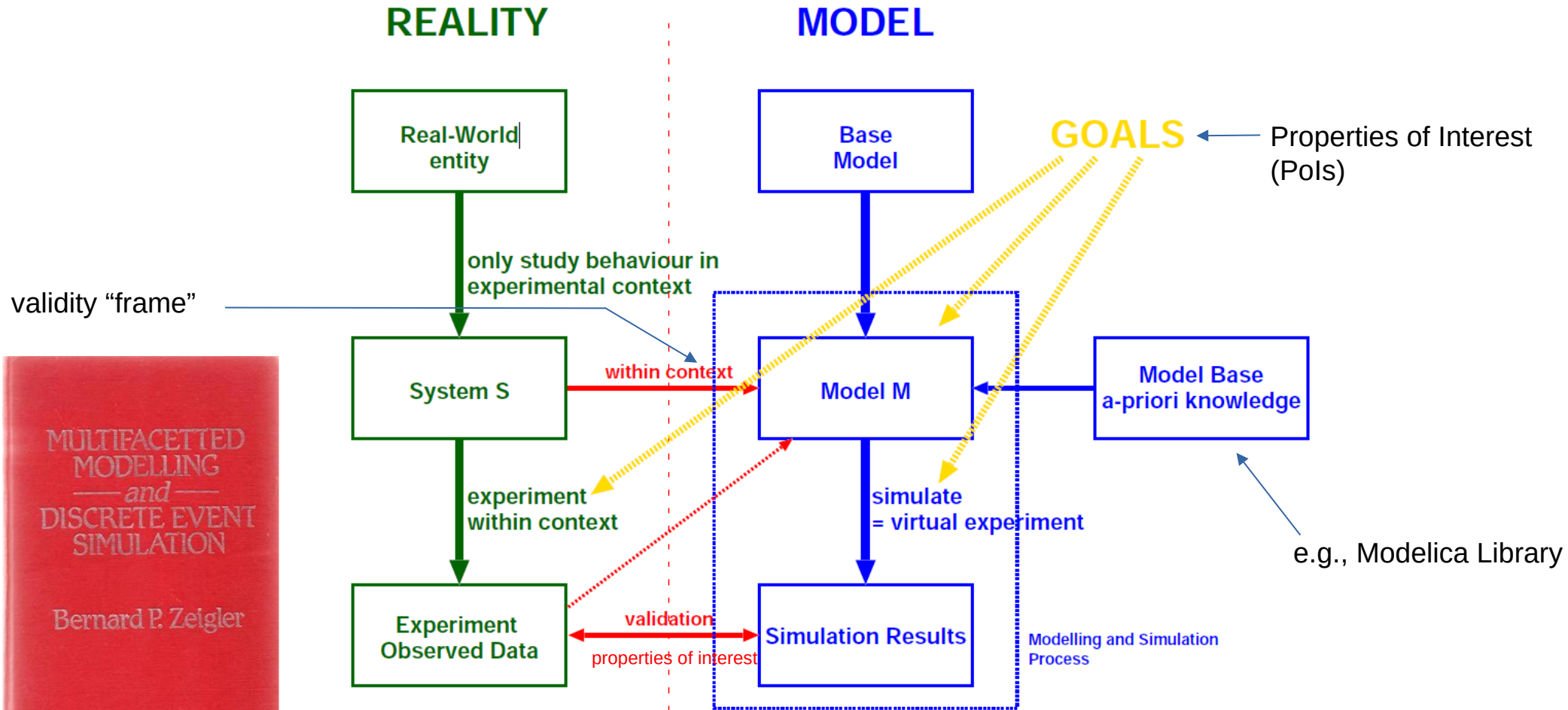
3. for $\{z_f + \sigma \leq z \leq L\}$:

$$\frac{\partial X(z,t)}{\partial t} = - \left[(1 - nX(z,t)) v_0 e^{-nX(z,t)} + \frac{Q_n(t)}{A} \right] \frac{\partial X(z,t)}{\partial z} + D_0 \frac{\partial^2 X(z,t)}{\partial z^2}.$$

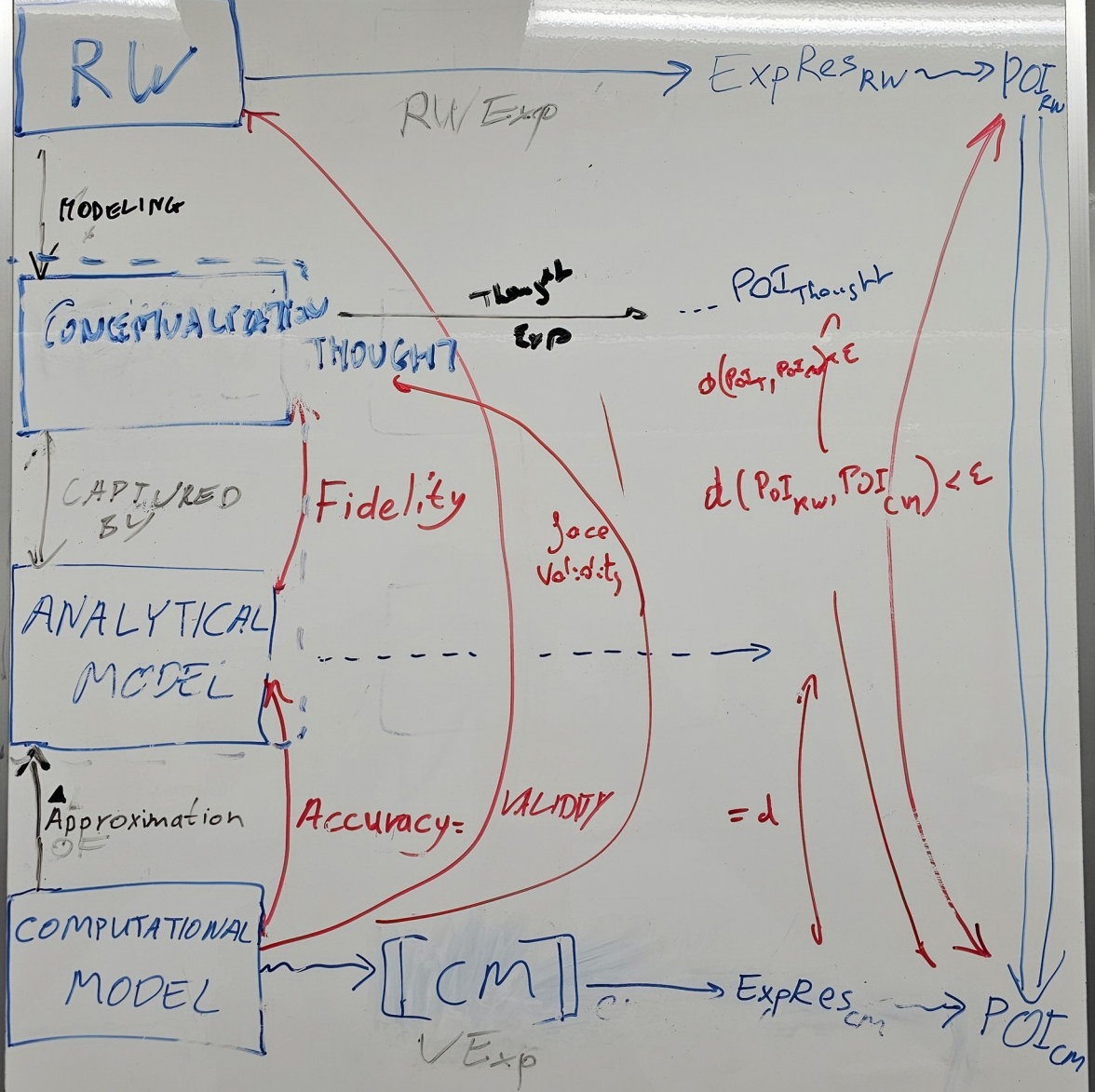




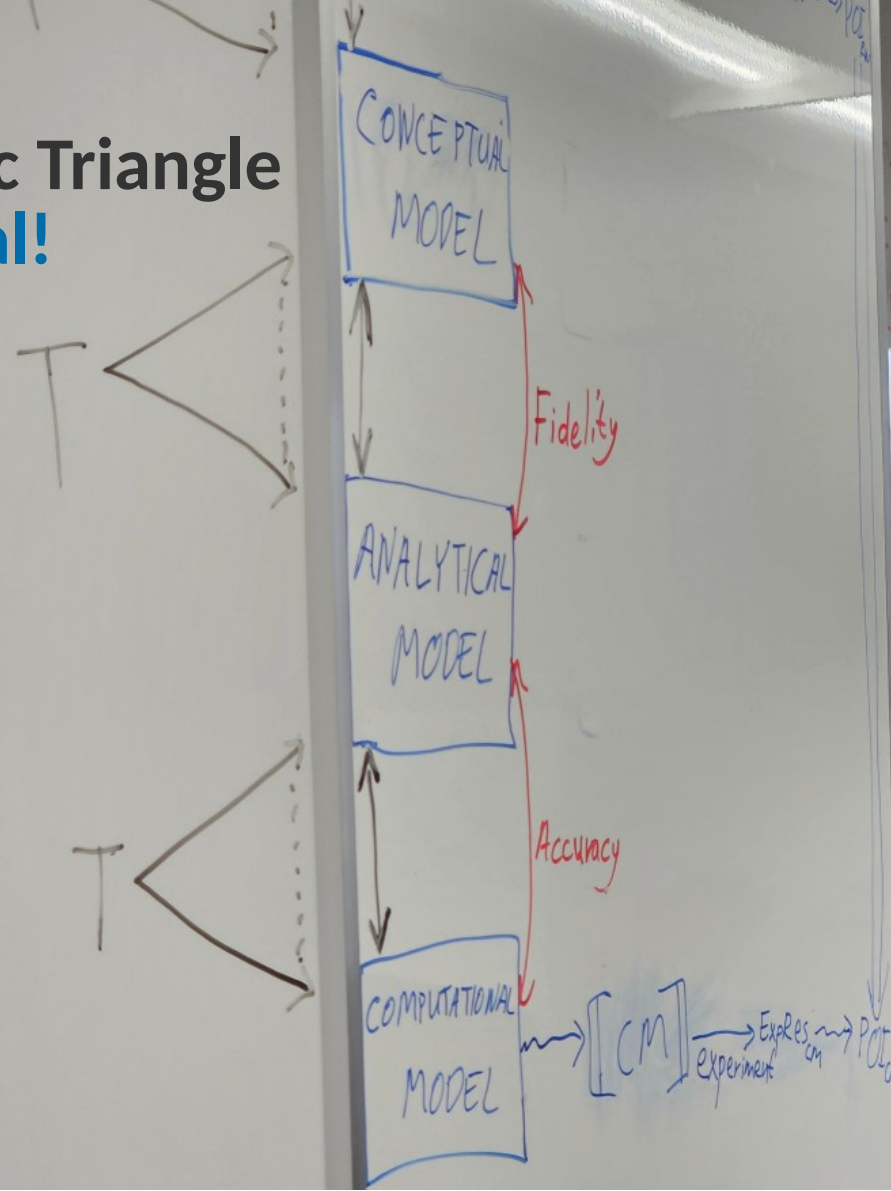
purpose of modelling: substitutability (engineering), explainability (science)



Bernard P. Zeigler. *Multi-faceted Modelling and Discrete-Event Simulation*. Academic Press, 1984.

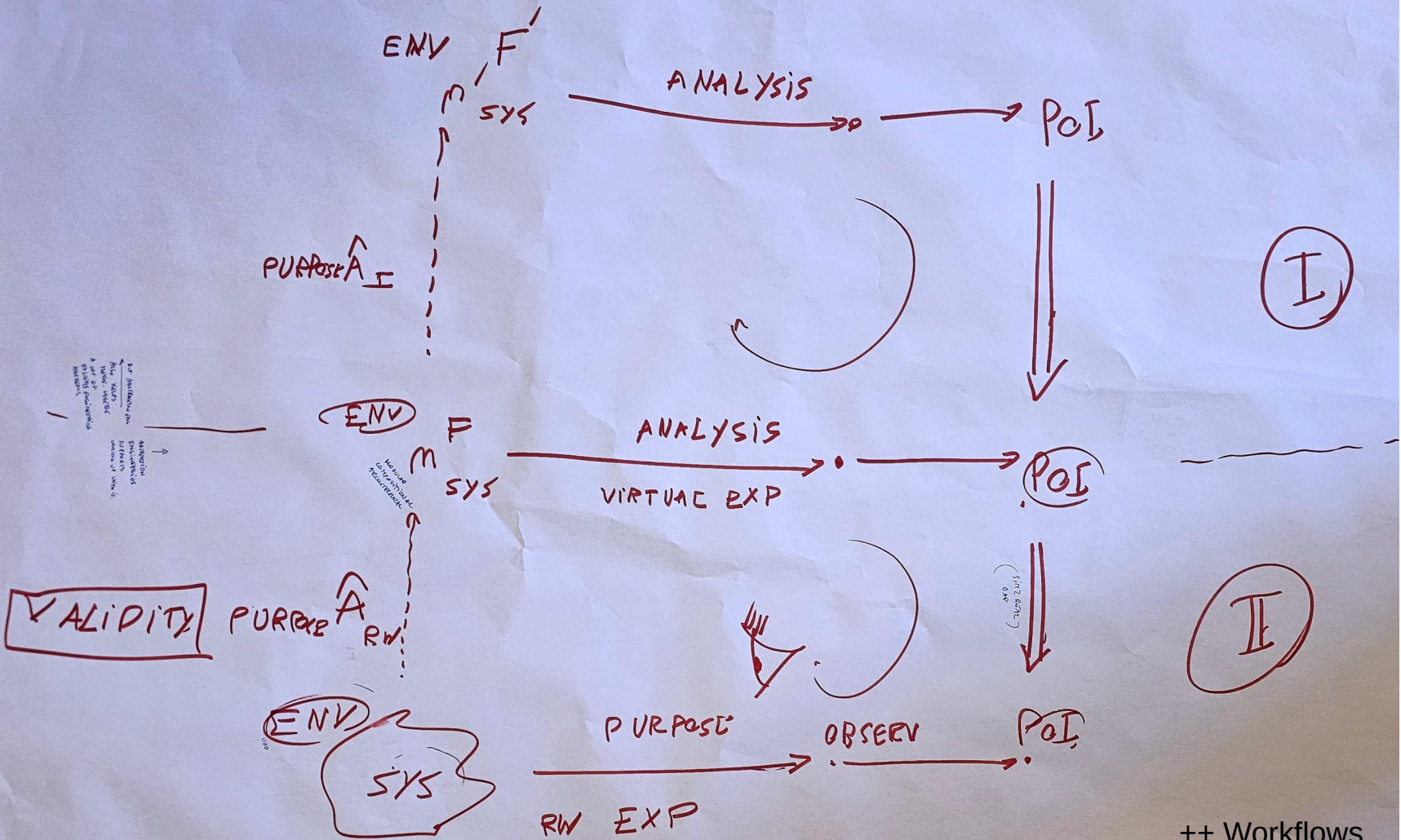


The Semiotic Triangle is orthogonal!



Abstraction \hat{A} is orthogonal!

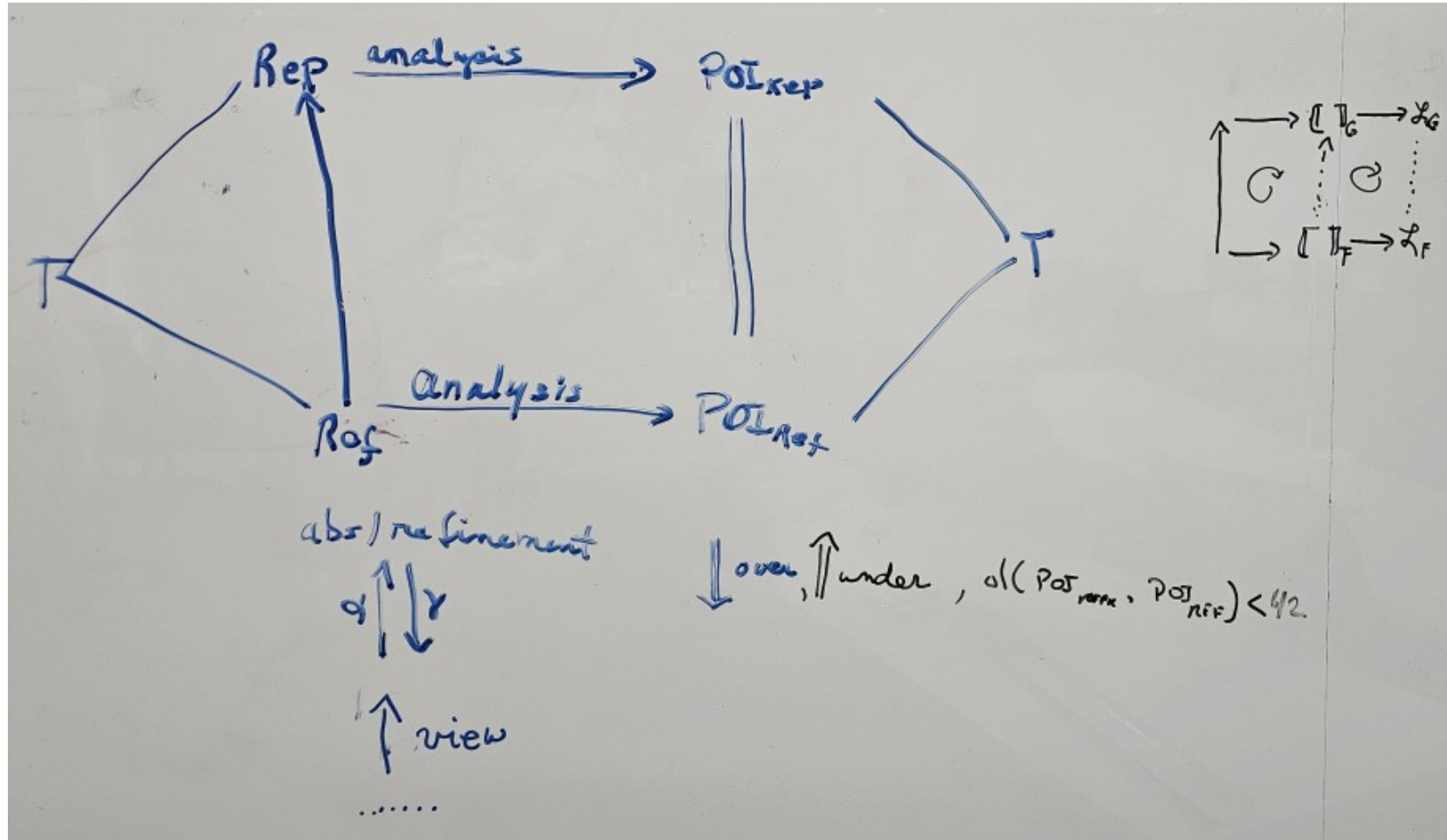




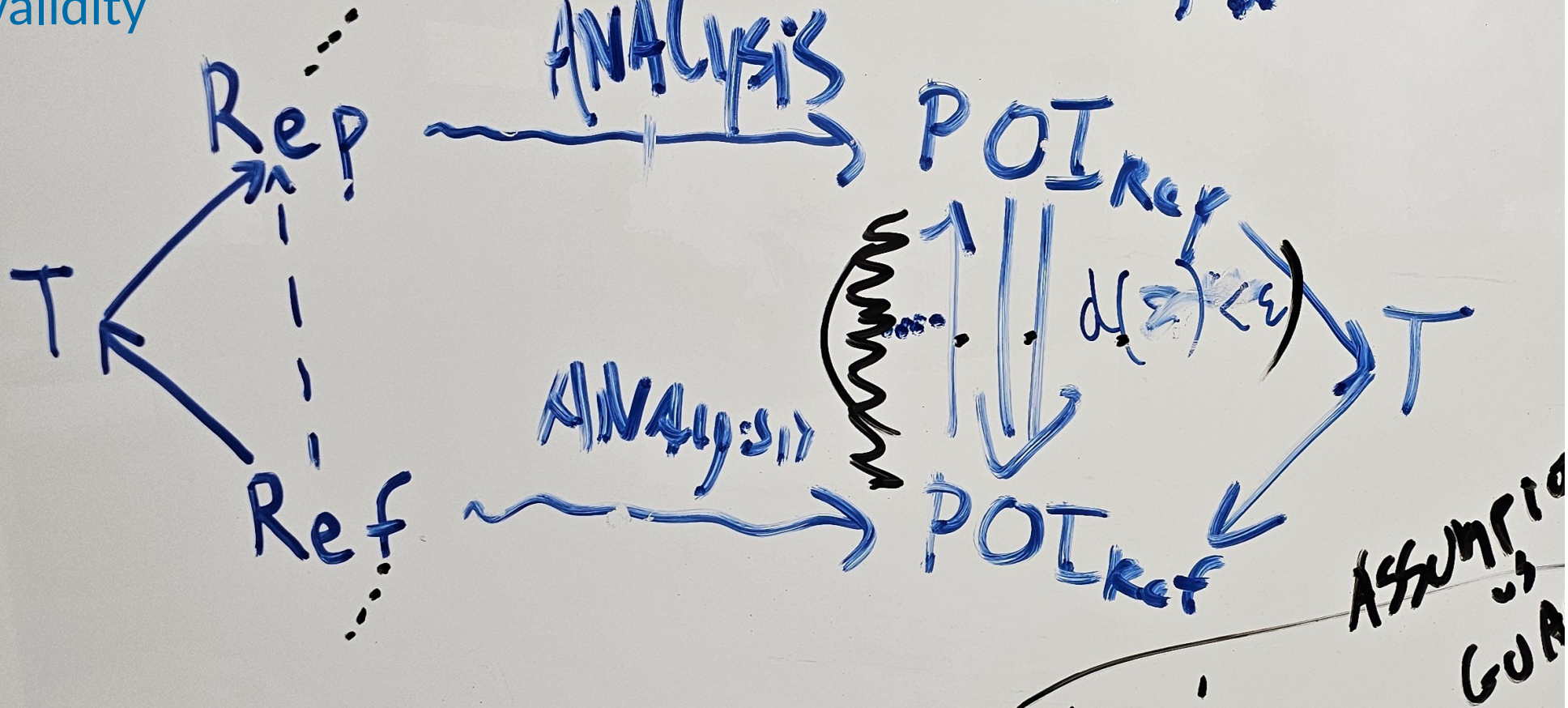
++ Workflows
 ++ Inductive vs. Deductive

Template for

- abstraction
- refinement
- validity



- Template for
- abstraction
 - refinement
 - validity



Multi-*

MULTI - COMPONENT / ARCHITECTURE / ^{Multi} ~~Arch~~ _{Arch}

- ① VIEW
- ② SCALE (TIME, SPACE, ...)
- ③ FORMALISM ←



Consistency
Workflow / life cycle

① Evolution

INDUCTIVE
vs
DEDUCTIVE

PRAGMATICS
REQ. DR. REIN

PRO SOURCE / TEST

④ ABSTRACTION
⑤ ACCURACY / APPROXIMATION
FIDELITY ASSESSMENT
MODELLING (COLLABORATION)

- STAKEHOLDER

LEVEL

- PURPOSE / POI

③ PRODUCT (FAMILIES) ^{variante} _{style}

① DOMAIN ^{conceptualization / PHASIS / words} _{view}

④ KULTI ~~style~~

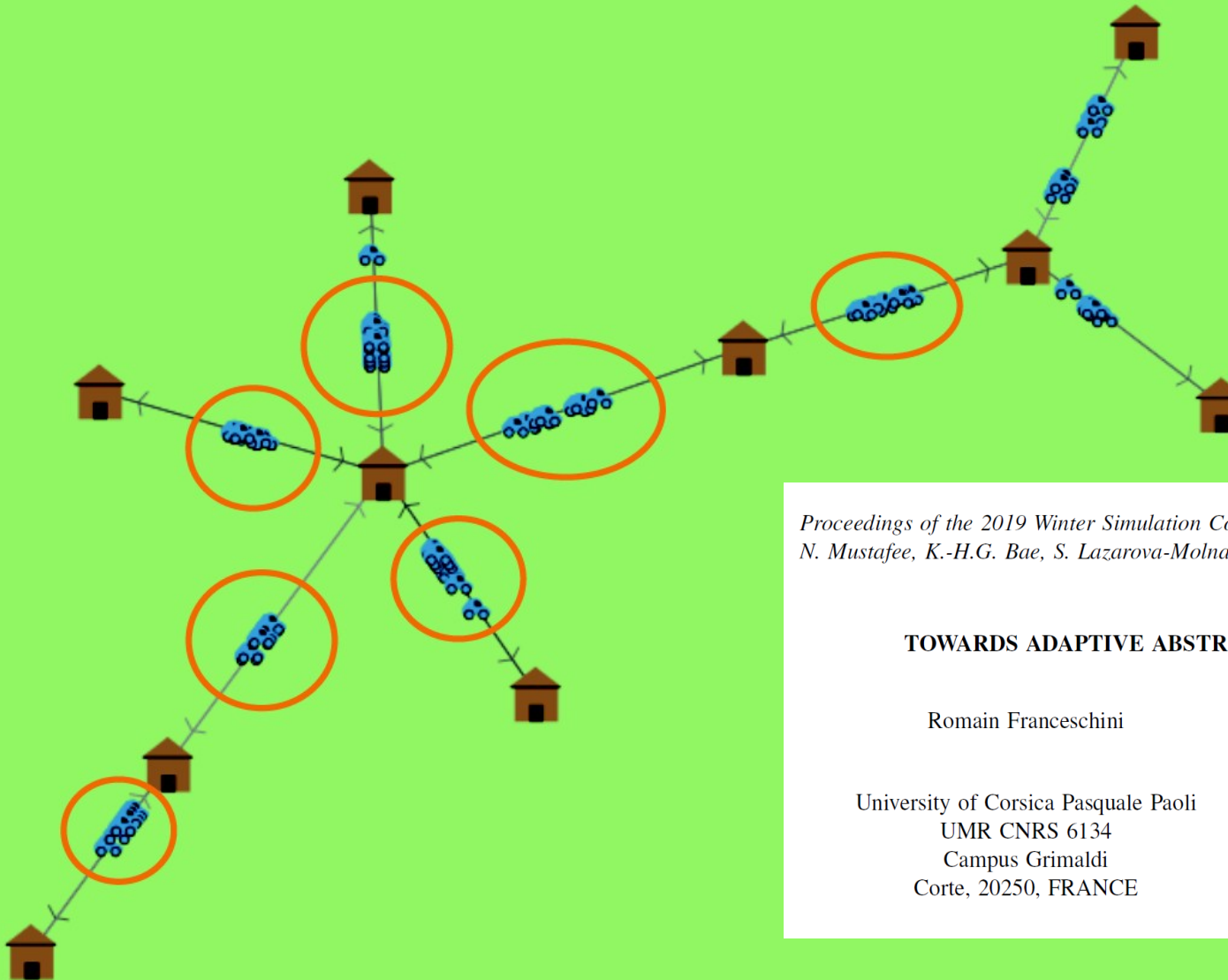
- PLATFORM

② VERSION ^{zeit}

② PREVENANCE / ~~multi product~~
- Phase (life-cycle)

Abstraction

- For performance (scale-ability)
- For insight



Proceedings of the 2019 Winter Simulation Conference

N. Mustafee, K.-H.G. Bae, S. Lazarova-Molnar, M. Rabe, C. Szabo, P. Haas, and Y.-J. Son, eds.

TOWARDS ADAPTIVE ABSTRACTION IN AGENT BASED SIMULATION

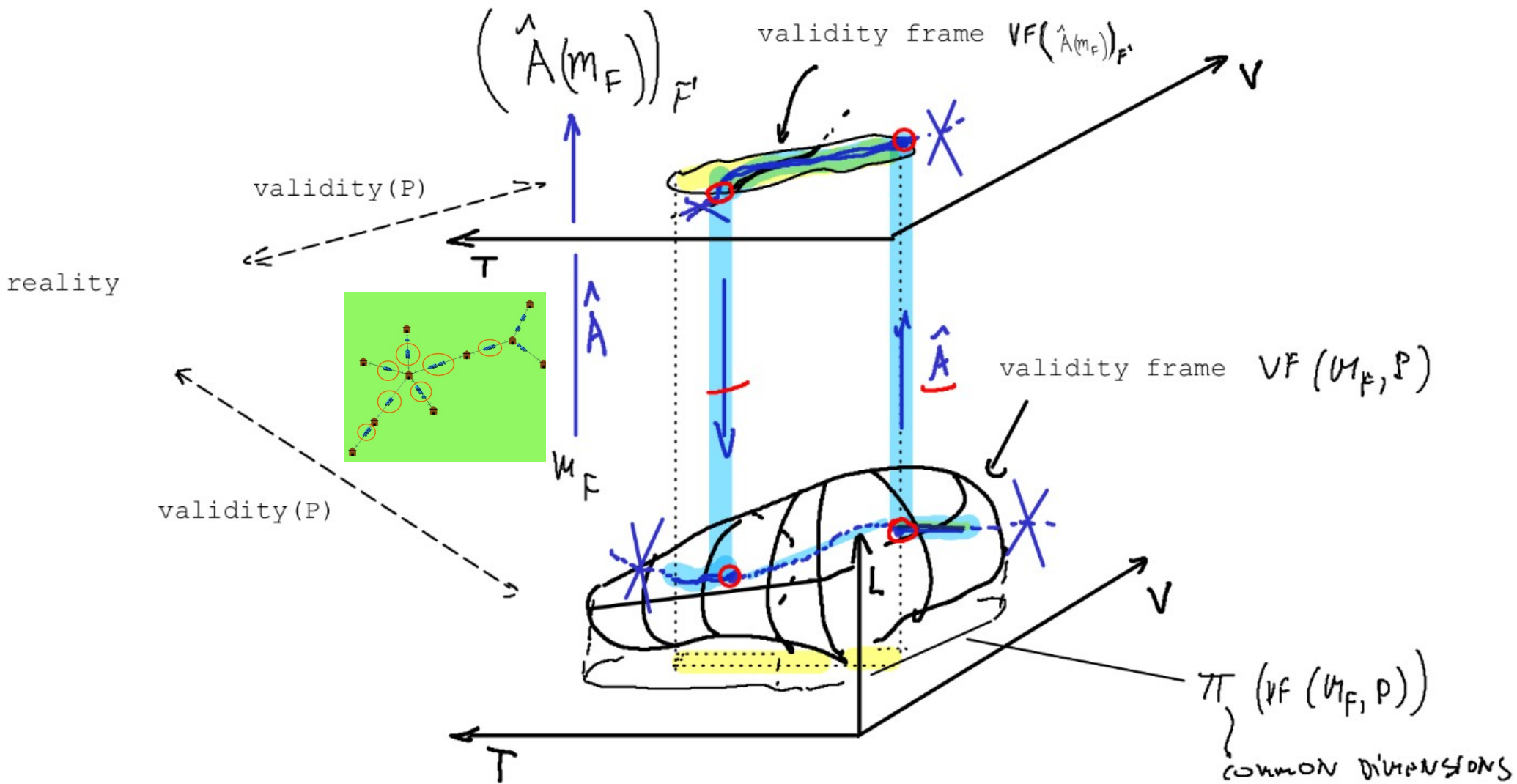
Romain Franceschini

University of Corsica Pasquale Paoli
UMR CNRS 6134
Campus Grimaldi
Corte, 20250, FRANCE

Simon Van Mierlo
Hans Vangheluwe

Department of Mathematics and Computer Science
University of Antwerp - Flanders Make
Middelheimlaan 1
Antwerp, 2020, BELGIUM

properties P



MULTI - COMPONENT / ARCHITECTURE / ^{Multi} _{Acqly}

- ① VIEW
- ② SCALE (TIME, SPACE, ...)

③ FORMALISM ←



Consistency
Workflow / life cycle

④ Evolution

INDUCTIVE
vs
DEDUCTIVE

PRAGMATICS
REQ. DR. REIN

PRO SOURCE / TEST

- ① ABSTRACTION
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- ③ FIDELITY ASSESSMENT
MODELLING (COLLABORATION)

- STAKEHOLDER

- LEVEL

- PURPOSE / POI

③ PRODUCT (FAMILIES) ^{variante} _{style}

④ DOMAIN ^{conceptualization / PHASIS / words} _{view}

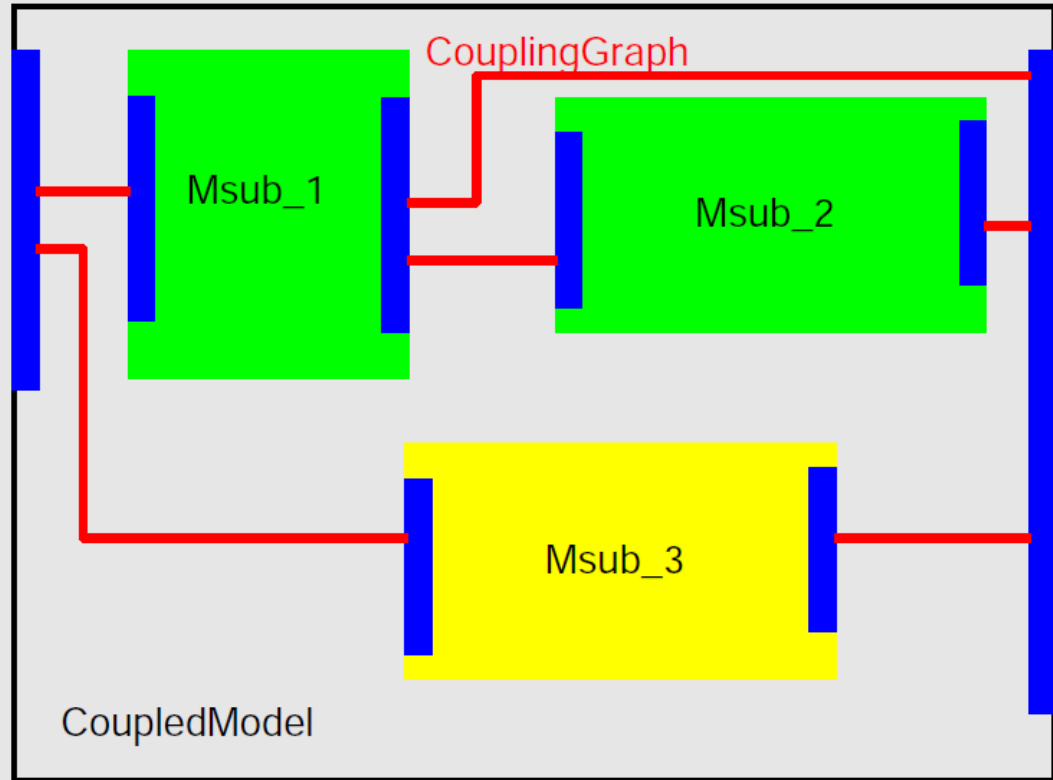
④ KULTI ~~PHASIS~~

- PLATFORM

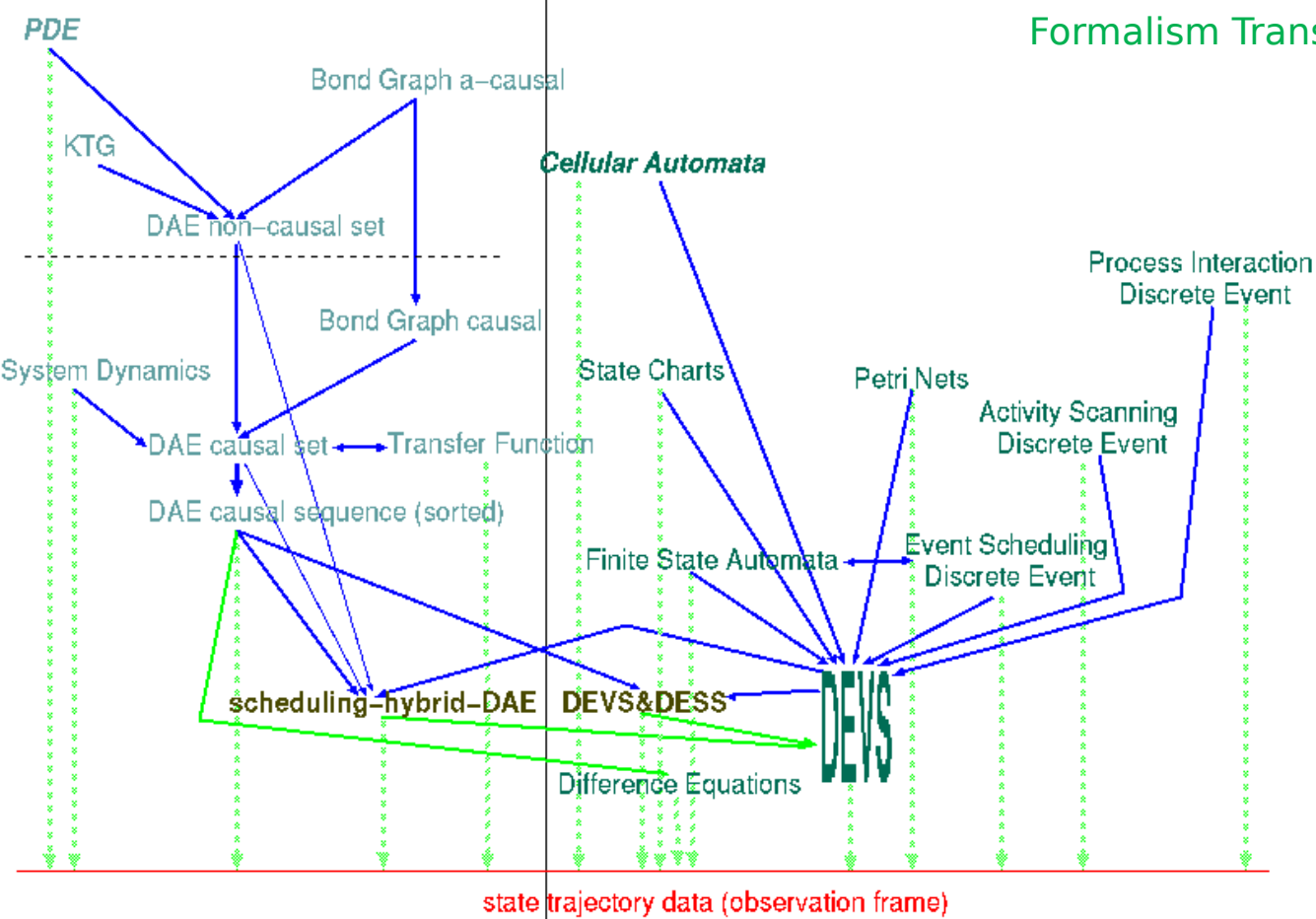
④ VERSION ^{zeitpunkt}

④ PROVENANCE ^{herkunft / produkt}
- Phase (life-cycle)

Multi-formalism coupled model: multi-formalism modelling



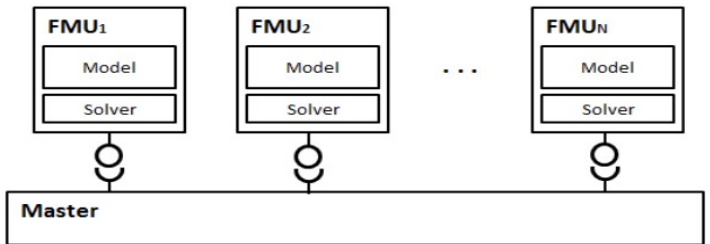
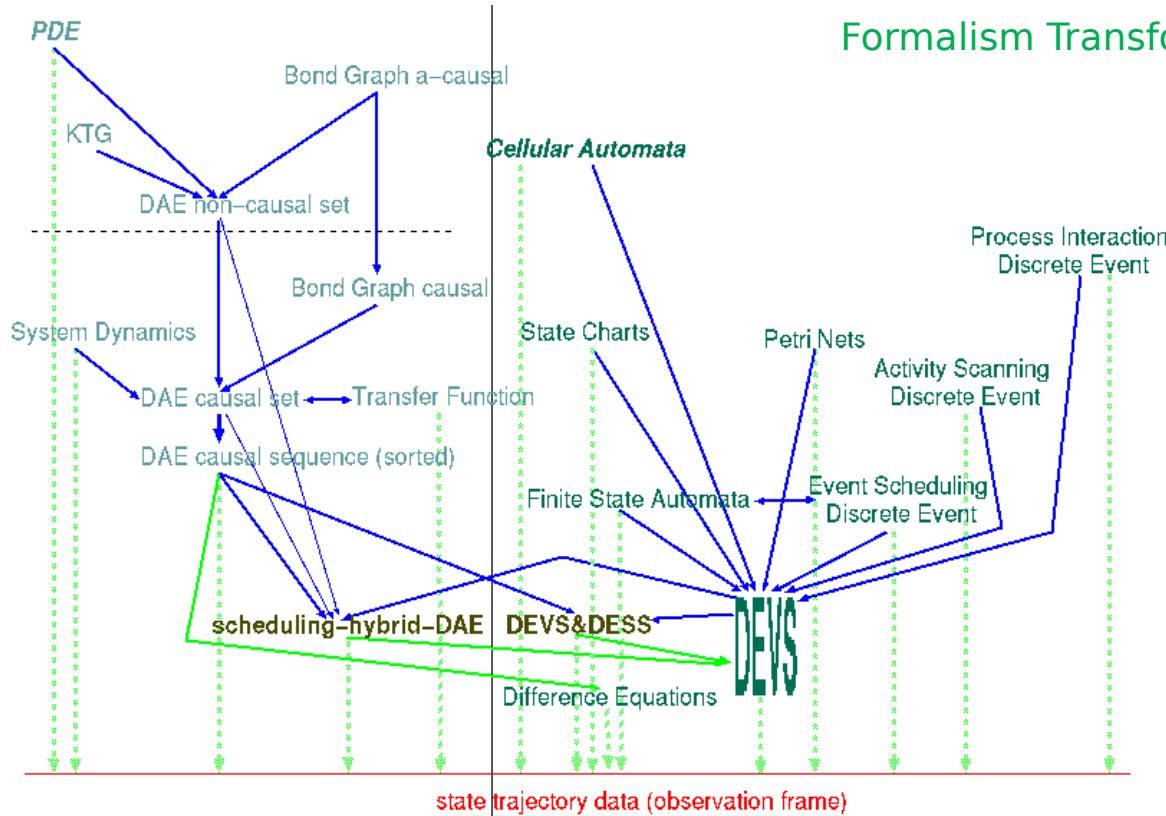
Formalism Transformation Graph (FTG)



Caveat: proving semantics/property preservation of a single transformation (denoted by a blue arrow) may take at least one PhD thesis!

Hans Vangheluwe and Ghislain C. Vansteenkiste. A multi-paradigm modeling and simulation methodology: Formalisms and languages. In European Simulation Symposium (ESS), pages 168 – 172. Society for Computer Simulation International (SCS), October 1996. Genoa, Italy.

Formalism Transformation Graph (FTG) co-simulation



Cláudio Gomes, Casper Thule, David Broman, Peter Gorm Larsen, and Hans Vangheluwe.
Co-simulation: A survey. ACM Computing Surveys (CSUR) , 51(3):49:1-49:33, 2018.

MULTI - COMPONENT / ARCHITECTURE / ^{Multi} _{Archy}

- ① VIEW
- ② SCALE (TIME, SPACE, ...)
- ③ FORMALISM ←



Consistency
Workflow / life cycle

④ Evolution

INDUCTIVE
vs
DEDUCTIVE

PRAGMATICS
REQ. DR. REIN
PRO SOURCE / TEST

- ⑤ ABSTRACTION
- ⑥ ACCURACY / APPROXIMATION
- ⑦ FIDELITY ASSESSMENT
MODELLING (COLLABORATION)

- STAKEHOLDER

- LEVEL

- PURPOSE / POI

⑧ PRODUCT (FAMILIES) ^{variante} _{style}

⑨ DOMAIN ^{conceptualization / PHASIS} _{words view}

⑩ KULTI ~~style~~

- PLATFORM

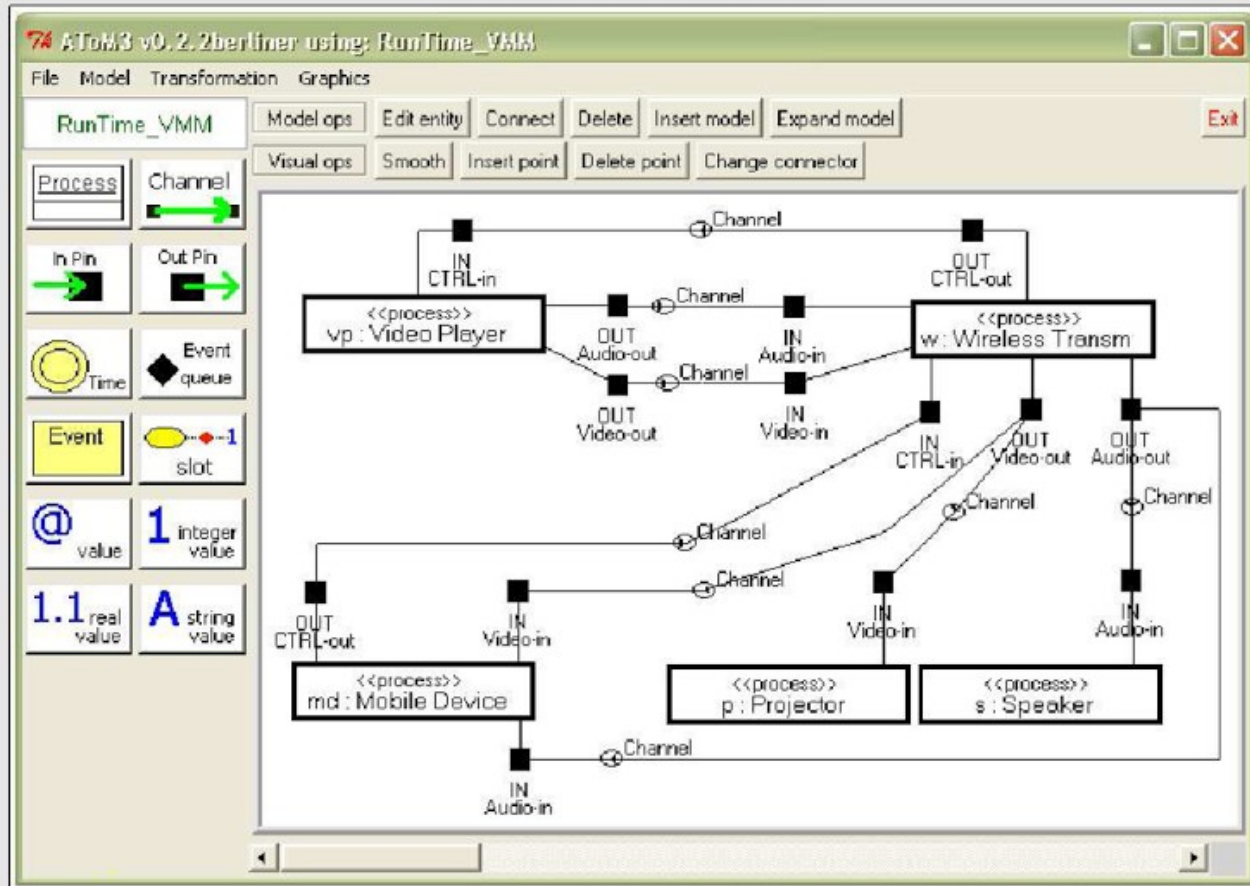
⑪ VERSION ^{zeit}

⑫ PROVENANCE ^{multi / product}
- Phase (life-cycle)

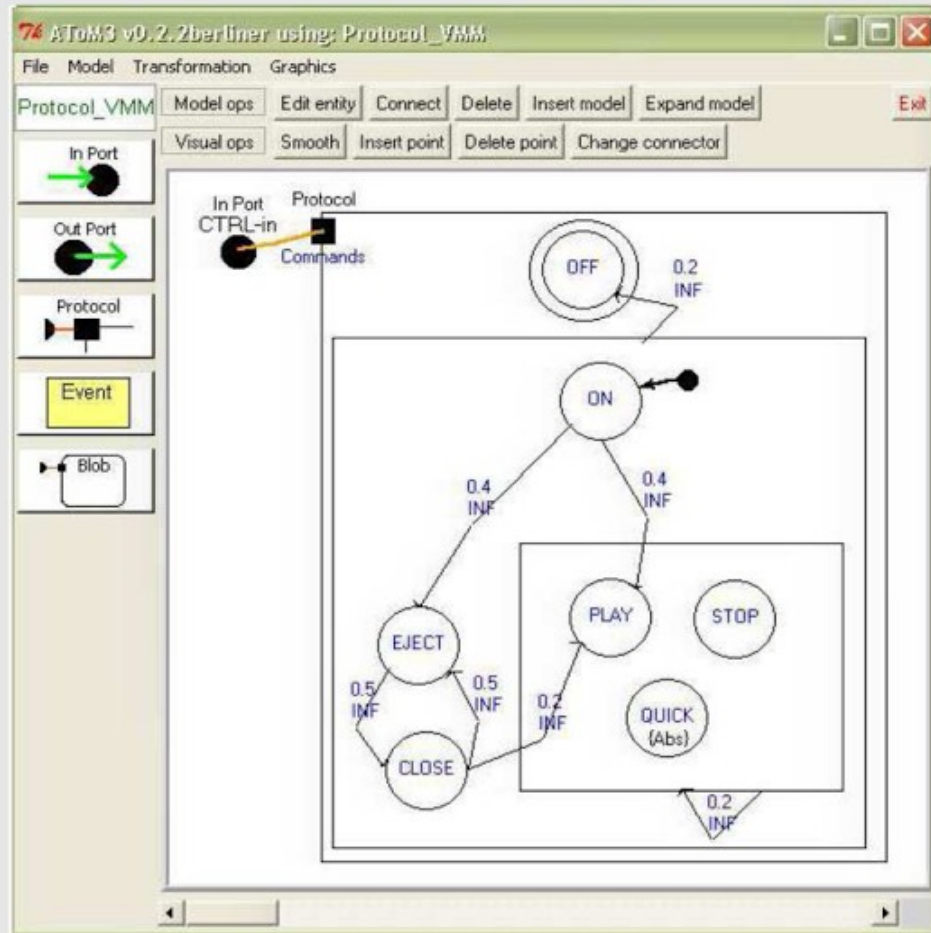
Wireless Home Entertainment System



Multiple (consistent !) Views (in \neq Formalisms)



View: Protocol Statechart

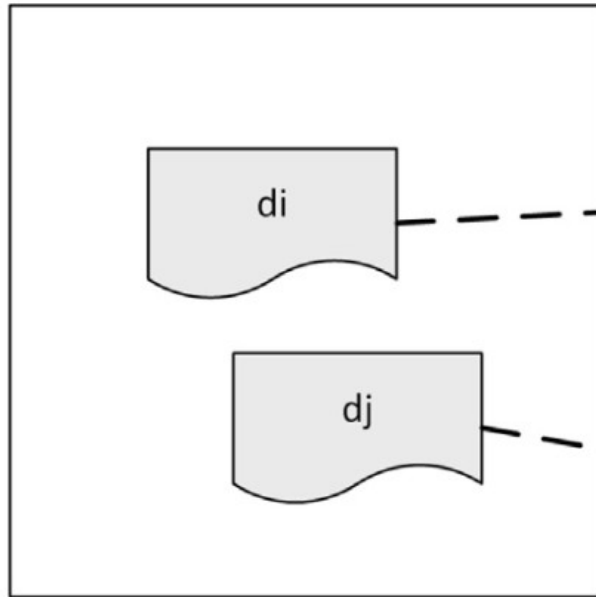




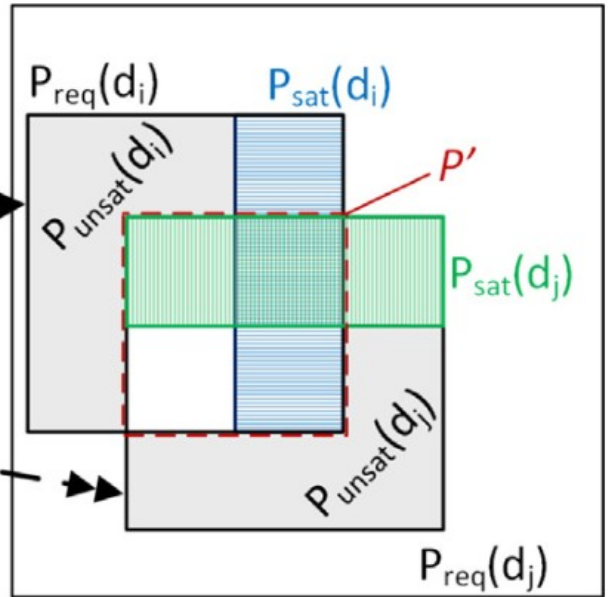
Model consistency as a heuristic for eventual correctness

Istvan David ^{a,*}, Hans Vangheluwe ^{b,c}, Eugene Syriani ^a

Design artifacts D



Properties P



MULTI - COMPONENT / ARCHITECTURE / ^{Multi} ~~Arch~~ _{Arch}

- ① VIEW
- ② SCALE (TIME, SPACE, ...)
- ③ FORMALISM ←



Consistency
Workflow / life cycle

④ Evolution

INDUCTIVE
vs
DEDUCTIVE

PRAGMATICS
REQ. DR. REIN

PRO SOURCE / TEST

- ⑤ ABSTRACTION
- ⑥ ACCURACY / APPROXIMATION
- ⑦ FIDELITY ASSESSMENT
- ⑧ MODELING (COLLABORATION)

- STAKEHOLDER

- LEVEL

- PURPOSE / POI

⑨ PRODUCT (FAMILIES) ^{vari. pr.} _{style}

⑩ DOMAIN ^{conceptualization / PHASIS / words} _{view}

⑪ KULTI ~~PRO~~

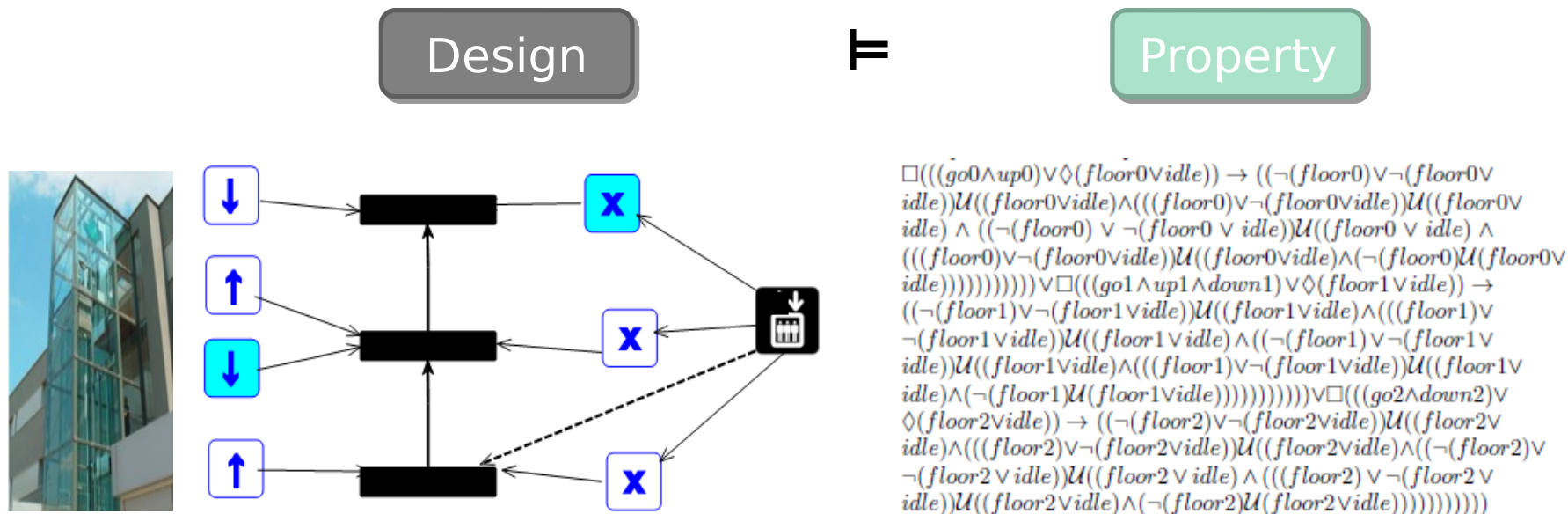
- PLATFORM

⑫ VERSION ²⁰⁰⁰

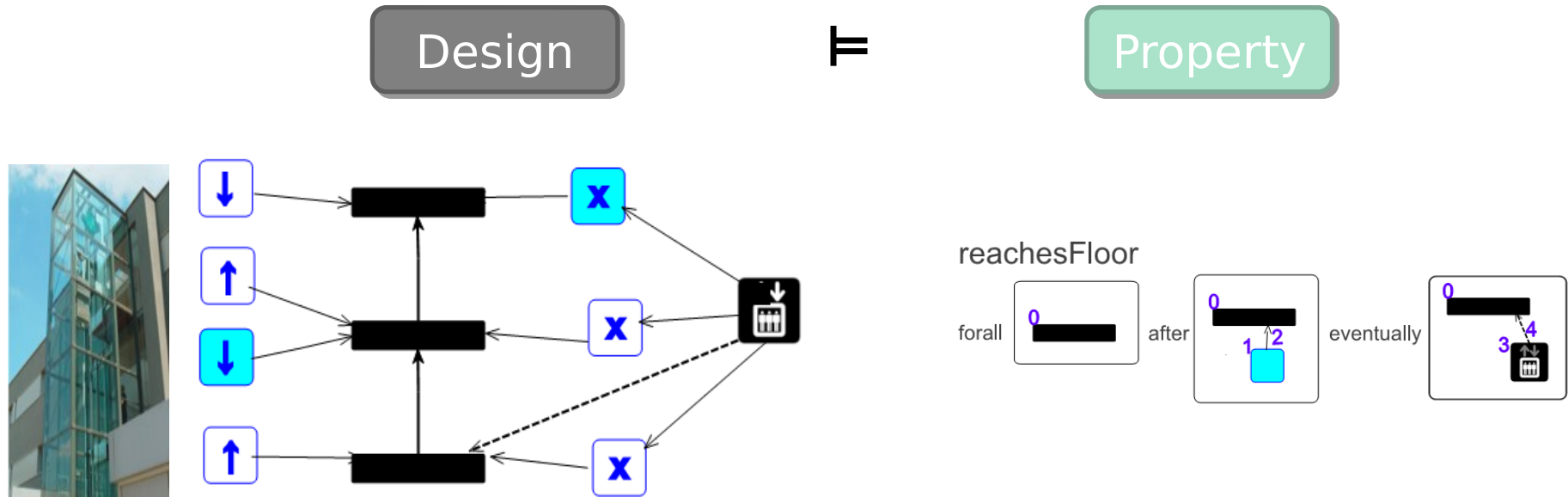
⑬ PROVENANCE ^{multi / product}
- Phase (life-cycle)



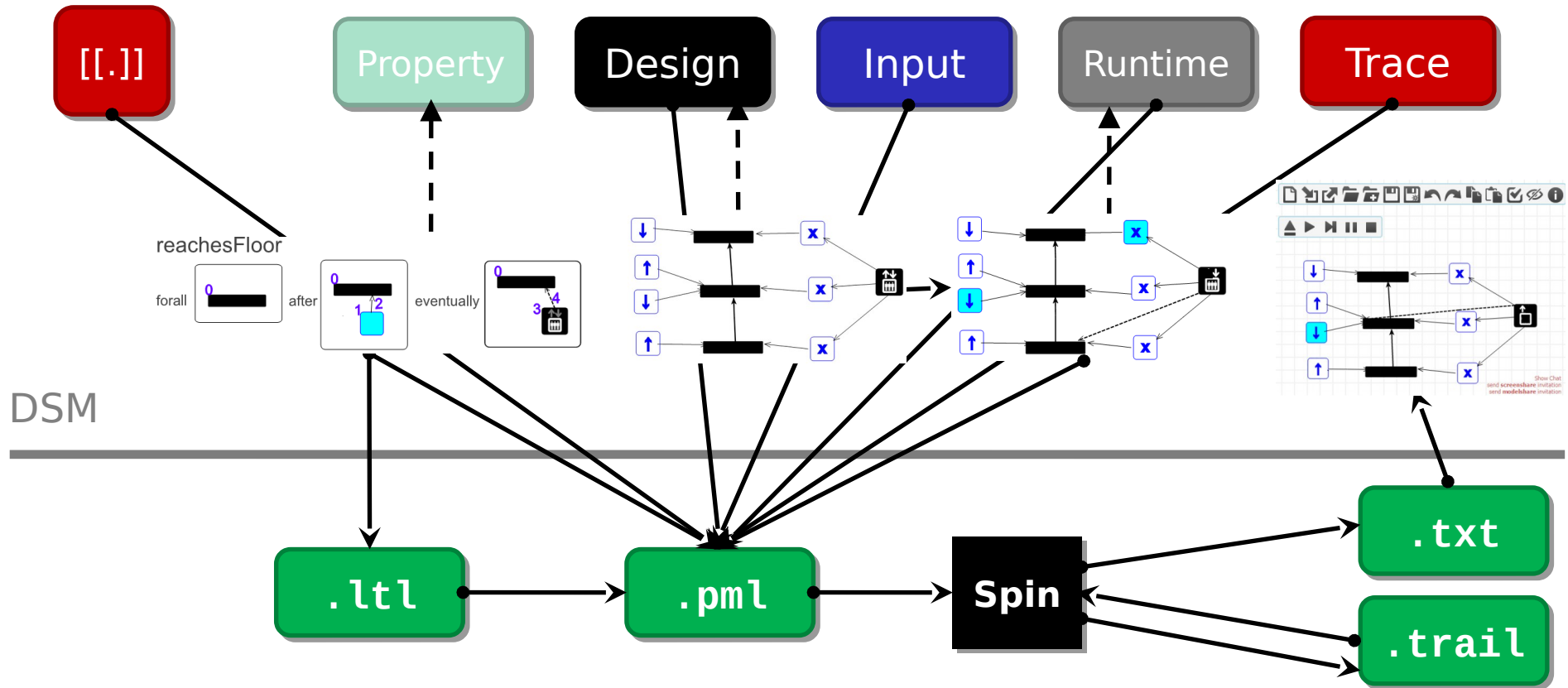
Designing Requirements/Property Languages



Designing Requirements/Property Languages



Designing DS Requirements/Property Languages





MODEL
EVERYTHING!



DSM TP 2014
Theory and Practice

5th International Summer School
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